# Surface effects in solar-like oscillators

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### The problem

## What is the surface effect?



# Why is it a problem?



# What causes it?

basically, poor modelling of near-surface convection see Rosenthal (1997)

(c.f. Böhm-Vitense 1958)



3D RHD simulations (e.g. review by Nordlund et al. 2009)



# What causes it?

Rosenthal (1997)

• "model" physics:

(everything missing from background model)

- MLT gives inaccurate temperature gradient
- no turbulent pressure
- atmospheric structure
- etc...

### • "modal" physics:

(everything missing from oscillation calculation)

- perturbation to turbulent
   pressure (Rosenthal et al. 1999)
- flows modify wave speeds (Brown 1984)
- non-adiabaticity (Houdek 1996)
- etc...

### **Parametrizations**

#### CORRECTING STELLAR OSCILLATION FREQUENCIES FOR NEAR-SURFACE EFFECTS

HANS KJELDSEN,<sup>1</sup> TIMOTHY R. BEDDING,<sup>2</sup> AND JØRGEN CHRISTENSEN-DALSGAARD<sup>1</sup> Received 2008 February 4; accepted 2008 July 9; published 2008 July 28

$$\nu_{\rm obs}(n) - r\nu_{\rm mdl}(n) = a \left[\frac{\nu_{\rm obs}(n)}{\nu_0}\right]^b$$

$$r = (b-1) \left[ b \frac{\nu_{\rm mdl}}{\nu_{\rm obs}} - \frac{\Delta \nu_{\rm mdl}}{\Delta \nu_{\rm obs}} \right]^{-1} \approx \left( \frac{\bar{\rho}_{\rm mdl}}{\bar{\rho}_{\rm obs}} \right)^2$$



### A new correction of stellar oscillation frequencies for near-surface effects

W. H. Ball<sup>1</sup> and L. Gizon<sup>2,1</sup>

from asymptotic behaviour of eigenfunctions near surface + sound speed or  $H_p$  perturbation

"cubic" term:  

$$\nu_{\rm obs} - \nu_{\rm mdl} = a_3 \nu^3 / \mathcal{I}$$

"combined" term:  

$$\nu_{\rm obs} - \nu_{\rm mdl} = (a_{-1}\nu^{-1} + a_3\nu^3)/\mathcal{I}$$

c.f. Gough (1990)

cubic term also in Libbrecht & Woodard (1990) and Goldreich et al. (1991)



### Surface-effect corrections for solar-like oscillations using 3D hydrodynamical simulations

#### I. Adiabatic oscillations

T. Sonoi<sup>1</sup>, R. Samadi<sup>1</sup>, K. Belkacem<sup>1</sup>, H.-G. Ludwig<sup>2,3</sup>, E. Caffau<sup>3</sup>, and B. Mosser<sup>1</sup>



### Power law correction

Kjeldsen et al. (2008)



# **Cubic correction**

Ball & Gizon (2014)



# **Combined correction**

Ball & Gizon (2014)



# Modified Lorentzian correction

Sonoi et al. (2015)



### Astronomy Astrophysics

### The ratio of small to large separations of acoustic oscillations as a diagnostic of the interior of solar-like stars

I. W. Roxburgh<sup>1,2</sup> and S. V. Vorontsov<sup>1,3</sup>

$$r_{02}(n) = \frac{\nu_{n,0} - \nu_{n-1,2}}{\nu_{n,1} - \nu_{n-1,1}}$$
$$r_{13}(n) = \frac{\nu_{n,1} - \nu_{n-1,3}}{\nu_{n+1,0} - \nu_{n,0}}$$

$$r_{01}(n) = \frac{1}{8} \frac{\nu_{n-1,0} - 4\nu_{n-1,1} + 6\nu_{n,0} - 4\nu_{n,1} + \nu_{n+1,0}}{\nu_{n,1} - \nu_{n-1,1}}$$
$$r_{10}(n) = -\frac{1}{8} \frac{\nu_{n-1,1} - 4\nu_{n,0} + 6\nu_{n,1} - 4\nu_{n+1,0} + \nu_{n+1,1}}{\nu_{n+1,0} - \nu_{n,0}}$$



### The ratio of small to large separations of acoustic oscillations as a diagnostic of the interior of solar-like stars

I. W. Roxburgh<sup>1,2</sup> and S. V. Vorontsov<sup>1,3</sup>

$$r_{02}(n) =$$
  
 $r_{13}(n) =$   $r_{13}(n) =$   $r_{13}(n) =$   $r_{13}(n) =$   $r_{13}(n) =$ 

$$r_{01}(n) = \begin{cases} five-point difference \\ large separation \end{cases}$$

(also visit Roxburgh's poster comparing his various methods)

# Separation ratios

Roxburgh & Vorontsov (2003)



# State of the art

- Parametrizations
  - ratios widely used and presumably reliable
  - "combined" term appears the best formula
  - Sun is still the only real test

Schmitt & Basu (2015)

# Three-dimensional radiation hydrodynamics



### Three-dimensional simulations of near-surface convection in main-sequence stars\*

B. Beeck<sup>1,2</sup>, R. H. Cameron<sup>1</sup>, A. Reiners<sup>2</sup>, and M. Schüssler<sup>1</sup>

G2V

F3V



K0V





1<sup>5</sup> x [Mm]



### **Convective contributions to the frequencies of solar oscillations**

C.S. Rosenthal<sup>1,\*</sup>, J. Christensen-Dalsgaard<sup>1,2</sup>, Å. Nordlund<sup>3,4</sup>, R.F. Stein<sup>5</sup>, and R. Trampedach<sup>1,2</sup>



#### Models of solar surface dynamics: impact on eigenfrequencies and radius

L. Piau,<sup>1</sup>\* R. Collet,<sup>2</sup> R. F. Stein,<sup>3</sup> R. Trampedach,<sup>4</sup> P. Morel<sup>5</sup> and S. Turck-Chièze<sup>6</sup>



### Surface-effect corrections for the solar model



A&A 583, A112 (2015) DOI: 10.1051/0004-6361/201526838 © ESO 2015



### Surface-effect corrections for solar-like oscillations using 3D hydrodynamical simulations

#### I. Adiabatic oscillations

T. Sonoi<sup>1</sup>, R. Samadi<sup>1</sup>, K. Belkacem<sup>1</sup>, H.-G. Ludwig<sup>2,3</sup>, E. Caffau<sup>3</sup>, and B. Mosser<sup>1</sup>

### CESTAM + CO<sup>5</sup>BOLD

### **MESA** meets MURaM

### Surface effects in main-sequence solar-like oscillators computed using three-dimensional radiation hydrodynamics simulations

W. H. Ball<sup>1,2</sup>, B. Beeck<sup>2</sup>, R. H. Cameron<sup>2</sup>, and L. Gizon<sup>2,1</sup>

(A&A accepted, arXiv:1606.02713)

### MESA + MURaM

# Simulation parameters

Sonoi et al. (2015), Ball et al. (2016)



# Solar-calibrated model (Model S)

Ball et al. (2016)



# All four models

Ball et al. (2016)







# State of the art

- Parametrizations
  - ratios widely used; phase-matching very new
  - "combined" term appears the best formula
  - Sun is still the only real test
- 3D RHD simulations
  - "patching" models seems reliable
  - results are robust
  - currently limited to structural effects

### The future

# The future

- Make more of the 3D RHD simulations
  - "modal" physics: flows, non-adiabaticity, etc.
  - calibrating mixing length parameter helps too

# The future

- Make more of the 3D RHD simulations
  - "modal" physics: flows, non-adiabaticity, etc.
  - calibrating mixing length parameter helps too
- Push observations to lower radial order
  - best nominal Kepler data almost there
  - velocity data from SONG



# Additional slides

# **Combining models**



# **Combining models**



#### CORRECTING STELLAR OSCILLATION FREQUENCIES FOR NEAR-SURFACE EFFECTS

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$$\nu_{\rm obs}(n) - r\nu_{\rm mdl}(n) = a \left[\frac{\nu_{\rm obs}(n)}{\nu_0}\right]^b$$





### Asteroseismic model fitting by comparing $\epsilon_{n\ell}$ values

Ian W. Roxburgh

$$\epsilon_{\ell}^{\text{obs}}(\nu) = \nu / \Delta \nu^{\text{obs}} - n - \ell / 2$$
  

$$\epsilon_{\ell}^{\text{mdl}}(\nu) = \nu / \Delta \nu^{\text{mdl}} - n - \ell / 2$$
  

$$\mathcal{E}(\ell, \nu) = \epsilon_{\ell}^{\text{mdl}}(\nu) - \epsilon_{\ell}^{\text{obs}}(\nu)$$

$$\chi^{2} = \frac{1}{N_{\rm obs} - M} \sum^{N_{\rm obs}} \left( \frac{\mathcal{E}(\ell, \nu_{n\ell} {}_{n\ell}^{\rm obs}) - \mathcal{F}(\nu_{n\ell}^{\rm obs})}{\sigma_{n\ell}/\Delta\nu} \right)^{2}$$

 $\mathcal{F}(\nu)$  is an *M*-degree polynomial

see also Roxburgh (2015; A&A 574, A45)



# **Epsilon matching**



# **Epsilon** matching



**Fig. 3.** Superposed curves for the outer phase shifts  $\alpha_{\ell}(v, t)$  of Model A at 3 frequencies. The values of  $\alpha_{\ell}$  are independent of  $\ell$  until deep inside the star.

THE ASTROPHYSICAL JOURNAL, 342: L95–L98, 1989 July 15 © 1989. The American Astronomical Society. All rights reserved. Printed in U.S.A.

#### TOPOLOGY OF CONVECTION BENEATH THE SOLAR SURFACE

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AND

Å. NORDLUND Copenhagen University Observatory Received 1989 March 9; accepted 1989 April 14



FIG. 1.—Simulated snapshots of integrated radiation surface intensity. These approximate monochromatic continuum intensity snapshots. Each snapshot is  $6 \times 6$  Mm ( $8'' \times 8''$ ). The sequence, spanning 12 minutes, approximates a  $6 \times 24$  Mm image of the Sun.

# Non-local convection and non-adiabaticity



# Lower radial order with SONG?





# Comparing parametrizations: G2



# Comparing parametrizations: F3



# Solar oscillations

Sun (VIRGO)



# Echelle diagram

16 Cyg A (Kepler)



## **Displacement eigenfunctions**



# **Displacement eigenfunctions**





Simulation	F3V	G2V	K0V	K5V	M0V	M2V
Box height [Mm]	9	3	1.8	1.5	0.9	0.8
above $z_0^a$	1.57	0.95	0.48	0.41	0.25	0.21
below $z_0$	7.43	2.05	1.32	1.09	0.65	0.59
# of pressure scale heights	13.1	14.0	13.2	15.3	14.8	14.5
above $z_0$	6.9	8.6	7.1	9.1	8.4	7.8
below $z_0$	6.2	5.4	6.2	6.4	6.4	6.8
$H_{\rm p}$ at $z_0$ [km]	500	200	90	65	38	35
$\Delta z^{b}$ [km]	11.25	10	6	5	4	3.2
$\min(H_p)/\Delta z$	18.1	10.0	9.57	7.87	6.53	7.19
Horizontal box size [Mm]	30	9	6	4	2.5	1.56
$\Delta x, \Delta y^c$ [km]	58.6	17.6	11.7	7.81	4.88	3.05
$\Delta x/\Delta z$	5.21	1.76	1.95	1.56	1.22	0.953

B. Beeck et al.: 3D simulations of near-surface convection in main-sequence stars. I.

Table 2. Box sizes and grid resolutions.

**Notes.** <sup>(a)</sup>  $z_0 = \langle z(\tau_R = 1) \rangle$ ; <sup>(b)</sup>  $\Delta z$  is the vertical grid resolution; <sup>(c)</sup>  $\Delta x$  and  $\Delta y$  are the horizontal grid resolution; in all simulations considered here,  $\Delta x = \Delta y$  was chosen.

# GAIA







# PLATO



# Solar Oscillations Network Group





 $T_{\rm eff} = 6725 \,\mathrm{K}$  $\log g = 4.25$ 

 $T_{\rm eff} = 5775 \,\mathrm{K}$  $\log g = 4.44$