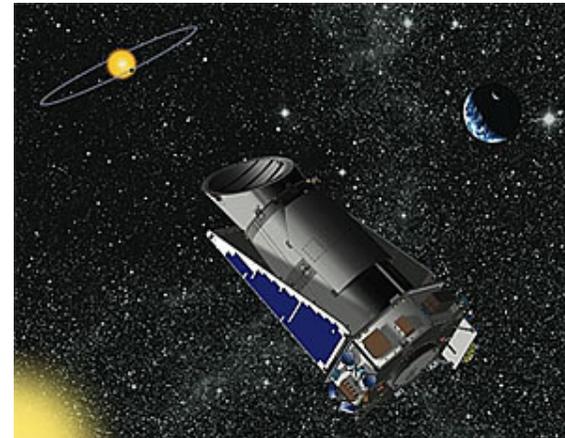


What the seismology of red giants is teaching us about stellar physics

S. Deheuvels



Introduction

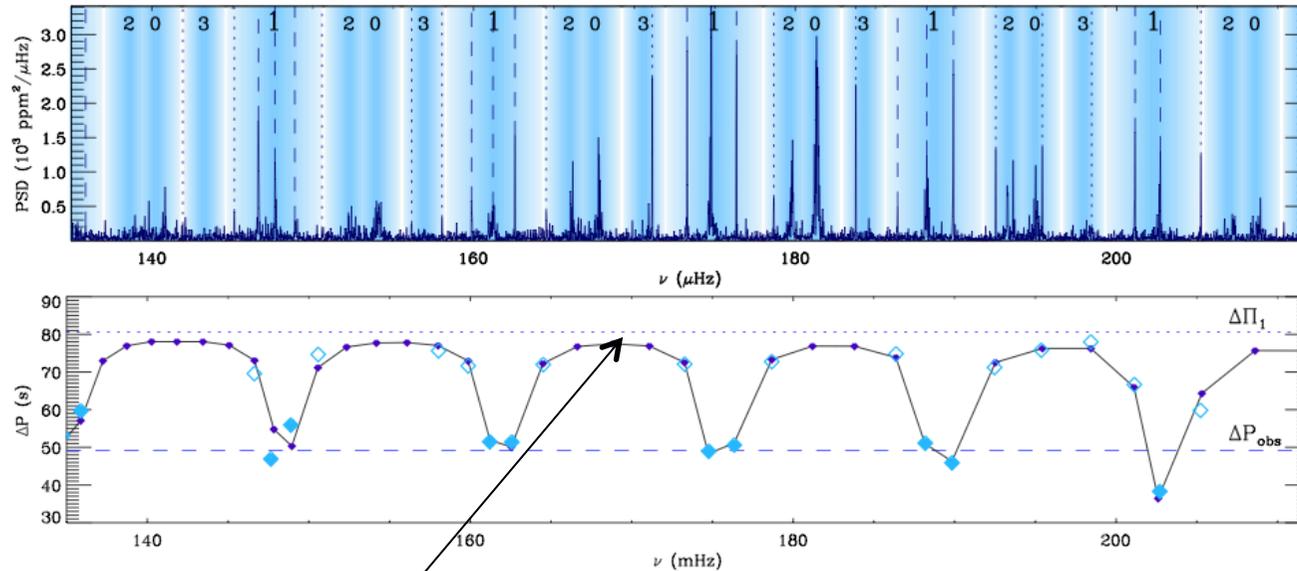
- Red giant phase is **a tumultuous stage of stellar evolution**
 - ⇒ evolution of red giants critically depends on several ill-understood physical processes (**mixing of chemical elements, transport of angular momentum, rotation...**)
 - ⇒ powerful tools to better understand these processes!
- **Seismology of red giants**
 - Detection of non-radial modes in red giants (**de Ridder et al. 2009**)
 - Stochastically-excited modes detected in $\sim 20,000$ red giants (CoRoT + Kepler)
 - Large diagnostic potential of mixed modes

Outline

- Understanding the oscillation spectra of giants
- Probing the convective cores of core-He-burning giants
- Monitoring stellar evolution using mixed modes
- Toward a better understanding of angular momentum transport in stars

Understanding red giant oscillation spectra

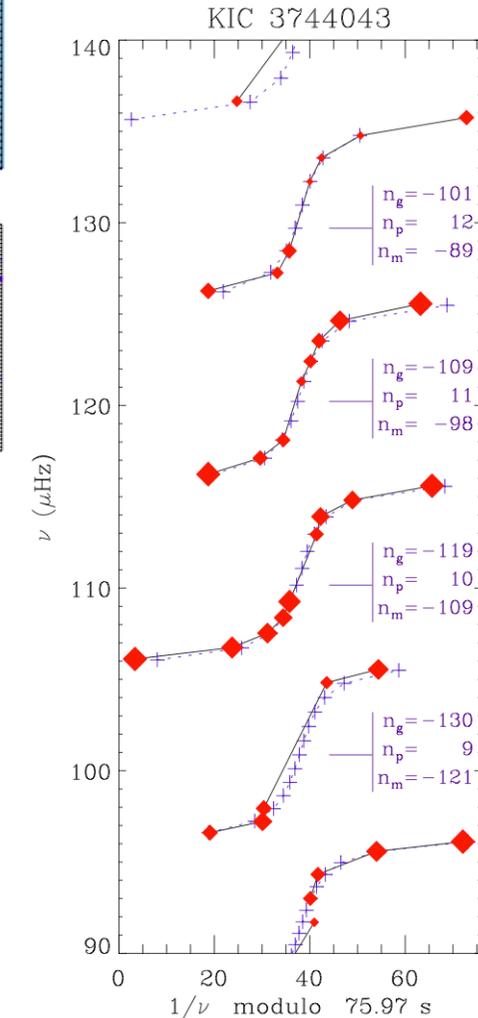
Mosser et al. (2012)



$$\Delta\Pi_1 = \frac{2\pi^2}{\sqrt{2}} \left[\int_{\text{core}} \frac{N_{\text{BV}}}{r} dr \right]^{-1} \quad N^2 = \frac{g}{H_P} (\nabla_{\text{ad}} - \nabla + \nabla_{\mu})$$

- Several methods to estimate $\Delta\Pi_1$ (Mosser et al. 2012, Datta et al. 2015, Vrad et al. 2016)

Period échelle diagram



“Stretched” period échelle diagrams

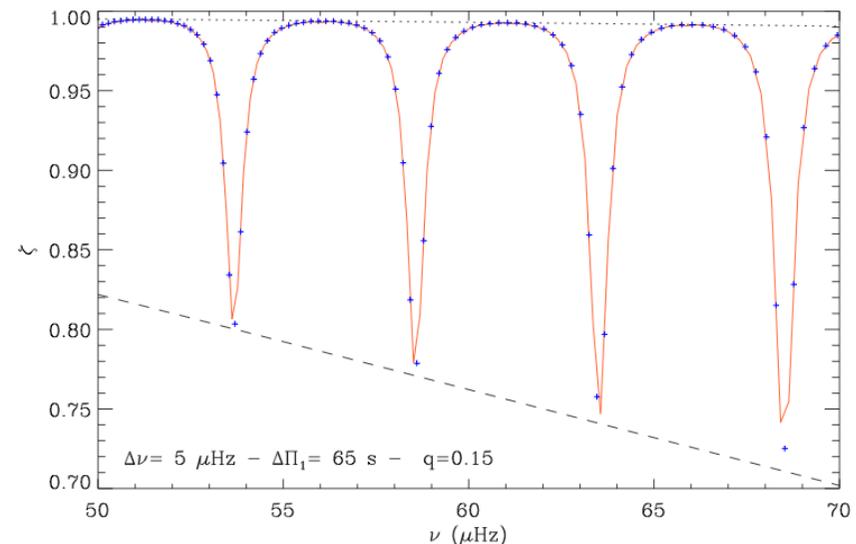
- Ratios of inertia $\zeta \equiv \frac{I_g}{I} = \frac{\int_{\text{g-cav}} |\xi|^2 dm}{\int_0^M |\xi|^2 dm}$

- Approximate expression for ζ from WKB analysis (Goupil et al. 2013, Deheuvels et al. 2015)

$$\tilde{\zeta} = \left\{ 1 + \frac{1}{q} \frac{\cos^2 \left[\pi \left(\frac{1}{v \Delta \Pi_1} - \varepsilon_g \right) \right]}{\cos^2 \left[\pi \frac{(v - v_p)}{\Delta v} \right]} \frac{v^2 \Delta \Pi_1}{\Delta v} \right\}^{-1}$$

- Idea: introduce a “modified” period τ to force a regular spacing of modes in period (Mosser et al. 2015)

$$d\tau = \frac{dP}{\zeta}$$



“Stretched” period échelle diagrams

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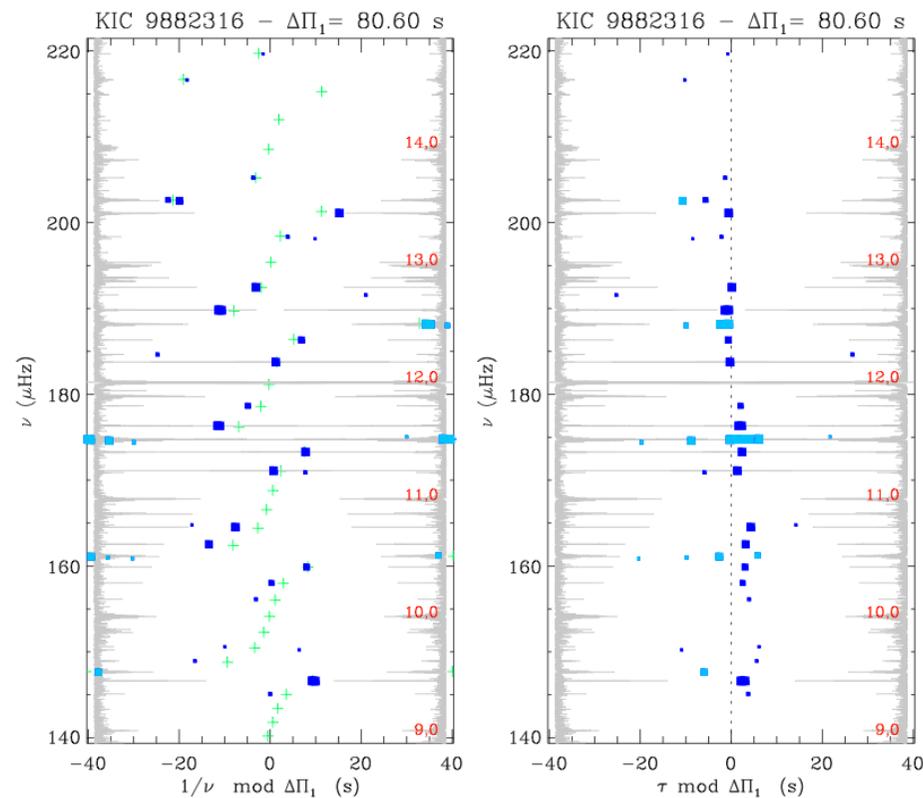
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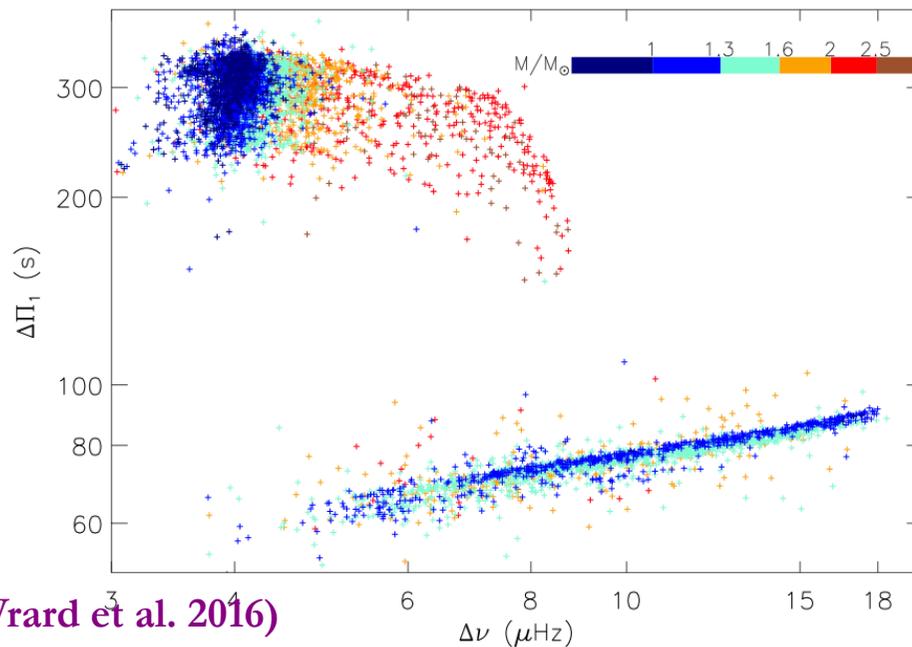
- Opened the way for automated measurements of $\Delta\Pi_1$



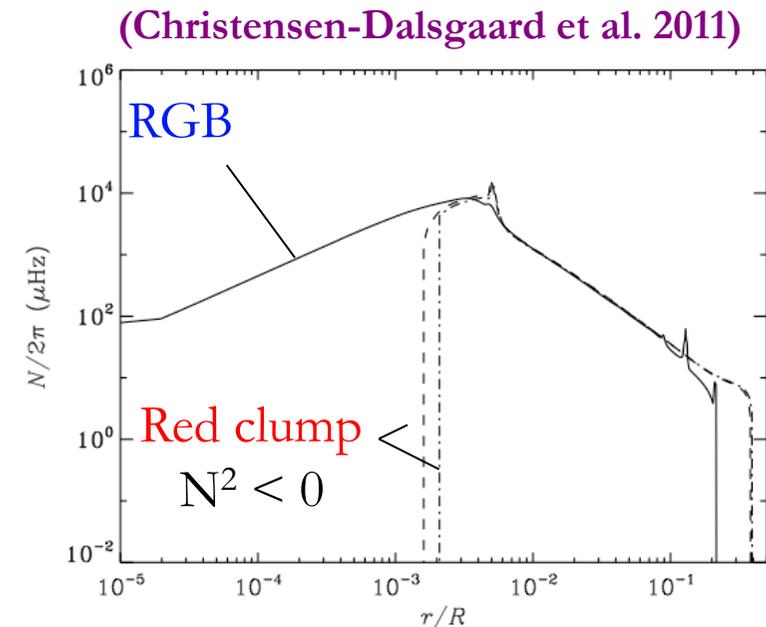
Measuring $\Delta\Pi_1$ for Kepler giants

- Automated measurements of $\Delta\Pi_1$ for ~ 6100 giants (Vrard et al. 2016)
 - Becomes impossible for the brighter part of RGB and AGB (radiative damping, Grosjean et al. 2014)
 - Analysis made tricky in the presence of “glitches”

$$\Delta\Pi_1 = \frac{\sqrt{2}\pi^2}{\int_g \frac{N_{\text{BV}}}{r} dr}$$



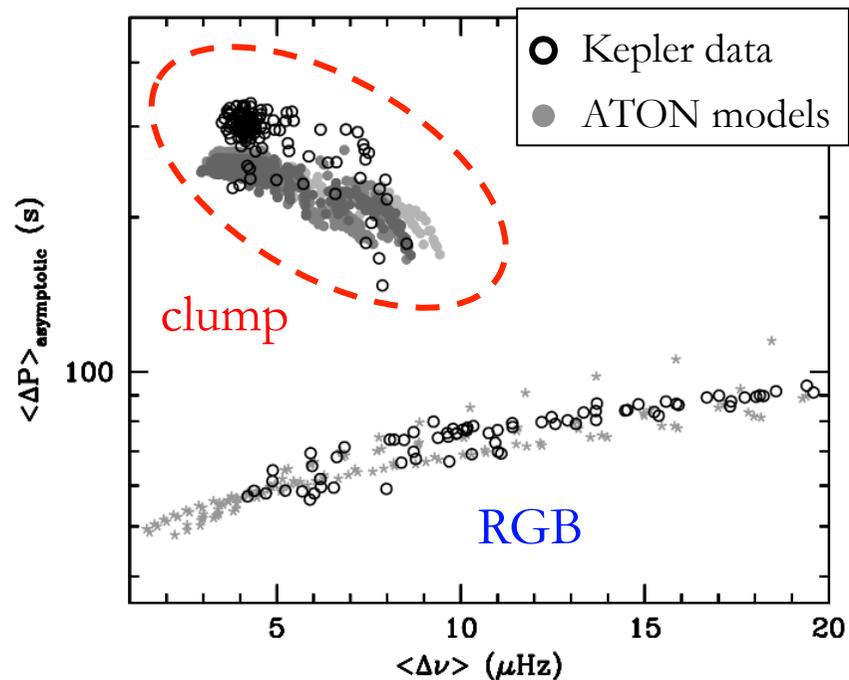
(Vrard et al. 2016)



- Disentangling RGB from clump giants! (Bedding et al. 2011)

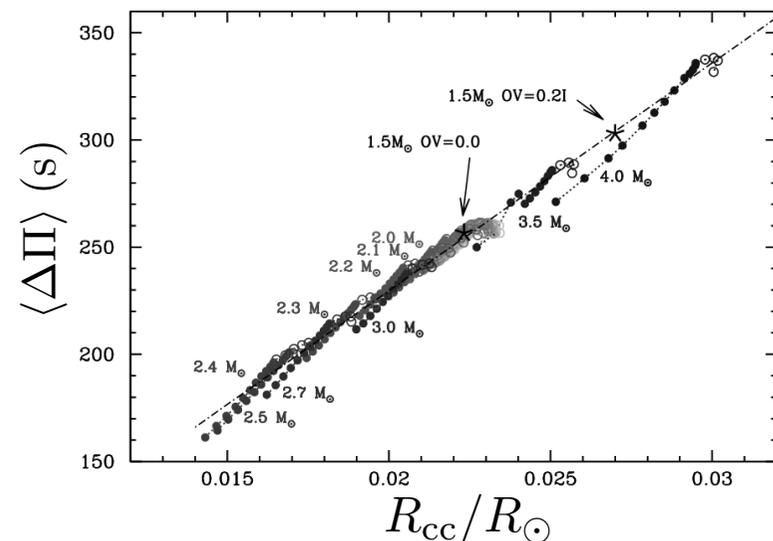
Need for an extended convective core in CHeB stars

- Discrepancy btw observed and theoretical $\Delta\Pi_1$ from models
 - Robust: obtained with several different evolutionary codes (e.g. MESA, ATON, MONSTAR)
 - Uncertainties on microphysics (EOS, reaction rates, opacities...) not sufficient to account for this difference (Campbell's talk in KASC6, Constantino et al. 2015)



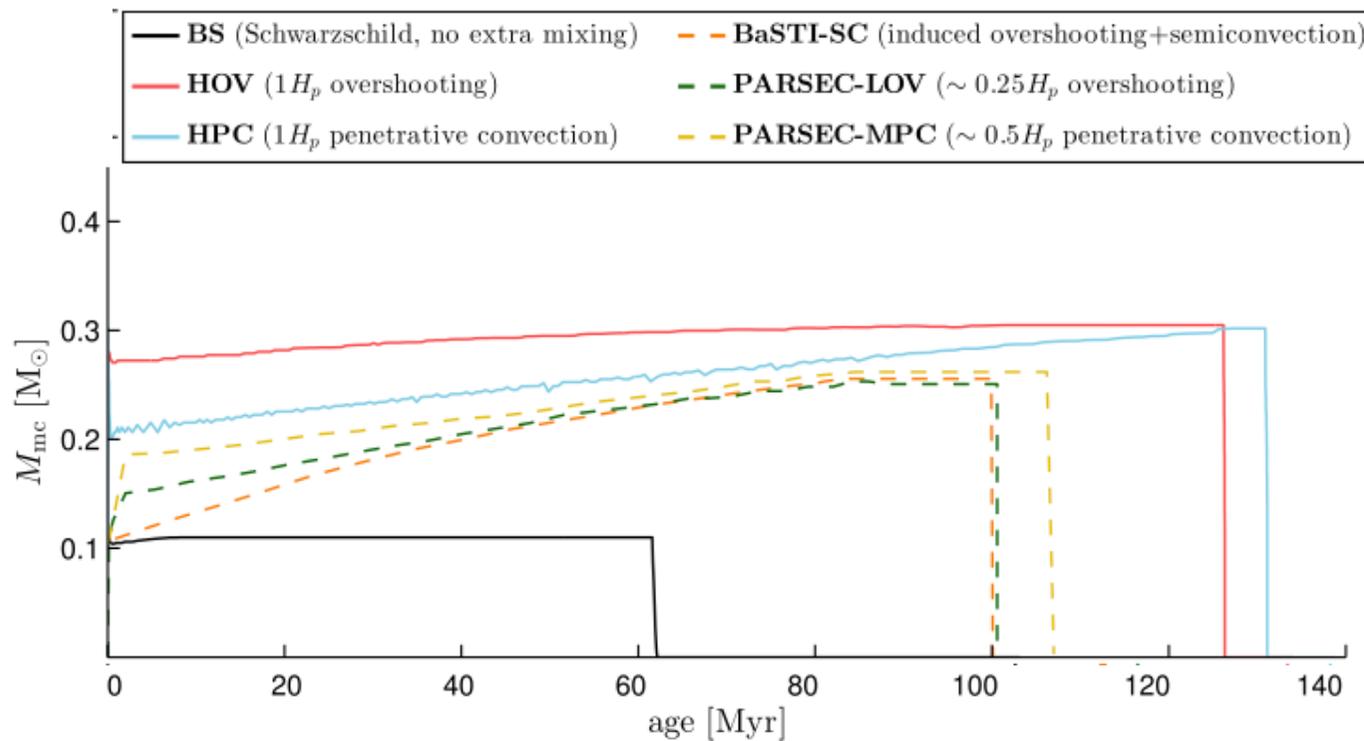
(Montalban et al. 2013)

- Linear relation between size of the convective core and $\Delta\Pi_1$ (Montalban et al. 2013)



Extent of mixed core in CHeB giants

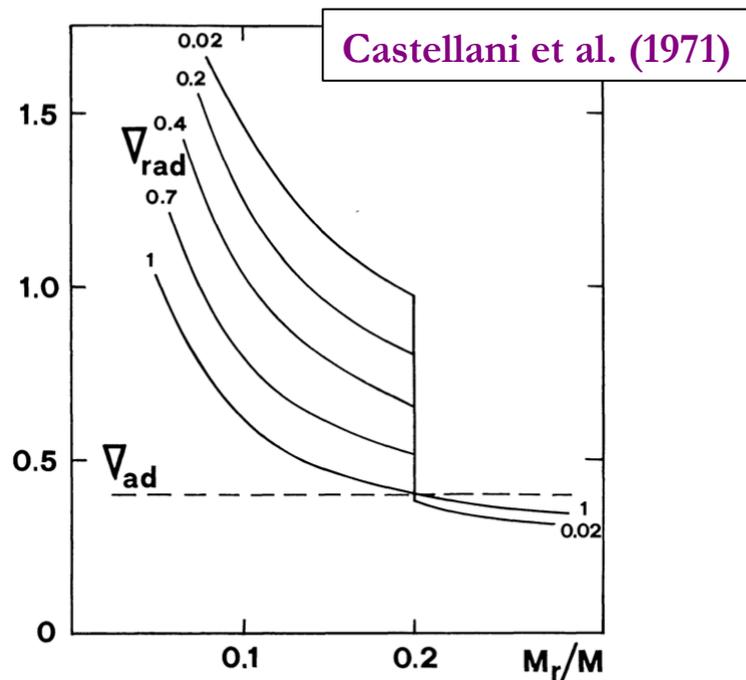
- Uncertainties in the extent of mixed core in core-He-burning giants
 - Size of He core when reaching the clump (Catelan et al. 1996)
 - **Mixing processes** at the edge of the core (Constantino et al. 2015, Bossini et al. 2015)



Bossini et al. (2015)

Extent of mixed core in CHeB giants

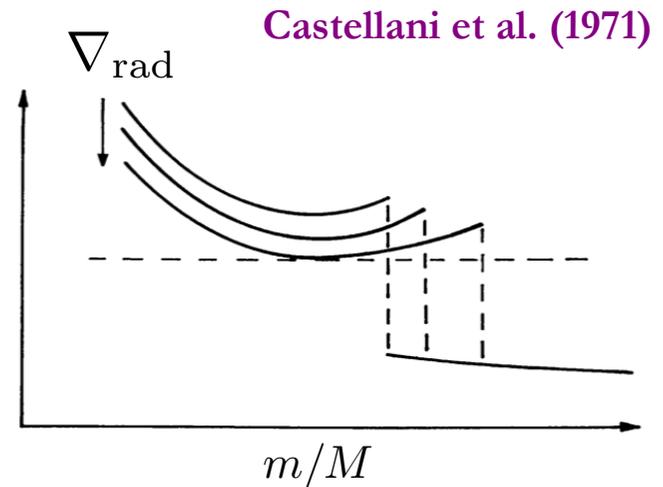
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 - **Mixing processes** at the edge of the core (Constantino et al. 2015, Bossini et al. 2015)
- Common (and yet erroneous) numerical procedure to search for boundary of convective cores $\nabla_{\text{rad}}^{\text{ext}} = \nabla_{\text{ad}}^{\text{ext}}$



- ∇_{rad} increases in the core due to increasing κ (accumulation of C,O)
- $\Rightarrow \nabla_{\text{rad}} \neq \nabla_{\text{ad}}$ at the core boundary, which is unphysical (Schwarzschild 1958, Gabriel et al. 2014)
- produces **spuriously small convective cores**

Extent of mixed core in CHeB giants

- “Induced” **core overshooting**
 - Boundary of the mixed core goes back and forth
 - Overshooting ($\nabla = \nabla_{\text{rad}}$ in mixed zone) or convective penetration ($\nabla = \nabla_{\text{ad}}$)?



- **Semi-convection**

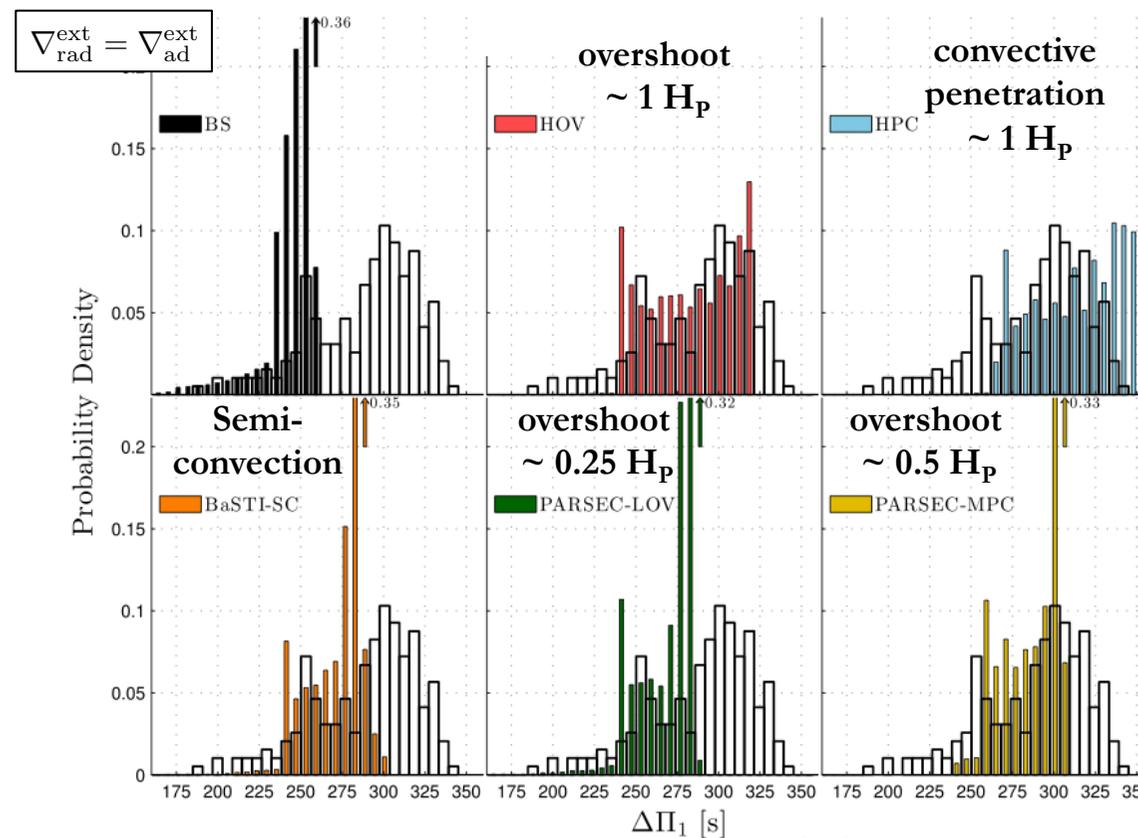
- Convective core expanding into He-rich layers \Rightarrow stabilizing ∇_{μ}
- Semi-convection triggered when $[\text{He}]_c \sim 0.7 \Rightarrow$ partial mixing

produce a different effect on $\Delta\Pi_1$

- Waves evanescent in the mixed region (convective penetration) \Rightarrow **higher $\Delta\Pi_1$**
- Propagation of waves inside the mixed region (overshooting, semi-convection) \Rightarrow **lower $\Delta\Pi_1$**

Extent of mixed core in CHeB giants

- Comparison of the distribution in $\Delta\Pi_1$ between observations and models with different mixing schemes (Bossini et al. 2015, Constantino et al. 2015)



- Need for high overshooting to match observed $\Delta\Pi_1$ (similar conclusion by Constantino et al. 2015)

Extent of mixed core in CHeB giants

- Evidence of **large mixed cores in CHeB giants** from other sources of observations
 - Time spent in core-He-burning vs time spent on AGB: star counts in globular clusters favor **large mixed cores** (e.g. [Constantino et al. 2016](#))
 - Seismic measurements of mixed core sizes in subdwarf-B stars ([van Grootel et al. 2010a, 2010b](#), [Charpinet et al. 2011](#))
 - Extend between 0.22 and 0.28 M_{\odot} ($\sim 50\%$ total mass)
 - Need for large overshoot ($\sim 0.8 H_p$) to account for such large cores ([Schindler et al. 2015](#))

(Jan-Torge Schindler's talk)

- Body of evidence in favor of extended mixed cores in the interior of CHeB giants
 - ⇒ Clump stars are now good laboratories to test mixing beyond cores

“Buoyancy” glitches

- **Glitches:** variations in equilibrium quantities (e.g. the Brunt-Väisälä profile) over length scales \sim mode wavelength

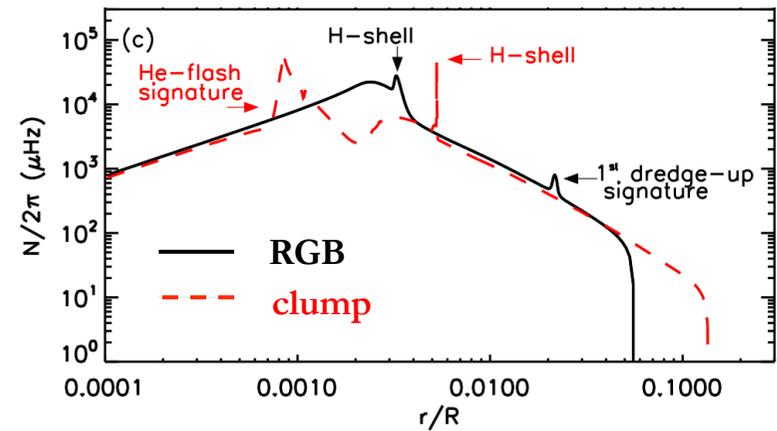
– Buoyancy glitches arise due to

- 1st dredge-up
- H-shell
- He-flash signature...

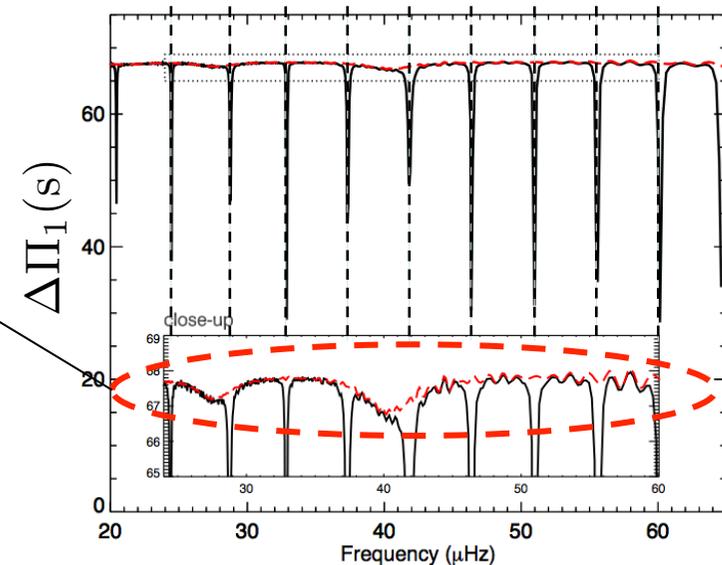
– Cause periodic modulation in the mode periods (and thus in $\Delta\Pi_1$)

$$\Delta n = \frac{\Pi_{\text{glitch}}}{\Pi_{\text{g-cav}}} = \frac{\int_{r_i}^{r_0} \frac{N}{r} dr}{\int_{r_i}^{r_{\text{glitch}}} \frac{N}{r} dr}$$

Cunha et al. (2015)

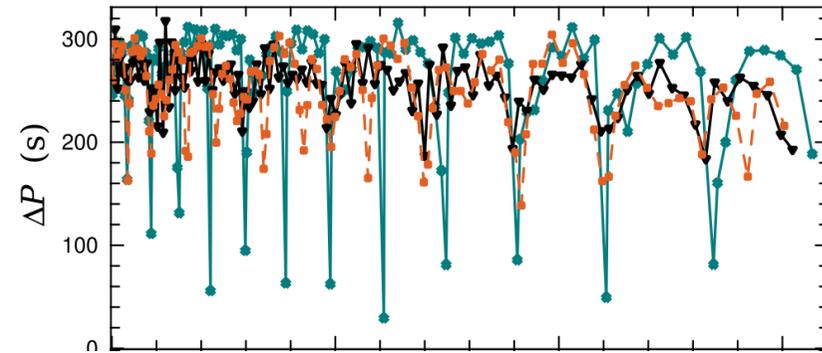
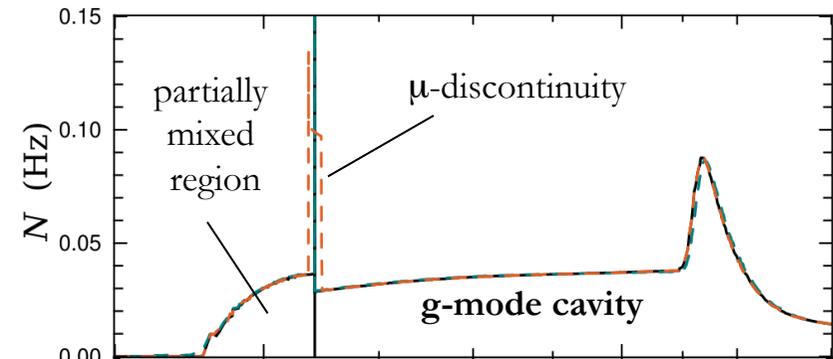
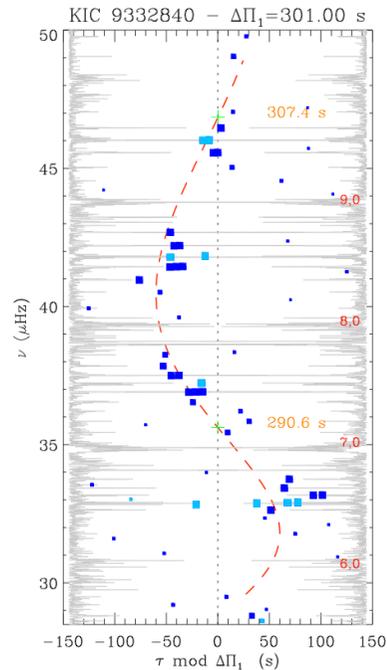
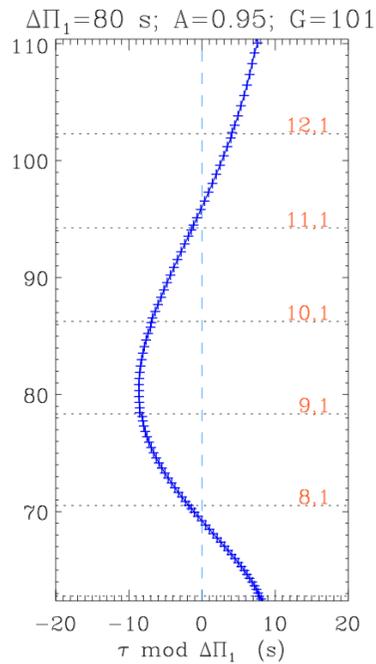


p-modes



“Buoyancy” glitches

- Glitch at boundary of mixed core
 - Could increase $\Delta\Pi_1$ with semi-convection (Constantino et al. 2015)
- Detection of buoyancy glitches
 - Stretched échelle diagrams

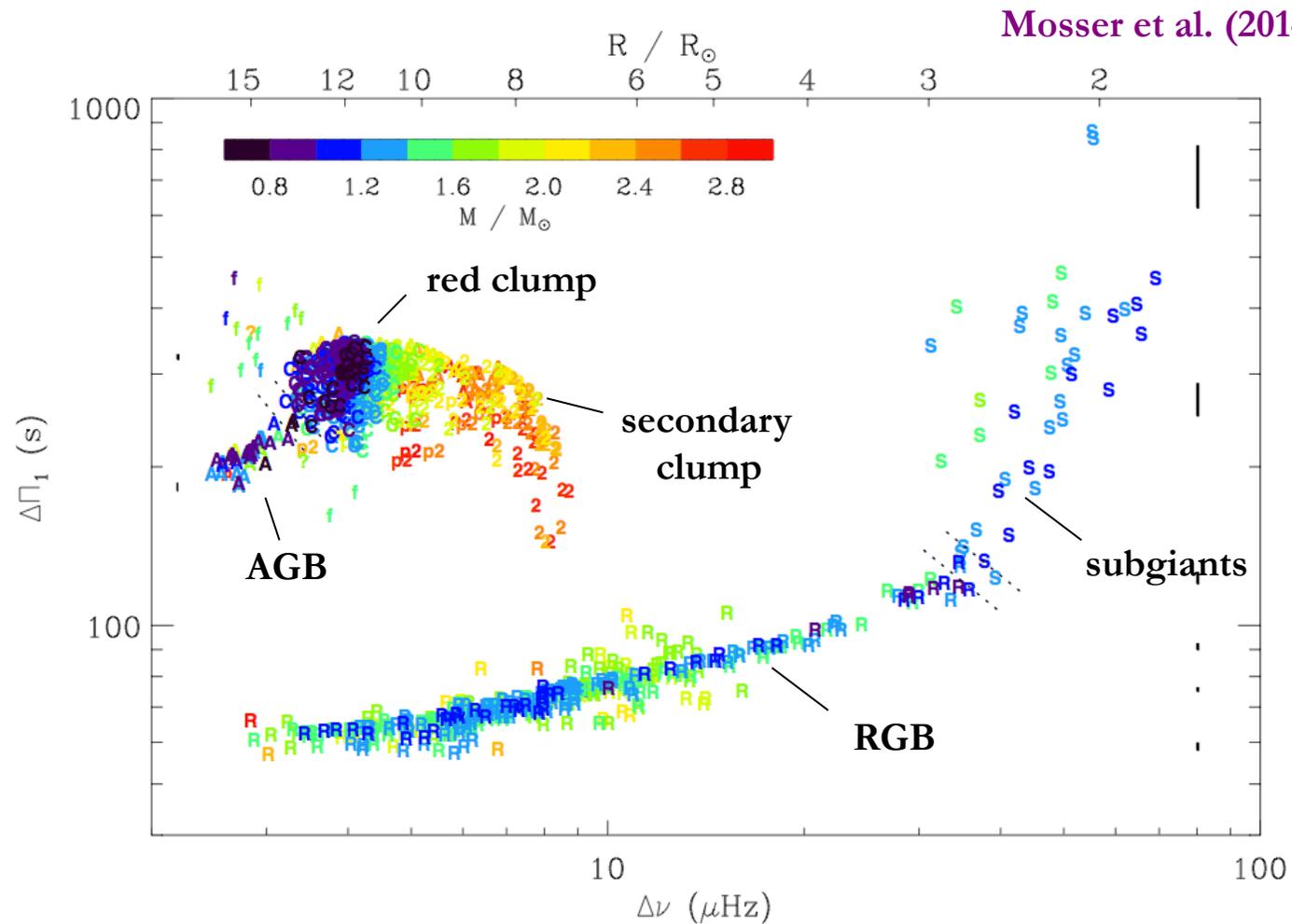


— Sharp μ -transition
 - - - Smooth μ -transition

(Mosser et al. 2015)

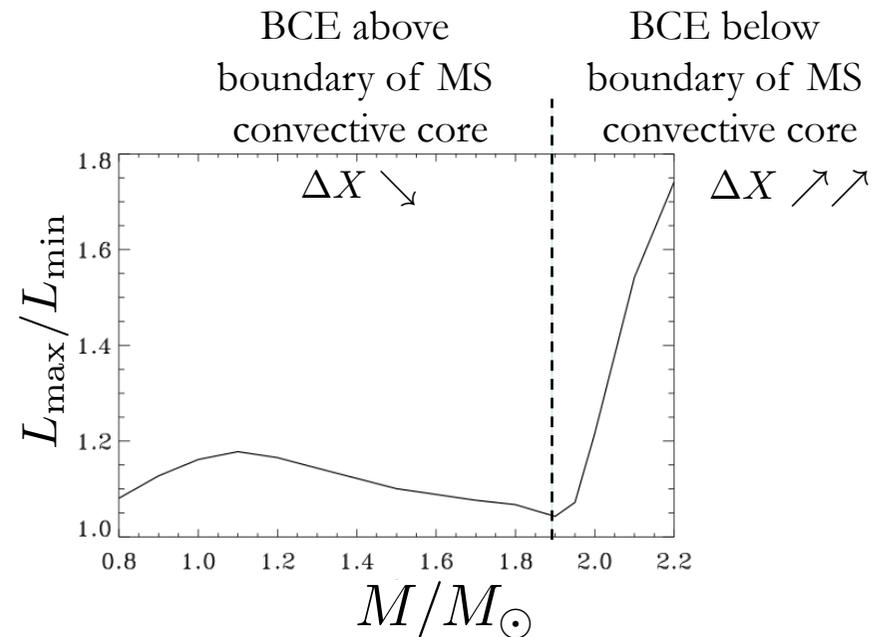
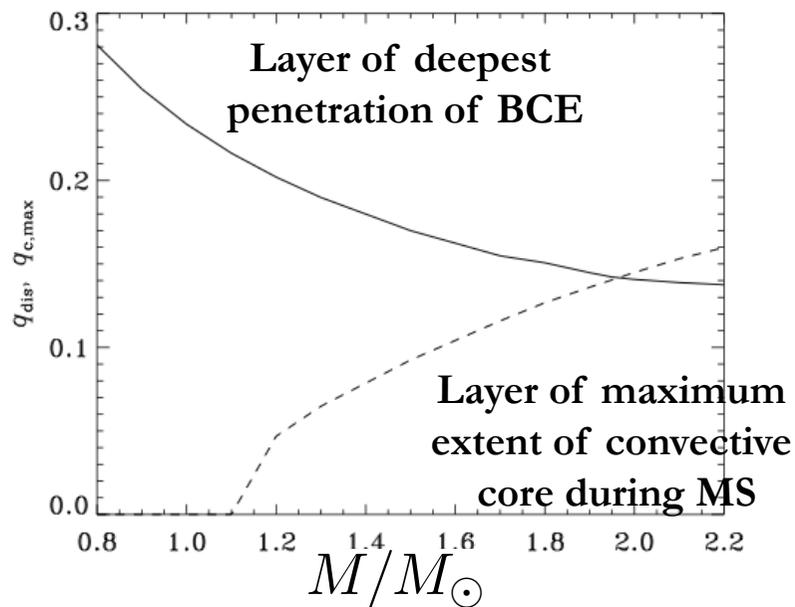
A window on stellar evolution

- The $\Delta\Pi_1$ - $\Delta\nu$ diagram



Luminosity bump

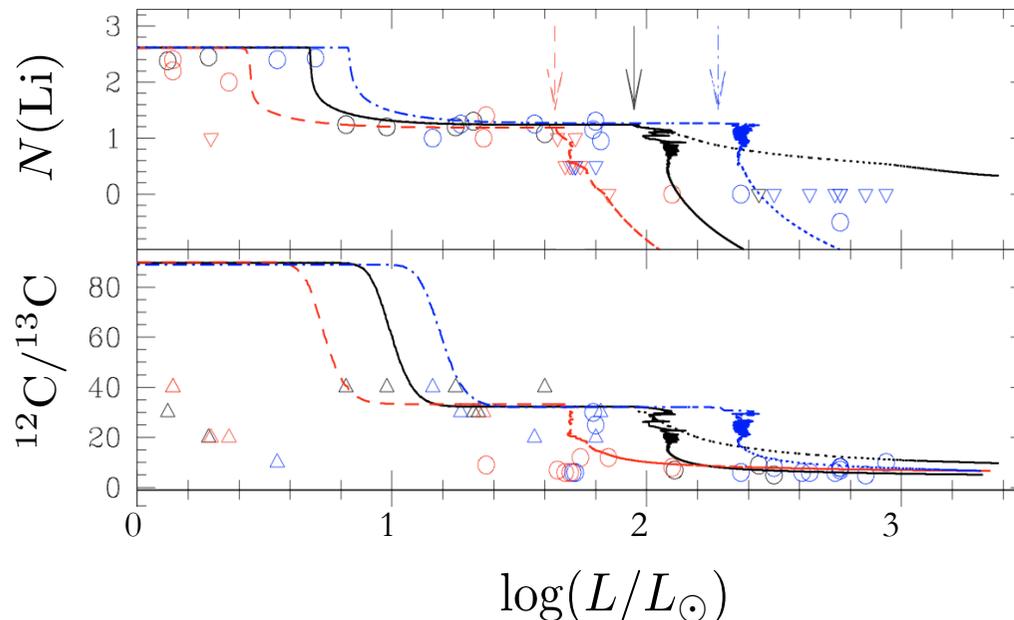
- Using **luminosity bump** as an observational constraint (Christensen-Dalsgaard et al. 2015)
 - L_{\max}/L_{\min} depends mainly on ΔX above H-shell



- Potential probe of **the extension of convective regions** (needs to be further tested)

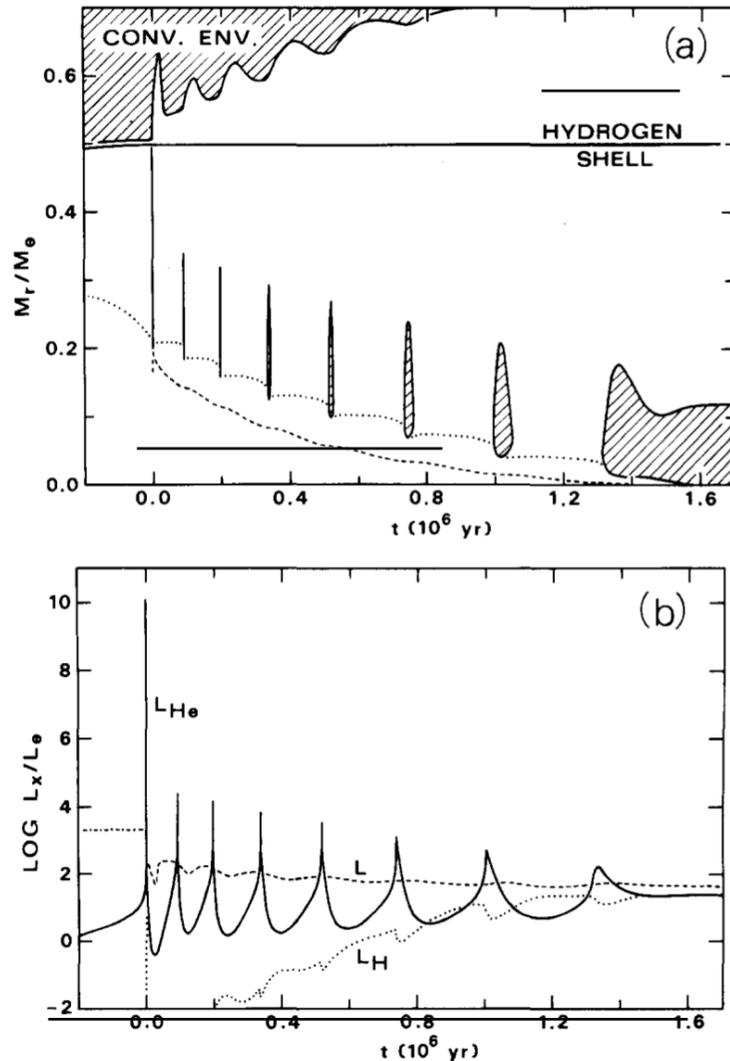
Luminosity bump

- **Mixing in radiative interiors** after luminosity bump
 - After luminosity bump, ${}^3\text{He}$ burning above the H-shell
 - ⇒ Inverse μ -gradient, which triggers **thermohaline convection**
(Charbonnel & Zahn 2007)
 - Combine asteroseismology with spectroscopic measurements (Lagarde et al. 2015) + APOKASC data



(Charbonnel & Zahn 2007)

Searching for giants undergoing the He-flash

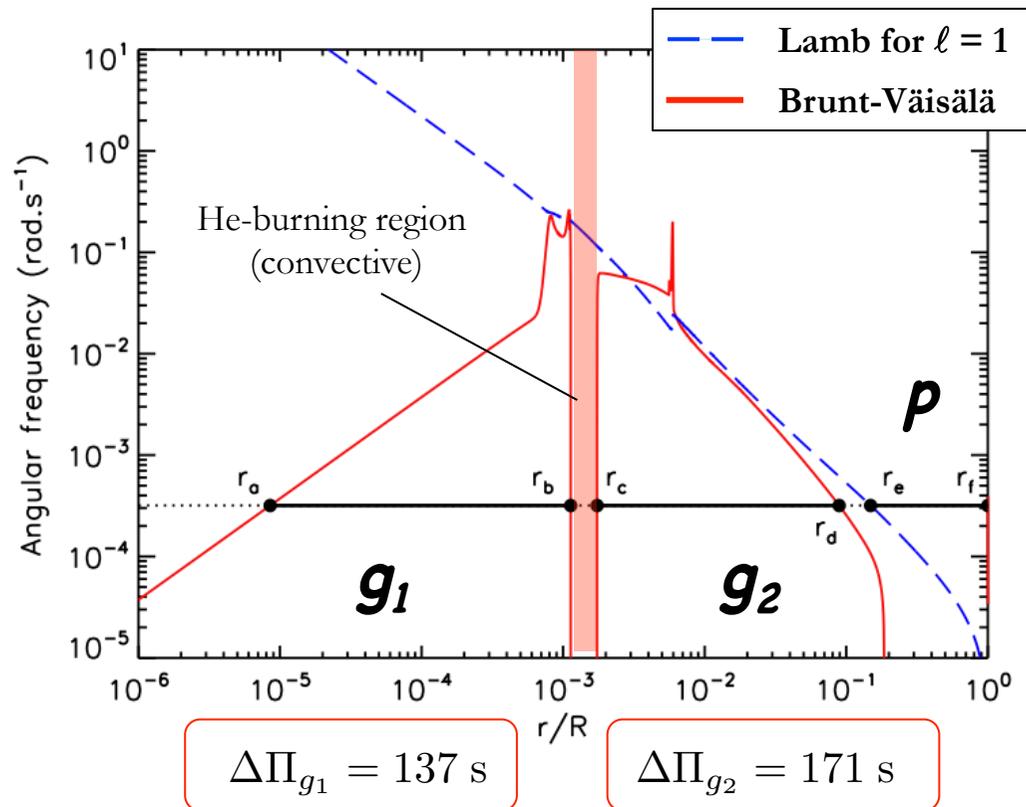


- Several 1D codes predict the He-flash to occur as a series of successive subflashes (Thomas 1967, Iben & Renzini 1984, Bildsten et al. 2012)
- Existence of such subflashes debated in view of 2D- and 3D- numerical computations (Mocak et al. 2008, 2009)
 - Fast extension of inner and outer convective region caused by He-burning
 - Would suppress the He-subflashes

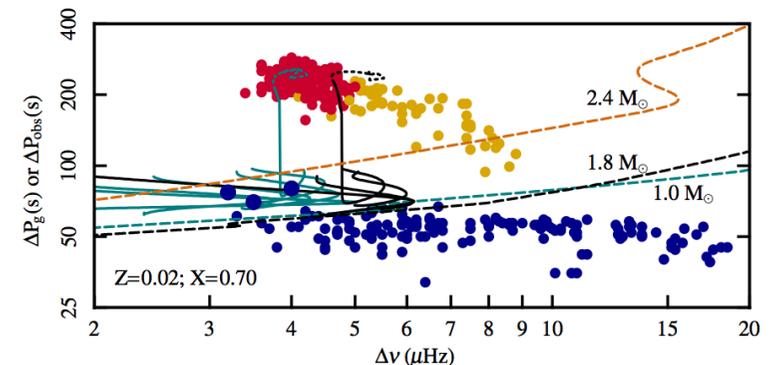
Iben & Renzini (1984)

Searching for He-flashing giants among *Kepler* data

- What is the influence on the oscillation spectrum?



- Decrease of the period spacing of the outer g-mode cavity (g_2) (Bildsten et al. 2012)



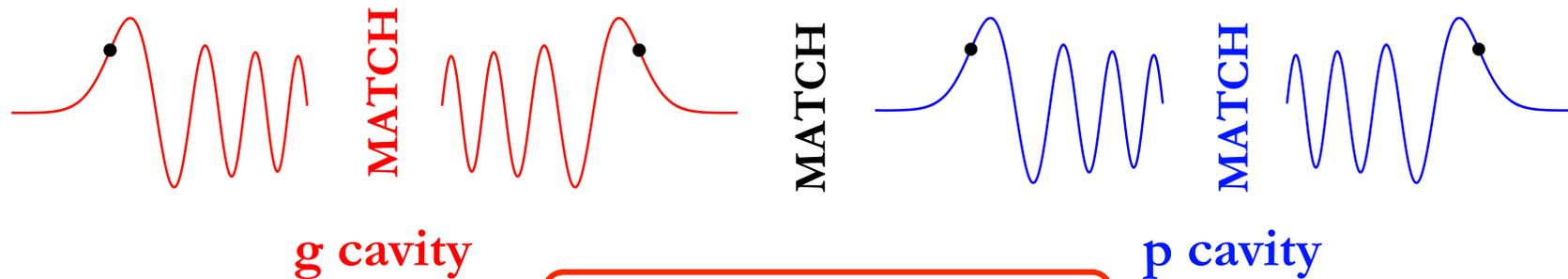
- Propagation of waves in 3 cavities (g_1, g_2, p):
What impact on the mode frequencies?

WKB approximation applied to 2 cavities (mixed modes)

- Equations of **non-radial stellar oscillations** (adiabatic, Cowling approximation) can be expressed as turning-point (TP) equations (**Unno 1989**)

$$\begin{cases} \frac{d^2 v}{dr^2} + k_r^2 v = 0 \\ \frac{d^2 w}{dr^2} + k_r^2 w = 0 \end{cases} \quad \text{with} \quad \begin{cases} v \equiv \rho^{1/2} c r \left| 1 - \frac{S_l^2}{\omega^2} \right|^{-1/2} \xi_r \\ w \equiv \rho^{-1/2} r |N^2 - \omega^2|^{-1/2} p' \end{cases}$$

- For two cavities, i.e. **mixed modes**



$$\cot(\theta_g) \tan(\theta_p) = q$$

$$\theta_g(\omega, \Delta\Pi_1, \varepsilon_g, \dots)$$

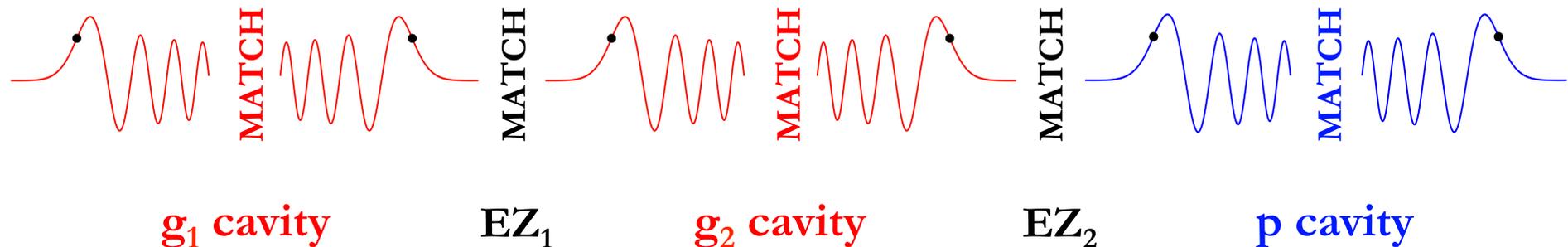
$$\theta_p(\omega, \Delta\nu, \varepsilon_p, \dots)$$

coupling term

$$q = \frac{1}{4} \exp\left(-2 \int_{\text{EZ}} |k_r| dr\right)$$

WKB approximation applied to 3 cavities (He subflash)

- Extension to the case of three cavities (two g-mode cavities + p-mode cavity)



$$\cot \theta_{g_1} \cot \theta_{g_2} \tan \theta_p - q_2 \cot \theta_{g_1} - q_1 \tan \theta_p - q_1 q_2 \cot \theta_{g_2} = 0$$

- Limiting case where $q_1 = 0$

$$\left\{ \begin{array}{l} \cot(\theta_{g_1}) = 0 \text{ ————— } g_1 \text{ pure mode} \\ \cot(\theta_{g_2}) \tan(\theta_p) = q_2 \text{ ————— } p/g_2 \text{ mixed mode} \end{array} \right.$$

- Coupling intensities

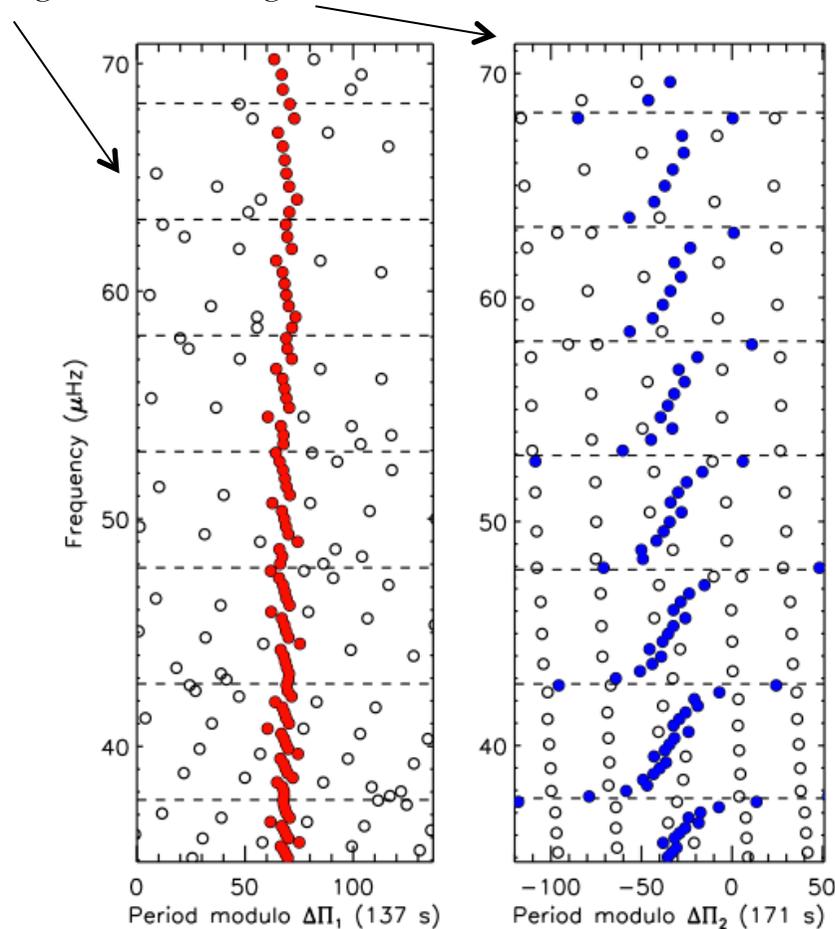
MESA model

$$q_1 = \frac{1}{4} \exp\left(-2 \int_{EZ_1} |k_r| dr\right) \text{ — } q_1 \approx 0.03$$

$$q_2 = \frac{1}{4} \exp\left(-2 \int_{EZ_2} |k_r| dr\right) \text{ — } q_2 = 0.13$$

WKB approximation applied to 3 cavities (He subflash)

- Period échelle diagrams of asymptotic oscillation spectrum, folded with $\Delta\Pi_{g_1}$ and $\Delta\Pi_{g_2}$, respectively

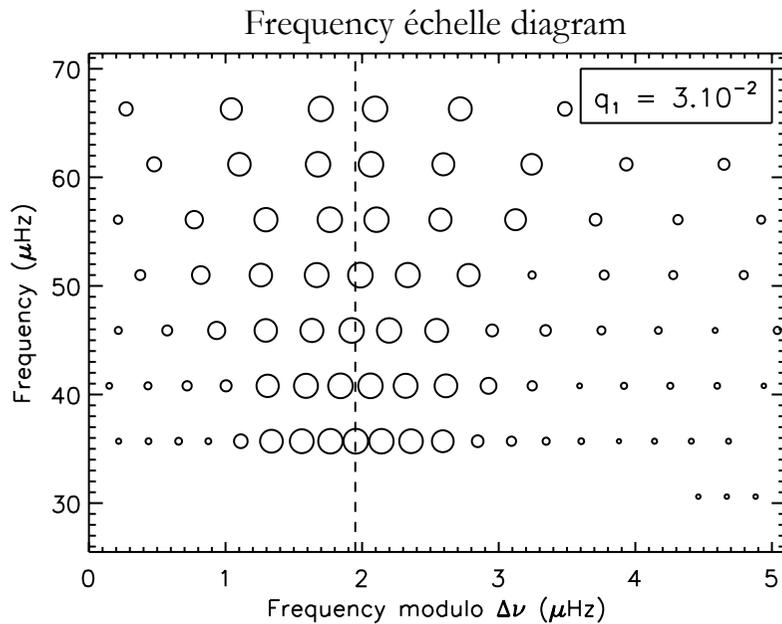


- modes trapped mainly in p and g_2 cavities
- modes trapped mainly in g_1 cavities

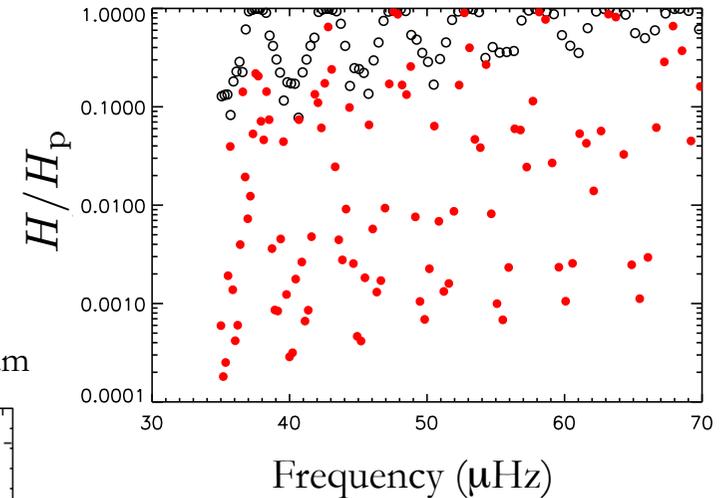
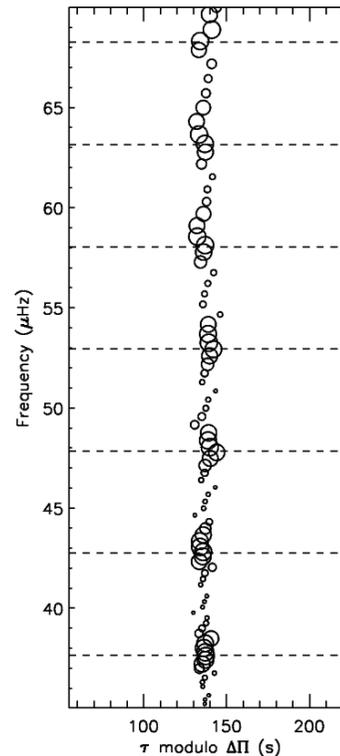
WKB approximation applied to 3 cavities (He subflash)

- Mode heights in the power spectrum
 - Ratios of inertia I_p/I derived from WKB analysis (based on [Goupil et al. 2013](#))
 - Effects of radiative damping (based on [Godart et al. 2009](#))

$$\eta_g = -\frac{W_{g_1} + W_{g_2} + W_e}{2\omega^2 I}$$



Stretched échelle diagram

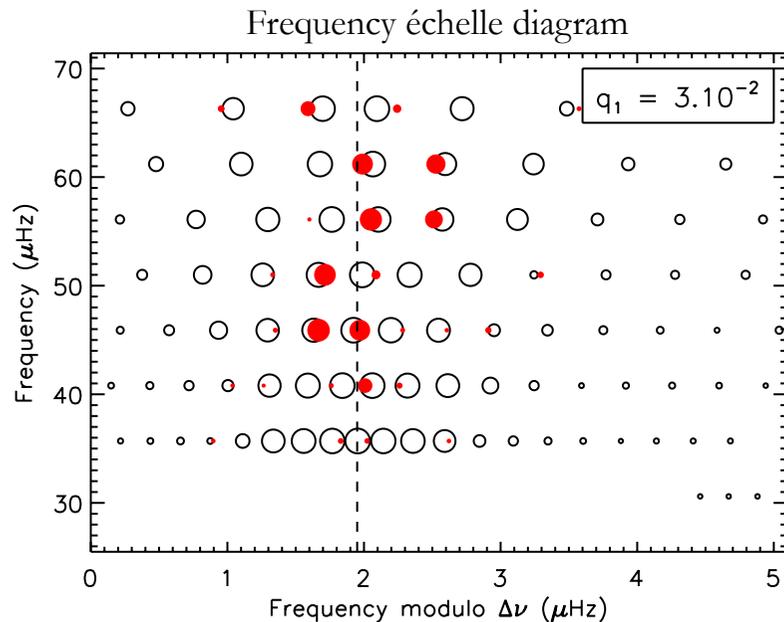


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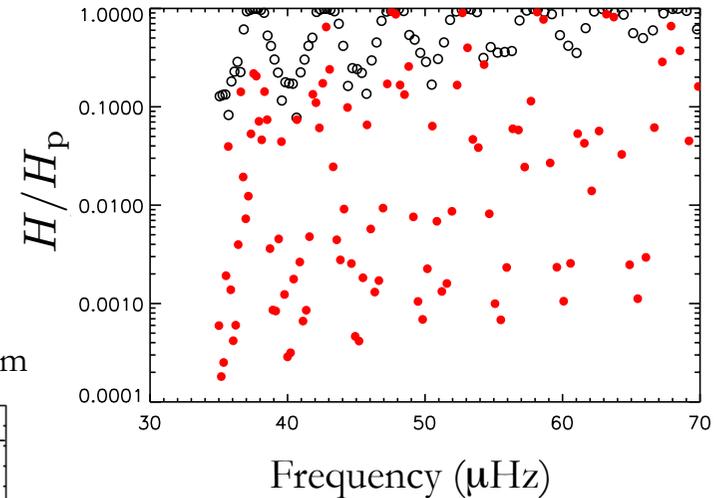
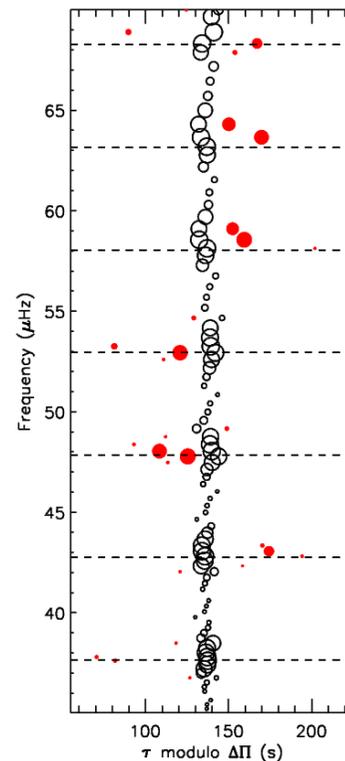
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Stretched échelle diagram



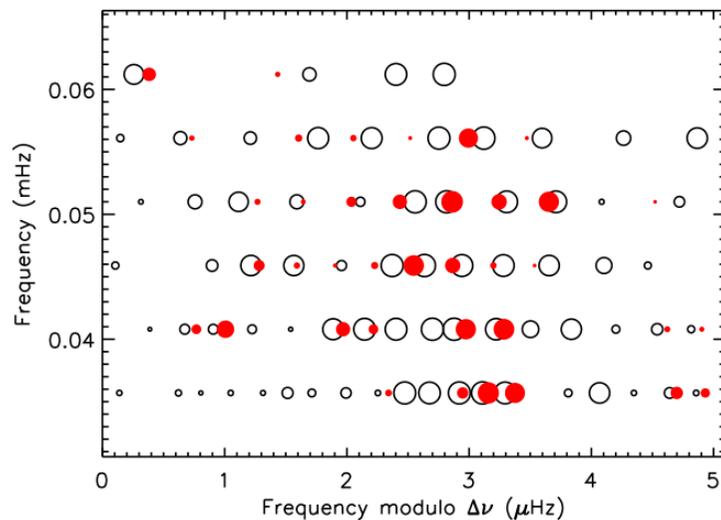
○ modes trapped mainly in p & g_2 cavities

● modes trapped mainly in g_1 cavity

Additional detectable modes in the vicinity of pure p modes

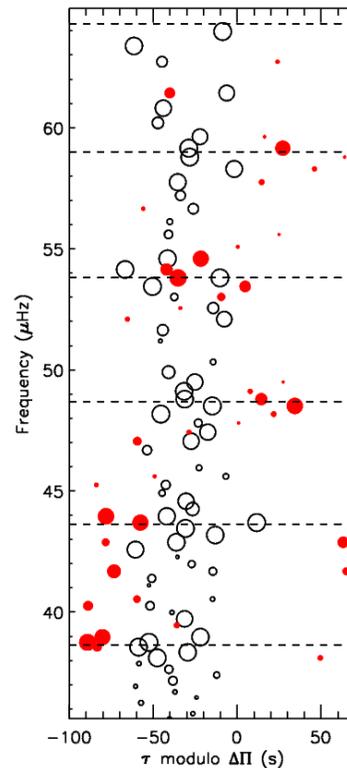
Comparison with full numerical solutions

- MESA model ($1.7 M_{\odot}$) during a He-subflash
 - Mode frequencies extracted with LOSC (Scuflaire et al. 2008) taking care to resolve rapidly varying eigenfunctions near the core
 - Ratios of inertia + effects of radiative damping estimated based on eigenfunctions



○ modes trapped mainly in p & g_2 cavities

● modes trapped mainly in g_1 cavity

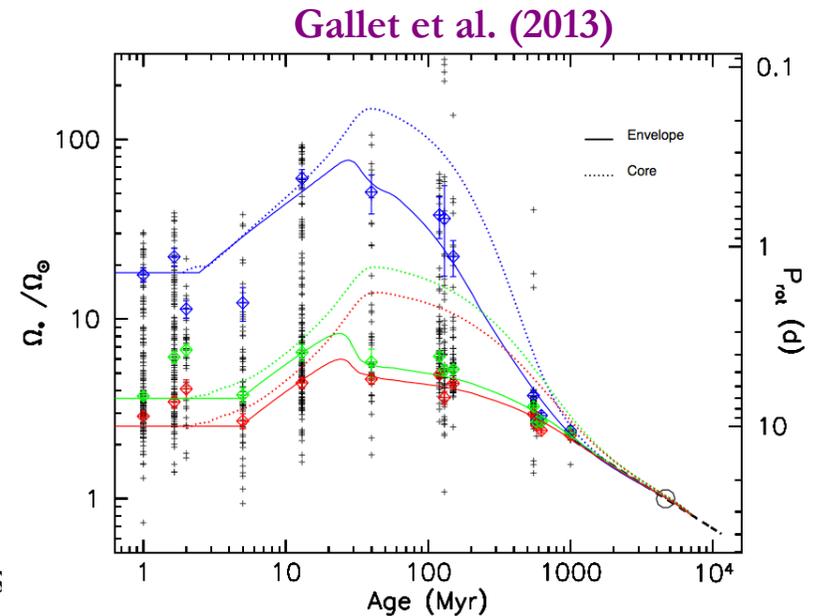


- Confirms presence of additional detectable modes
- Search for candidates among Kepler targets (in collaboration with M. Vrad and B. Mosser)

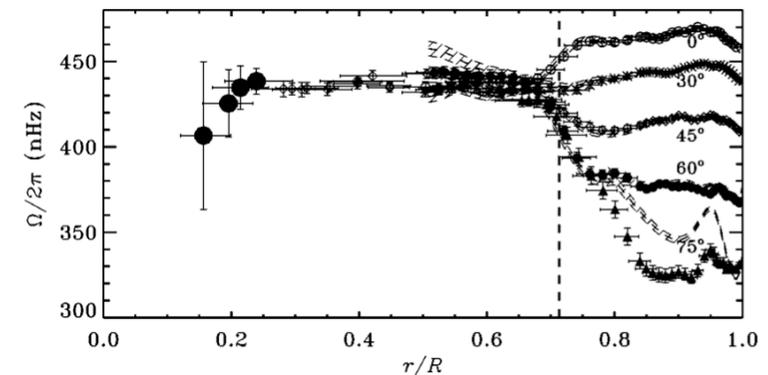
Constraining angular momentum transport in stars

- Transport of angular momentum in stars remains uncertain
 - Several processes (rotation-induced, magnetic fields, internal waves...)
Which ones dominate?
- Evidence for a missing ingredient
 - Surface rotation of young stars in clusters
 - Solar rotation profile
 - **Internal rotation of red giants**
 - Surface rotation of white dwarfs and neutron stars

⇒ **All point to a more efficient transport of angular momentum in stars**

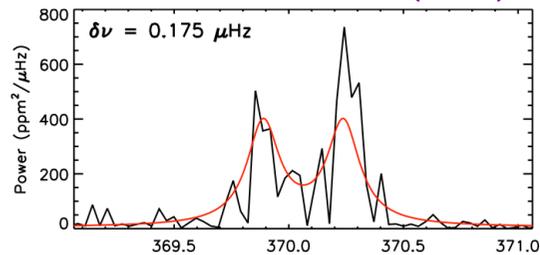


Solar internal rotation (Chaplin et al. 1999)

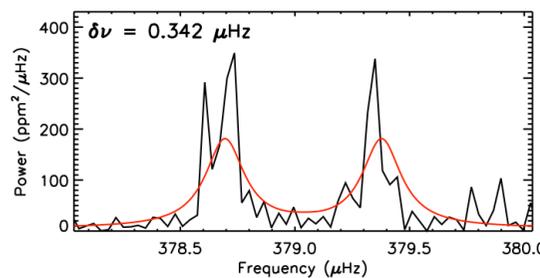
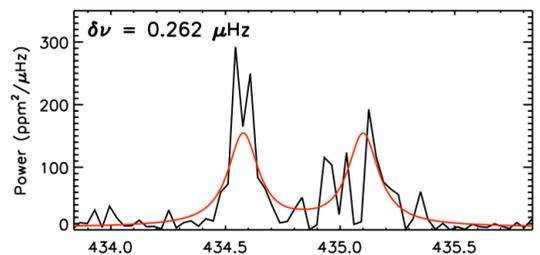
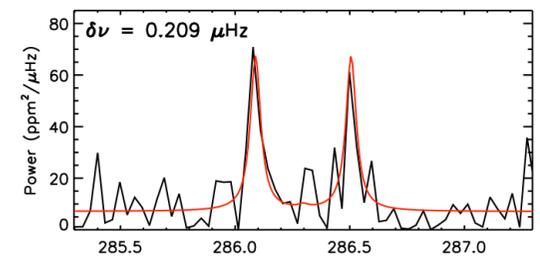


Seismology of red giants: a new piece to the puzzle

Deheuvels et al. (2012)



p-like
modes



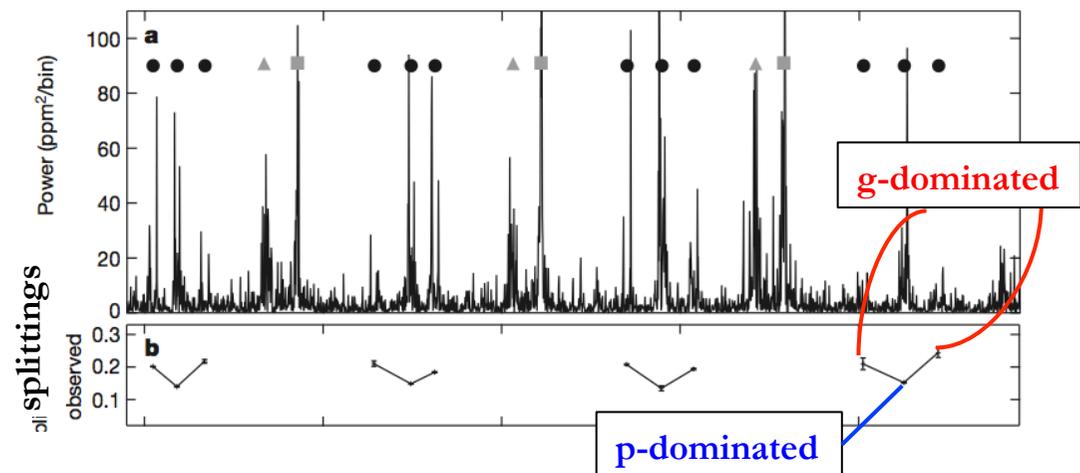
g-like
modes

- **Rotation** lifts the degeneracy between $m \neq 0$ modes

$$\delta\omega_{n,l,m} = m \int_0^R K_{n,l}(r) \Omega(r) dr$$

Rotational kernels

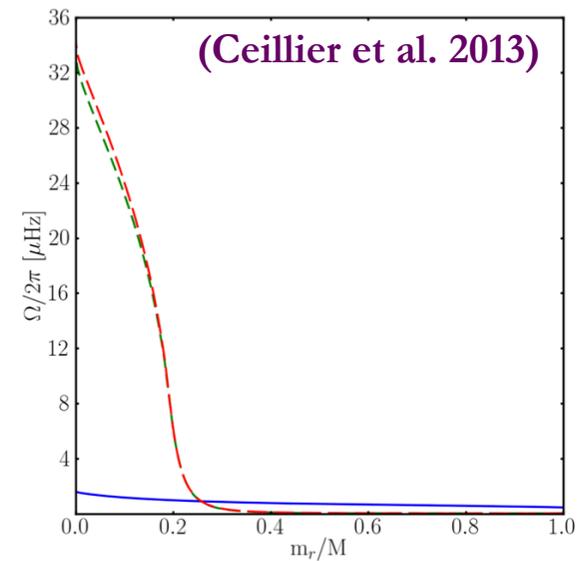
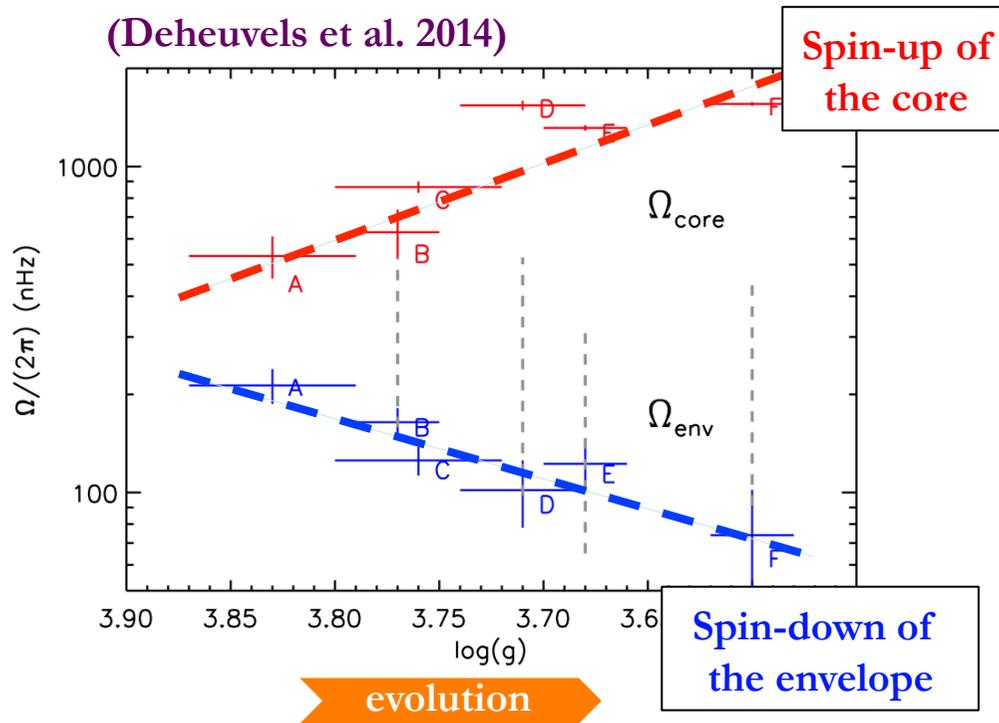
(Beck et al. 2012)



⇒ Core rotates faster than
envelope in young red giants

Subgiants & young red giants

- **Spin-up** of the core in subgiants & young red giants

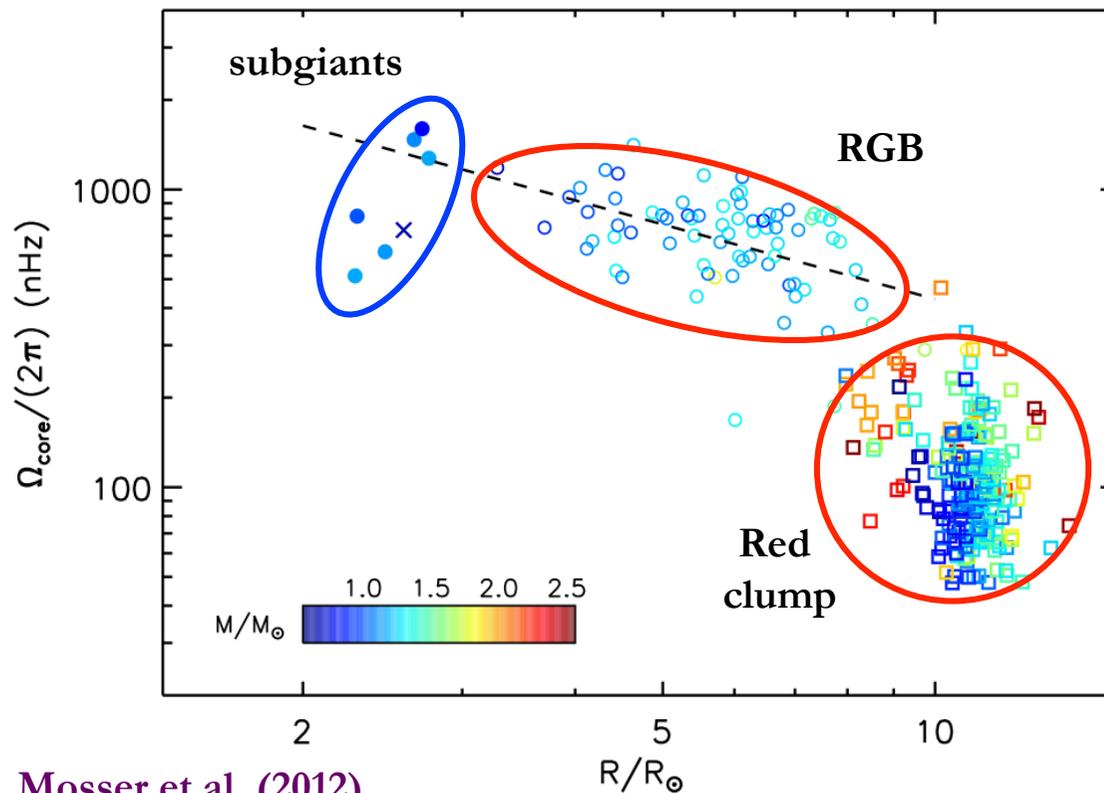


Need for an additional efficient mechanism of AM transport

AM transport including shear + circulation à la Zahn et al. (1992) predict **much faster core** rotation (Ceillier et al. 2013, Marques et al. 2013)

Spin-down of the core for red giants

- Extraction of rotational splittings in ~ 300 Kepler giants
(Mosser et al. 2012)



Mosser et al. (2012)

Spin-down of the
core in the RGB

⇒ Need for additional
AM transport

- Large core-envelope
contrast on the RGB
(Goupil et al. 2013)

$$\frac{\Omega_{\text{core}}}{\Omega_{\text{env}}} > 20$$

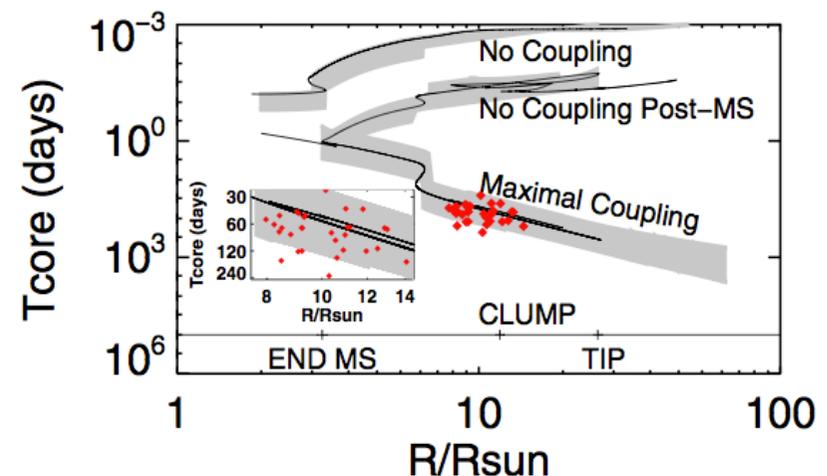
Intermediate-mass clump stars

- Evolution of intermediate-mass stars ($M > 2.1 M_{\odot}$)
 - experience **similar structural changes** as low-mass stars with similar radius...
 - BUT on much smaller timescales since **subgiant & RGB phases are short-lived** (on a thermal timescale)
 - Non-degenerate core => no He flash

⇒ **AM transport must act on shorter timescales**

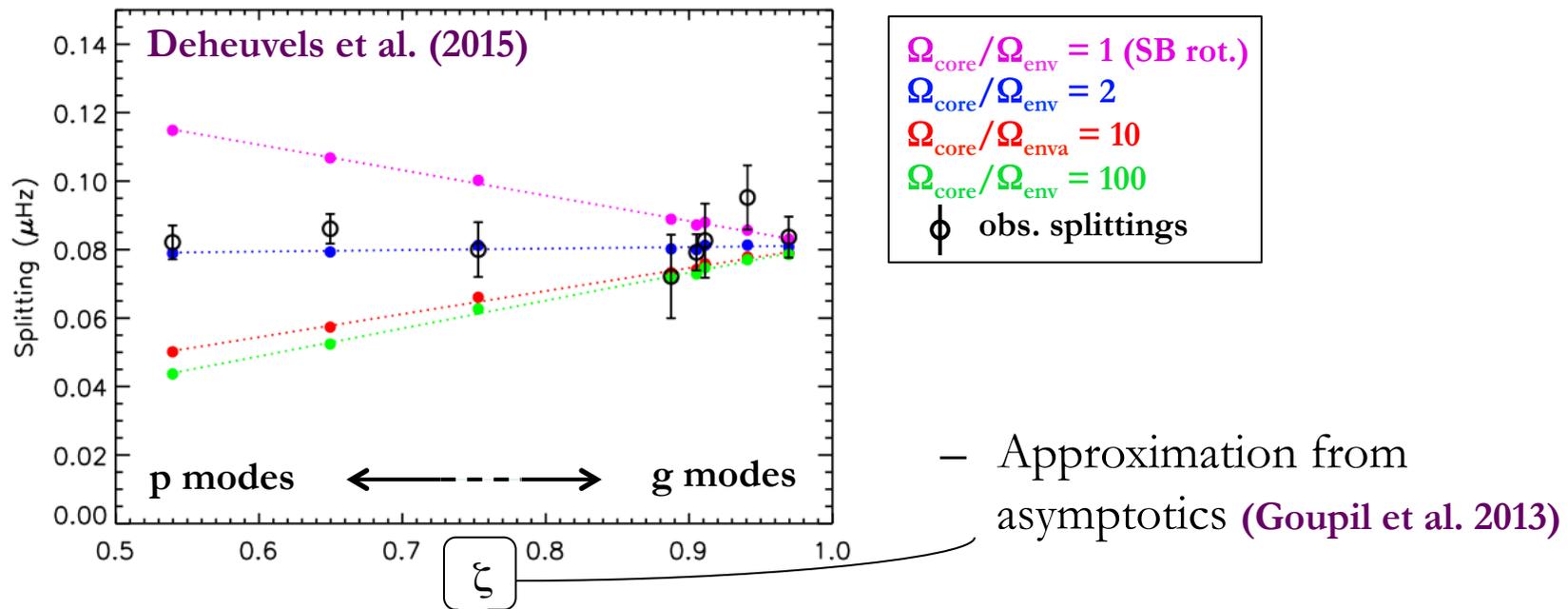
- Core rotation roughly compatible with solid-body rotation

(Tayar & Pinsonneault 2013)



Core-He burning giants (red clump)

- Secondary clump stars: intermediate-mass ($M > 2.1 M_{\odot}$) core He-burning stars



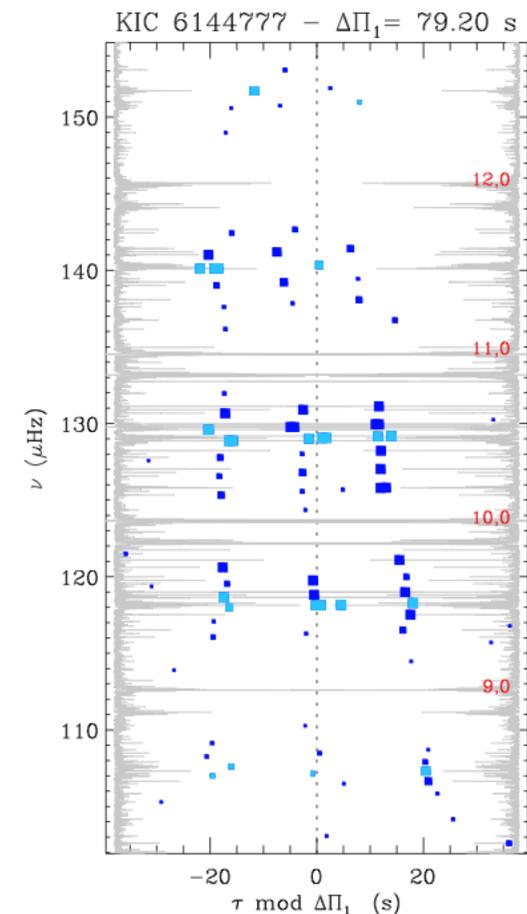
- **Weak differential rotation** $\left(1 \leq \frac{\Omega_{\text{core}}}{\Omega_{\text{env}}} \leq 3.2\right)$ for 7 Kepler clump stars (Deheuvels et al. 2015)

\Rightarrow **very fast redistribution of AM** either during short-lived subgiant phase or at the beginning of core He-burning

What more can we expect from seismology about rotation?

- Automatic measurement of core rotation in *Kepler* giants (Charlotte Gehan's poster S10.48)
- Inversion of rotation profiles for stars at particular stages of evolution or which have peculiarities (“fast” rotators, stars showing large surface magnetic fields...)
- More precise/localized information about rotation profiles
 - Potential existence of strong rotational gradients in the vicinity of the H-shell in young giants (Deheuvels et al. 2014)
- Future missions with long observations: TESS (1-yr observations), PLATO!

(Mosser et al. 2015)



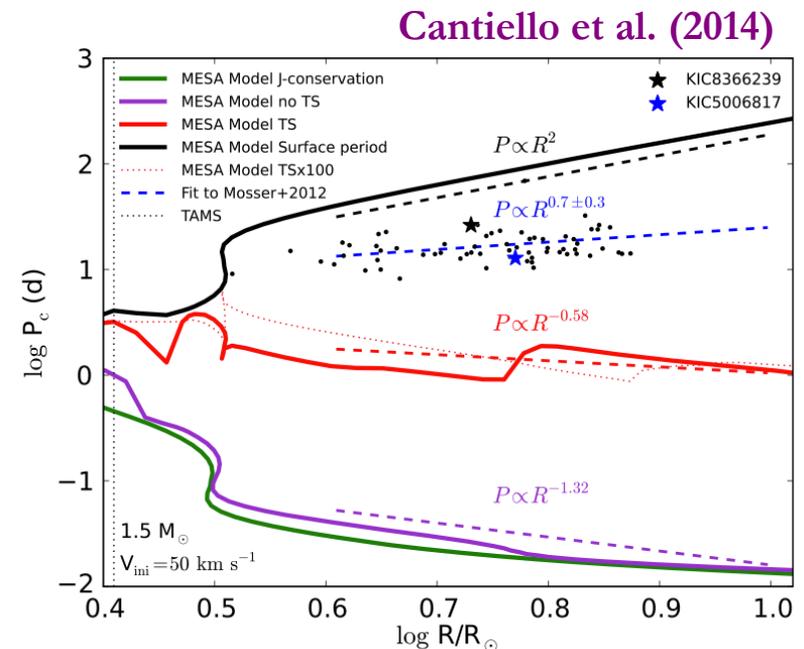
Mechanisms that could efficiently AM transport

- Purely hydrodynamical processes (shear, meridional circulation)
 - By far not efficient enough Füller et al (2014)
 - But Mathis et al. 2016?
- Internal gravity waves (Charlie Pinçon & Tamara Rogers' talks)
 - ✓ Might account for **core/envelope decoupling** during **subgiant** phase
 - + role of differential rotation for plume-induced IGW (Pincon et al. 2016)
 - ✗ But not for **core spin down** during **RGB**
 - ? During core-He burning (**clump**), **waves excited at the core edge** might efficiently couple
- Transport by mixed modes (Belkacem et al. 2015a,b)
 - Efficient in the upper part of the RGB, but not at the subgiant/young giant phase

Magnetic fields

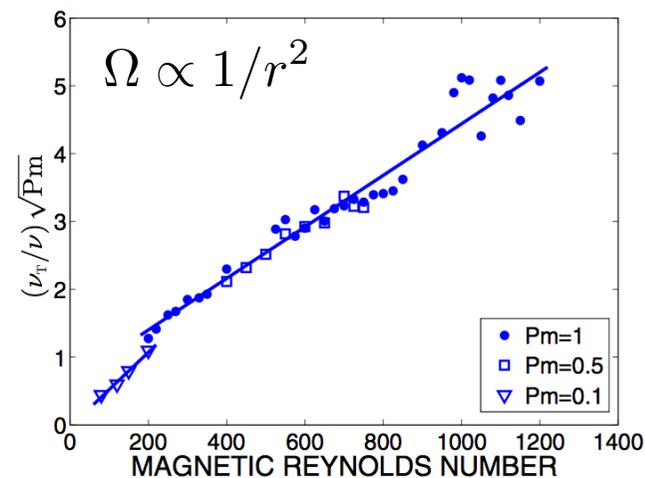
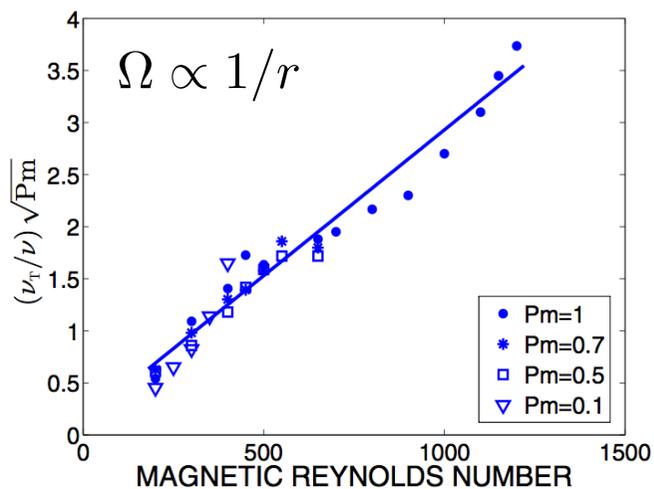
- Transport of angular momentum through **a fossil field** (Maeder & Meynet 2014)
 - order-of-magnitude calculations of the extension of a dipolar fossil magnetic field in core-He-burning stars
 - Coupling between core and convective envelope very unlikely
 - Coupling between core and intermediate radiative regions is “easy”

- **Taylor-Spruit dynamo** (amplification of toroidal magnetic field due to the combined effect of Taylor instability and differential rotation)
 - Existence debated (Zahn et al. 1997, Braithwaite et al. 2006)
 - Not efficient enough to account for core rotation of giants (Cantiello et al. 2014)



Magnetic fields

- Transport of angular momentum through **(A)MRI**: instability of a magnetic field induced by differential rotation)
 - Numerical simulations with different setups (Rüdiger et al. 2015, Jouve et al. 2015)
 - Development of (A)MRI **over $\tau \sim$ rotation period \ll evolution timescale**
 - **Efficient AM transport**: effective viscosity $\gg \nu_{\text{add}}$ required by Eggenberger et al. 2012 to account for core rotation of young giants (Rüdiger et al. 2015)
 - Only an **upper limit** (effects of stratification are ignored)
 - **Efficiency of AM transport depends on the intensity of the shear**

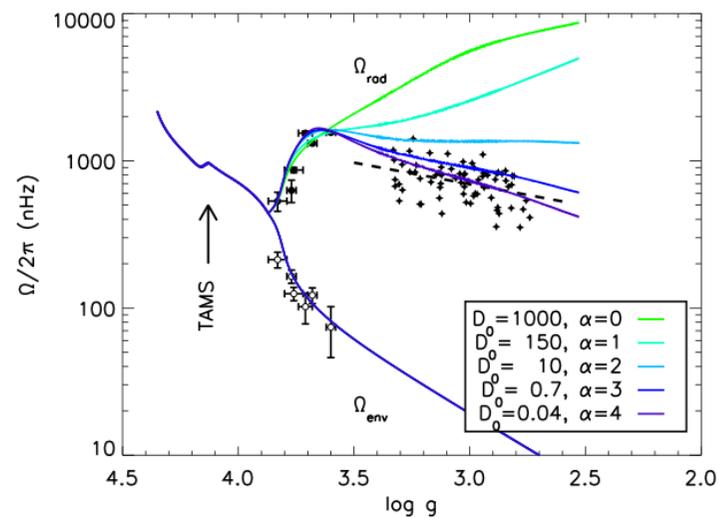
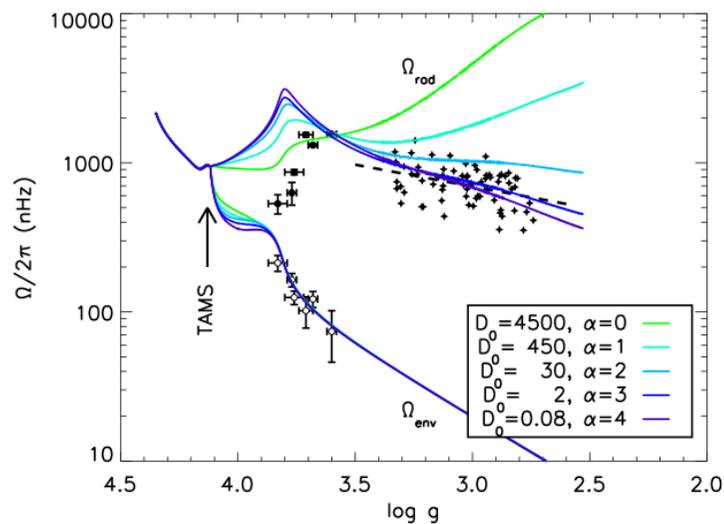
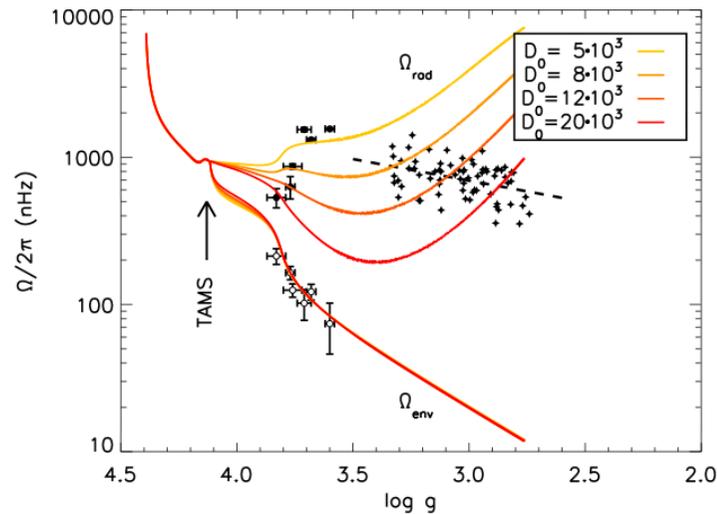


Magnetic fields

- Modeling additional AM transport as an ad hoc diffusion process (Spada et al. 2016)

$$\rho r^4 \frac{\partial \Omega}{\partial t} = \frac{\partial}{\partial r} \left[\rho r^4 D \frac{\partial \Omega}{\partial r} \right]$$

$$D = D_0 \left(\frac{\Omega_{\text{rad}}}{\Omega_{\text{env}}} \right)^\alpha$$

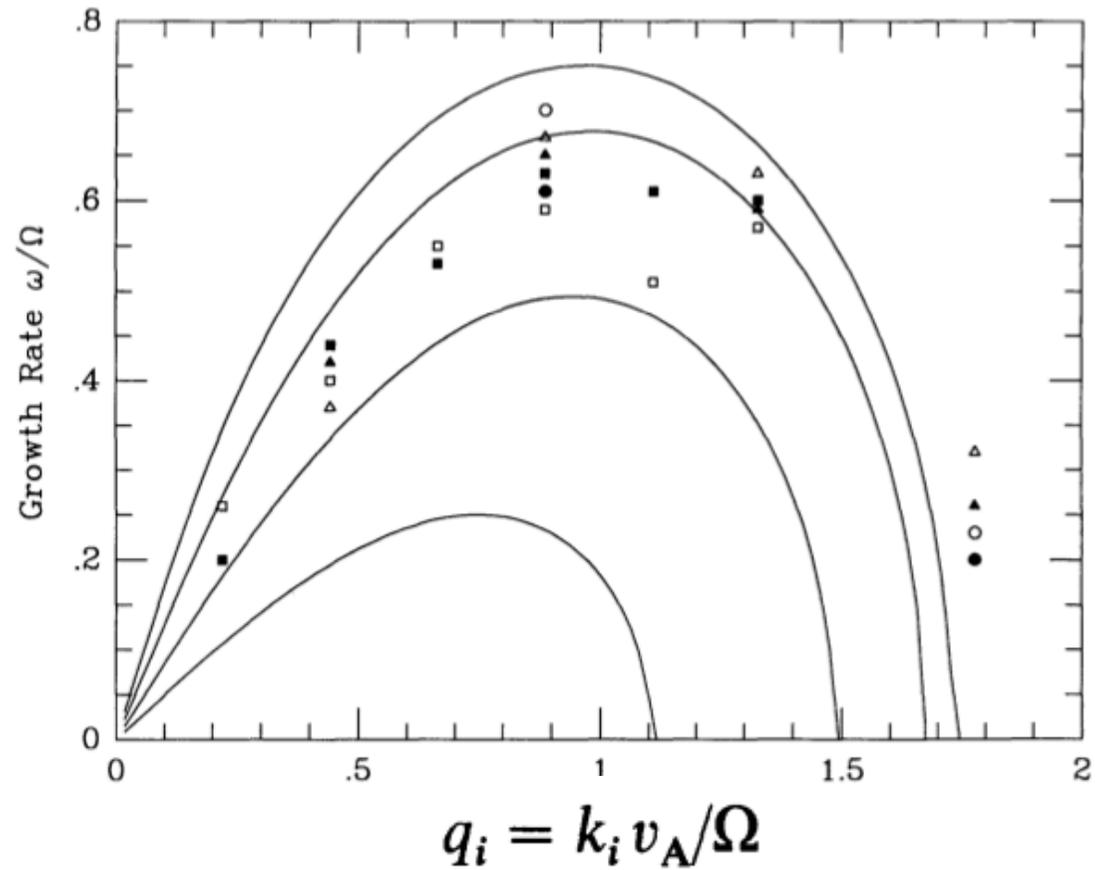


Conclusions

- Combination of observations, particularly interesting to test theory
 - Mass, radius, surface gravity (scaling relations)
 - Core (+envelope) rotation (rotational splittings)
 - Surface abundances (spectroscopic follow-up, APOKASC)
 - Luminosities (GAIA)
- Many other exciting results!
 - Potential signature of magnetic fields in the core of red giants from giants with $\ell=1$ depressed modes (Denis Stello and Matteo Cantiello's talk)
 - 1st detection of a Li-rich giant of a core-He burning giant (Silva Aguirre et al. 2014)
 - Mass loss using clusters (Miglio et al. 2012)
 - Acoustic glitches (Miglio et al. 2010, Vrad et al. 2015)
 - Using mixed modes in subgiants to measure MS convective cores (Deheuvels et al. 2011)
 - Detection of non-radial oscillation in M-giants (Stello et al. 2014)

AMRI

(Hawley & Balbus 1991)



$\lambda \sim 1\%$ of core for $B = 10^5 - 10^6$ G