

# Confusion, Correlations, and the Faint Extragalactic Radio Background

Tessa Vernstrom | CSIRO Bolton Fellow

May 2019

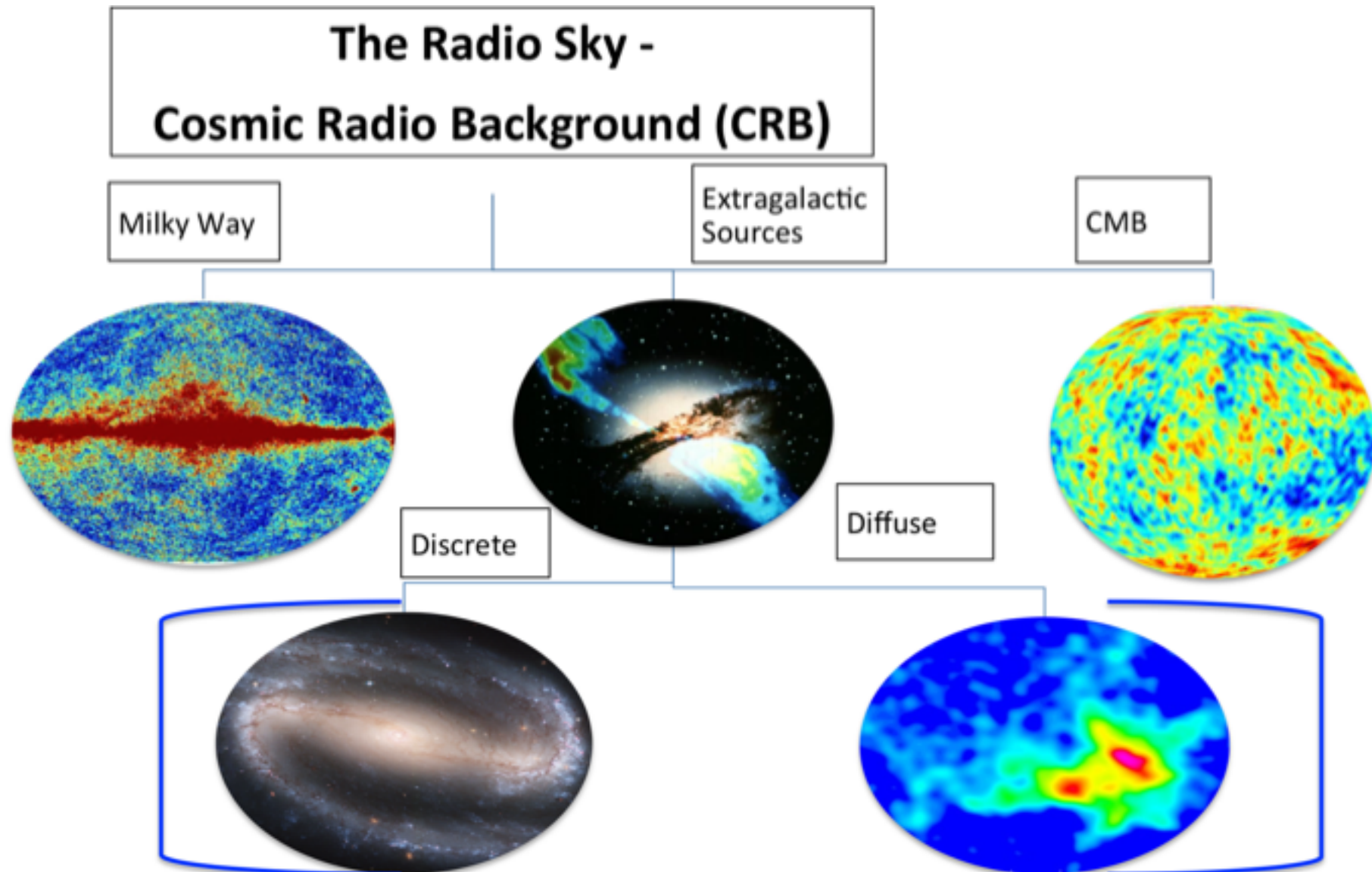
SPARCS IX – LISBON

CSIRO ASTRONOMY & SPACE SCIENCES, CASS

[www.csiro.au](http://www.csiro.au)



# The Cosmic Radio Background



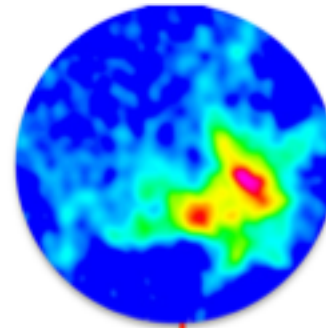
# The Cosmic Radio Background



Discrete

Point source emission:

- Starburst/star-forming galaxies
- Active Galactic Nuclei (AGN)
- Other: e.g. Dwarfs



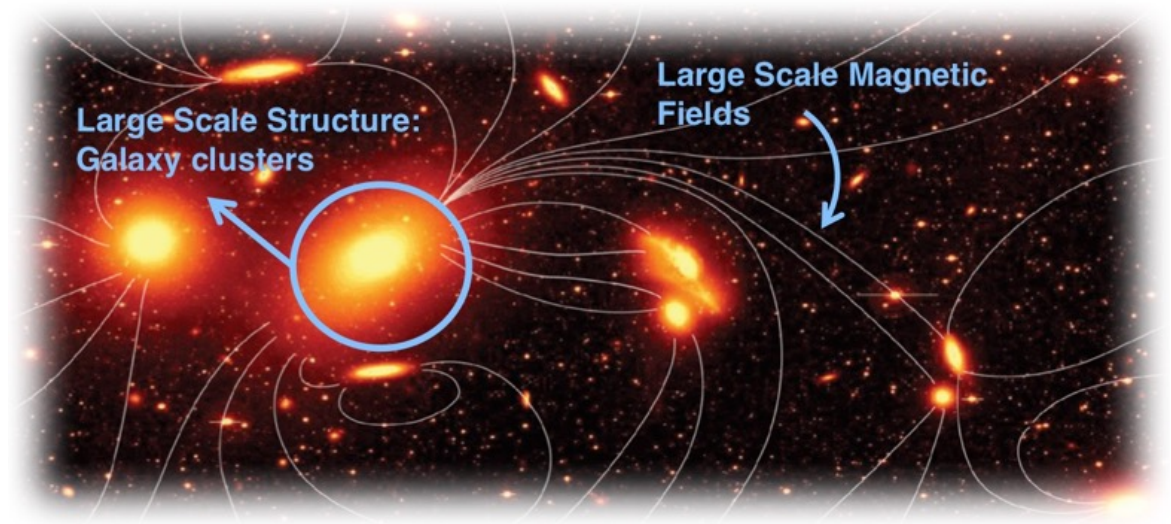
Diffuse

Low surface brightness emission:

- Galactic Halos
  - Starburst
  - AGN
- Cluster Emission
  - Giant/mini radio halos
  - Radio relics
  - Intra-cluster medium
- Cosmic web/Large Scale Structure

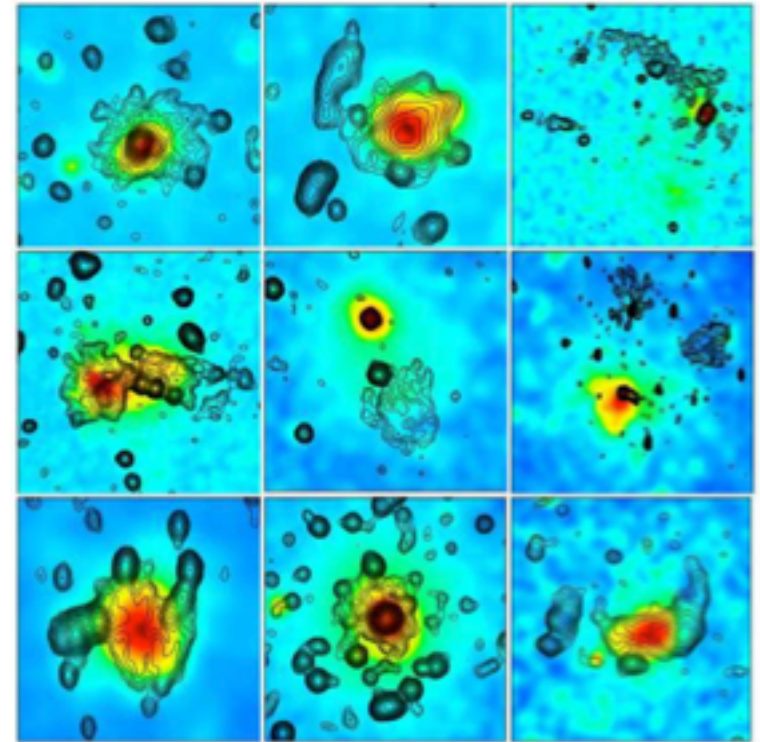
# How Can We Detect It?

- **Direct imaging**
- **Statistical methods:**
  - **Confusion**
  - **Cross Correlation**
  - **Stacking**
- **Polarization:**
  - **Faraday rotation from background AGN**
  - **Dispersion from fast radio bursts**

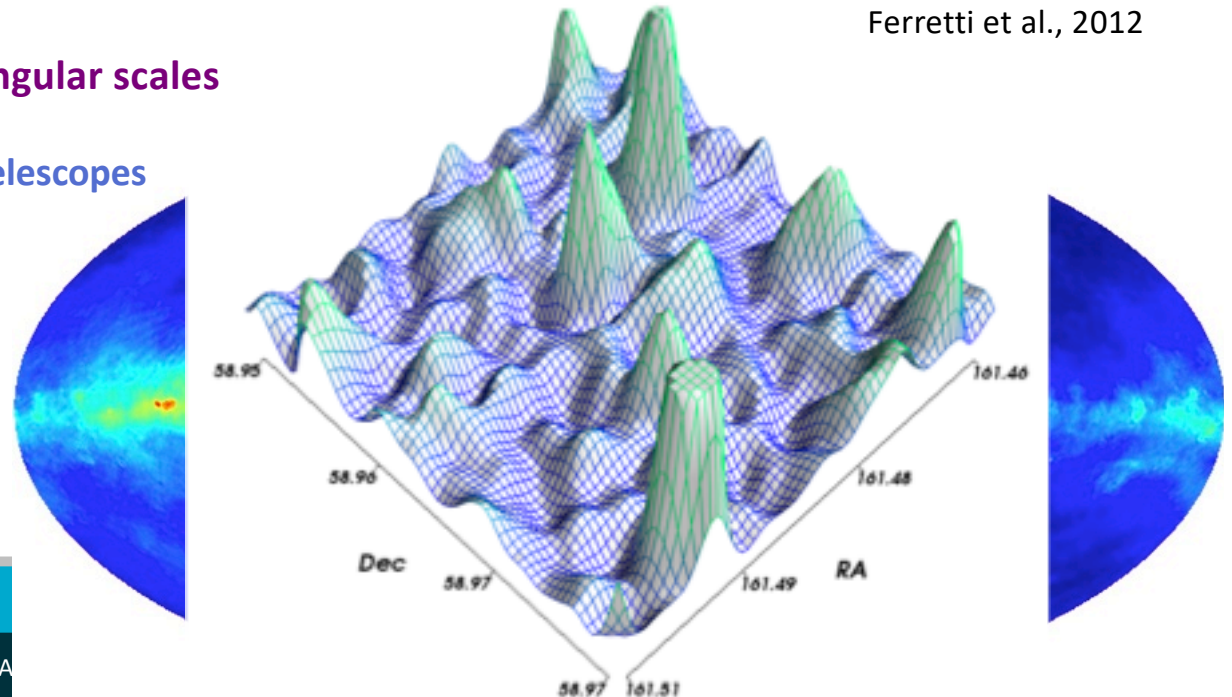


# Diffuse Emission – Direct Imaging

- Diffuse emission in clusters
  - Halos
  - Mini-halos
  - Relics
  - But only few hundred detected (more coming now from low frequency surveys)
- Only bright sources ( $>1\text{mJy}$ ) in high(er) mass clusters detected.
- Difficult to directly detect due to:
  - low surface brightness
  - Requires high sensitivity to large angular scales
    - Sizes up to Mpc scales
    - Difficult for radio interferometer telescopes
  - Bright Galactic foregrounds
  - Bright point sources
  - Faint point source confusion



Ferretti et al., 2012



# How Can We Detect It?

- ~~Direct imaging~~

- Statistical methods:

- Confusion

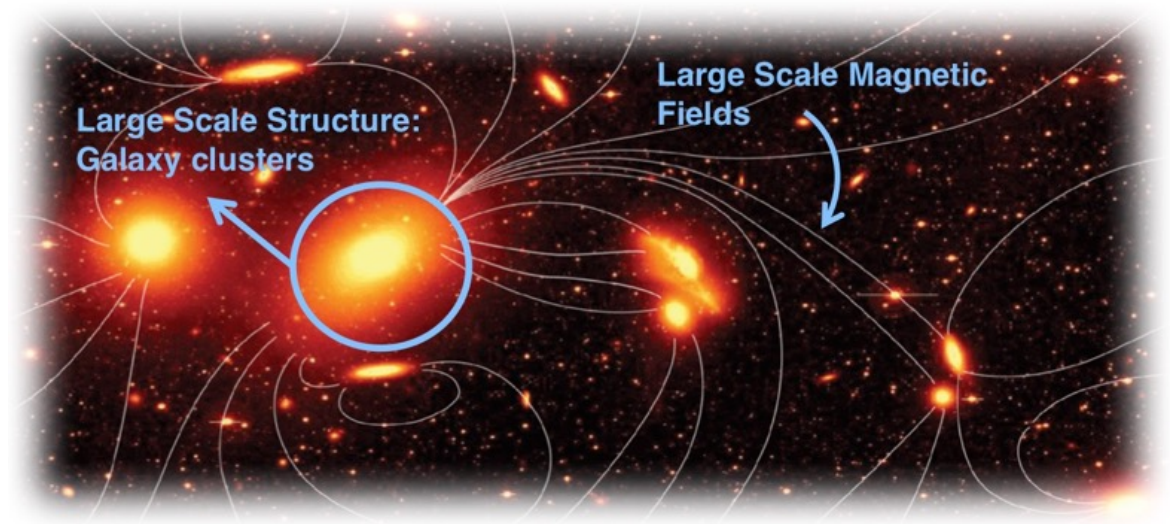
- Cross Correlation

- Stacking

- Polarization:

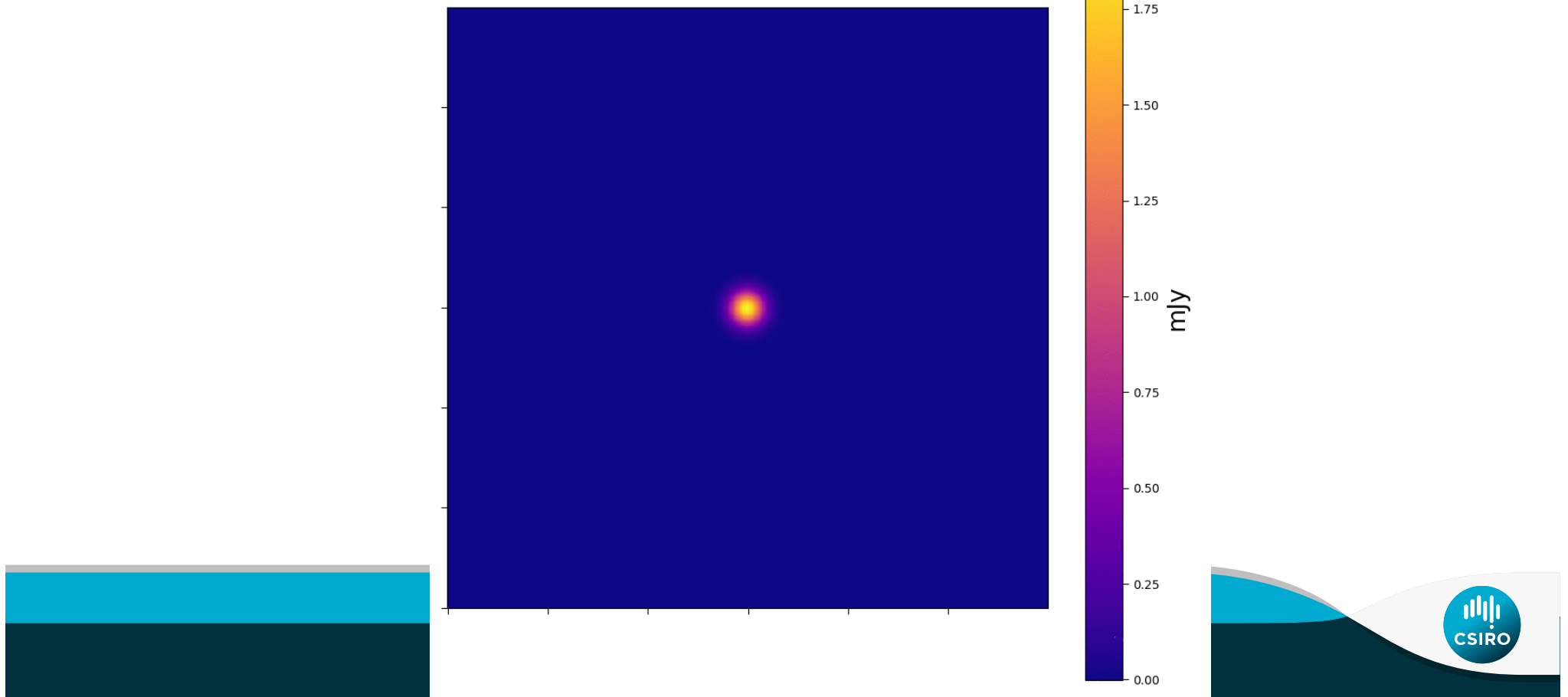
- Faraday rotation from background AGN

- Dispersion from fast radio bursts



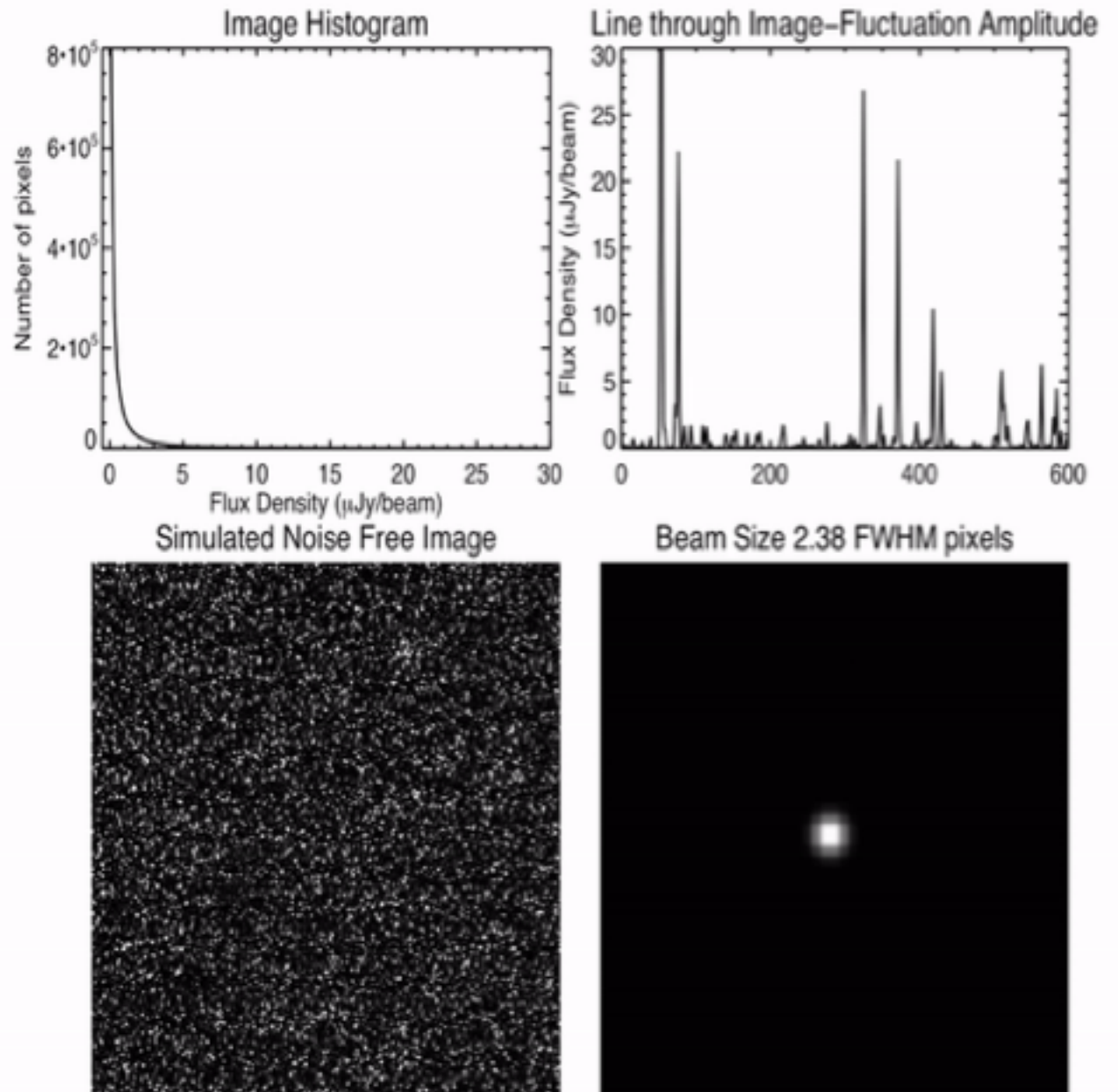
# Confusion: Friend or Foe?

- Simulated Gaussian “Halo”
  - 60” size
  - 5 mJy total brightness
  - 45” beam
  - Addition of brighter and brighter point sources
    - None brighter than 1mJy



# Using Confusion

- Confusion is the blending of faint sources within a telescope beam
- PDF of image pixel histogram from confusion known as  $P(D)$
- Confusion noise,  $\sigma_c$  ( width of  $P(D)$  )
  - governed by beam and source count





# How? Probability of Deflection

- Fitting of Image histogram  $\rightarrow$  statistical estimate of source counts as faint as  $\sim \sigma_c$

- Input

- Source count model
- Pixel size, beam shape(s)
- Instrumental noise

- Mean density of observed flux

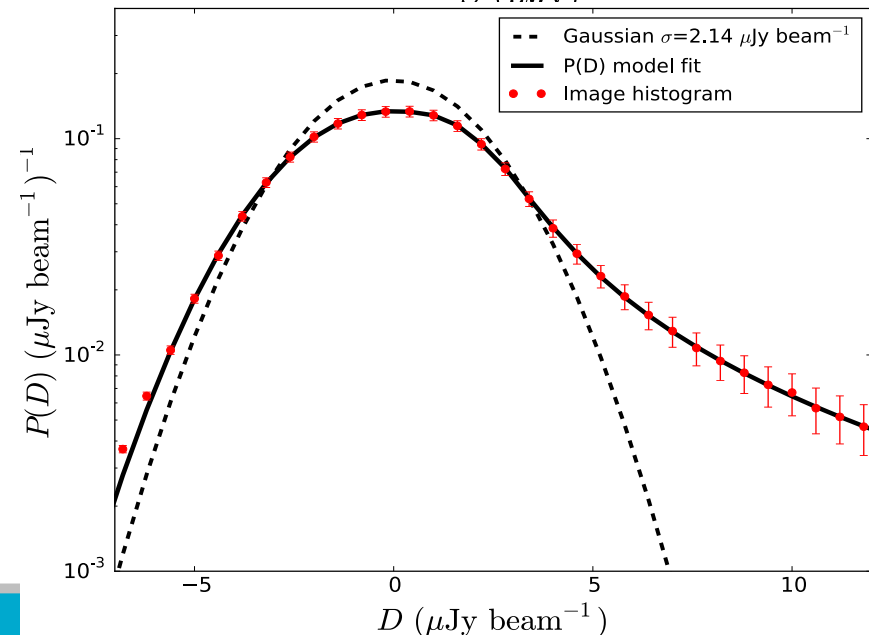
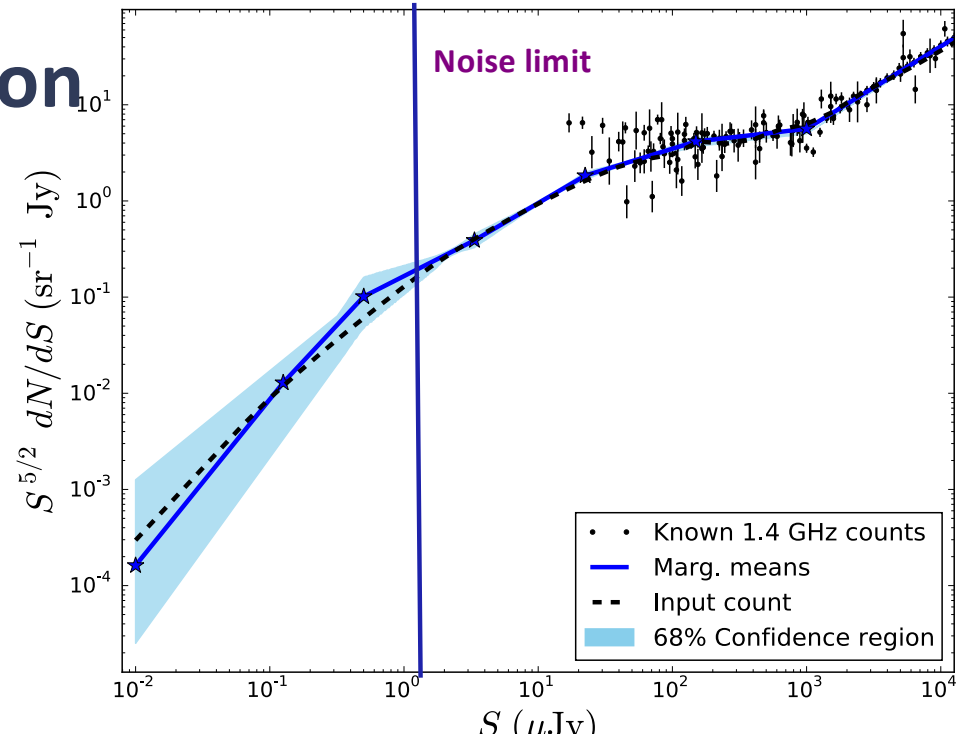
$$R(x) dx = \int_{\Omega} \frac{dN(x)}{dS} \left(\frac{x}{b}\right) b^{-1} d\Omega dx$$

$$P(D) = \mathcal{F}^{-1} \left[ \exp \left( \int_0^{\infty} R(x) e^{iwx} dx - \int_0^{\infty} R(x) dx - i\mu w - \frac{\sigma_n^2 w^2}{2} \right) \right]$$

- Can use any continuous source count model

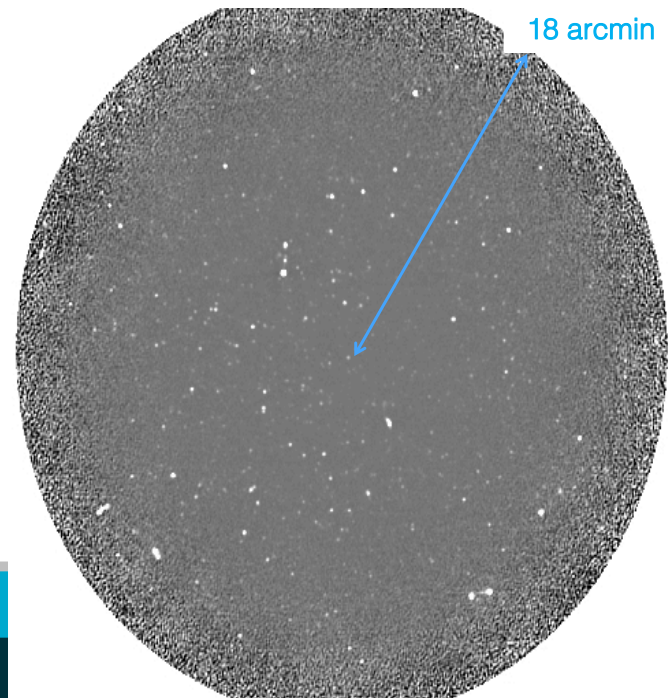
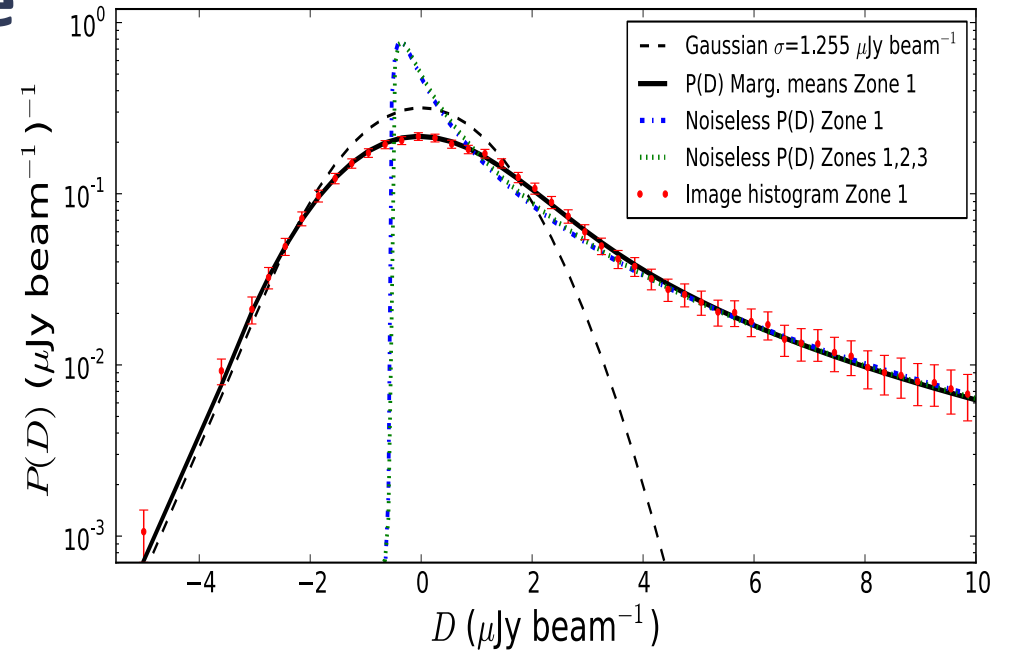
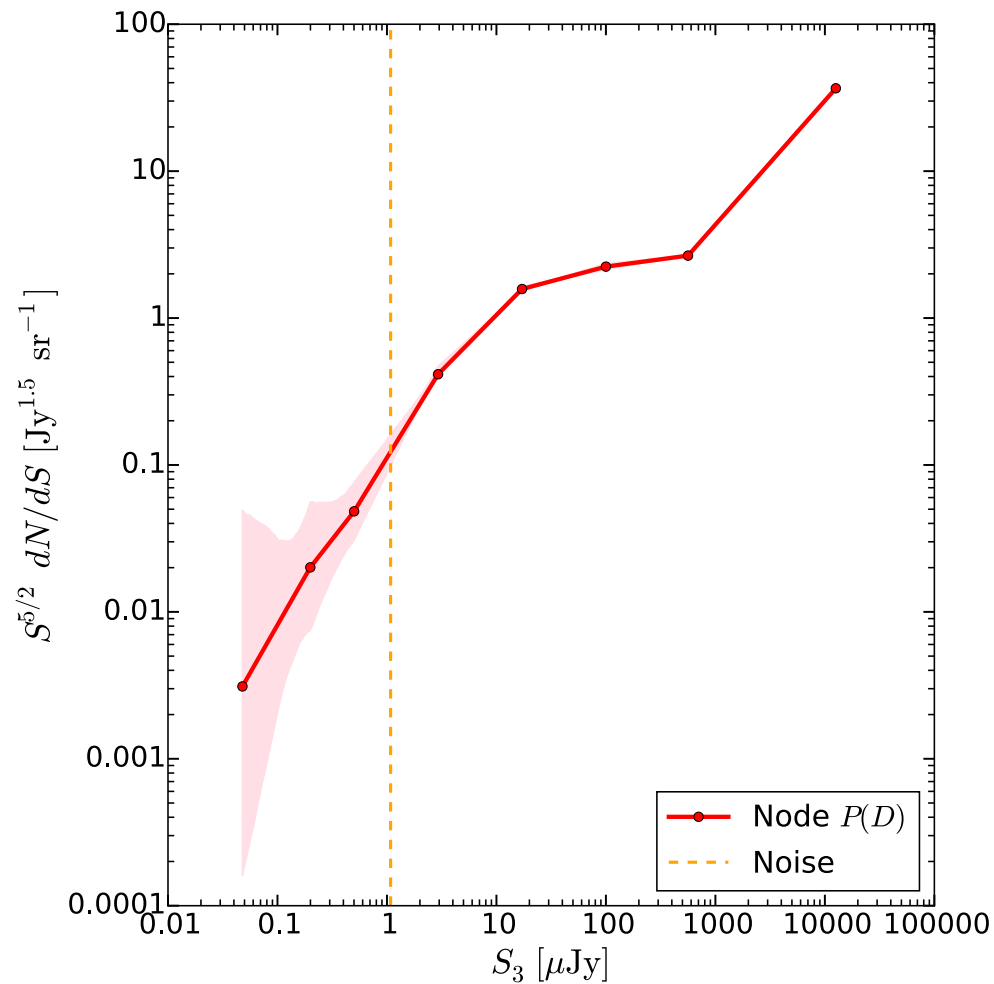
- Node model

- Fixed position in Log(S)
- Fit amplitude of node in Log(dN/dS)
- Interpolate between nodes
- Set of connected power-laws



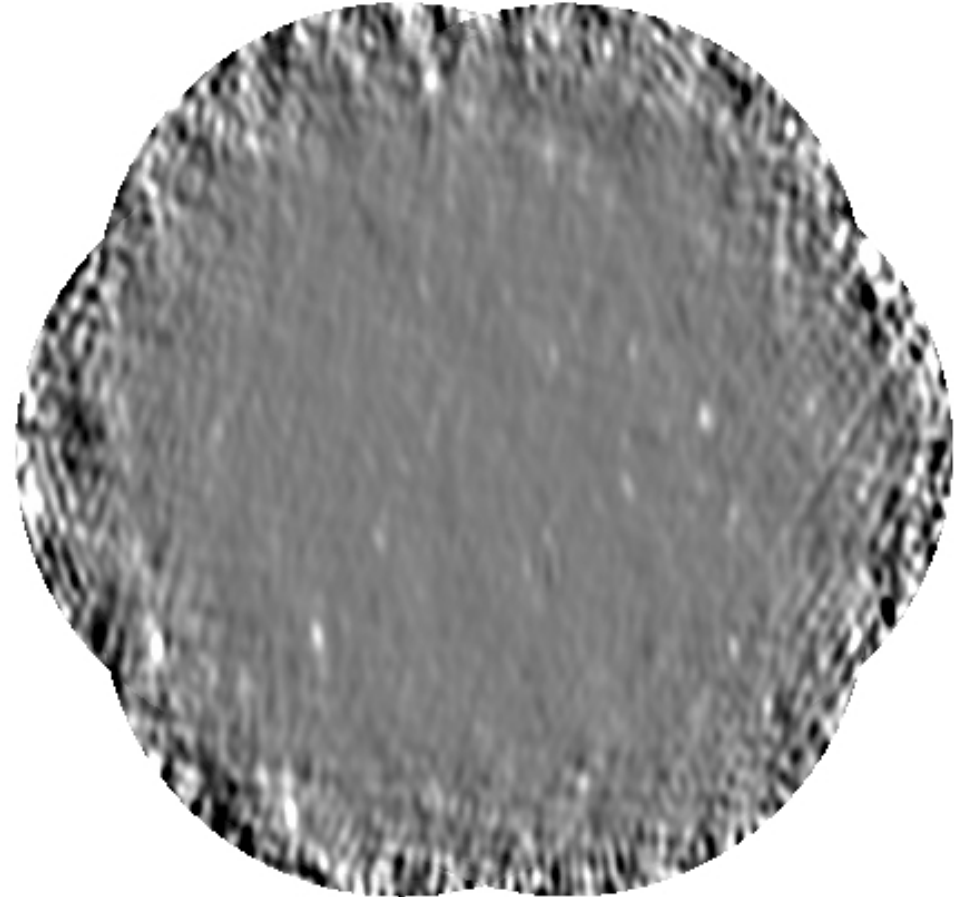
# P(D) Source Count - Discrete

JVLA 3GHz Lockman Hole North



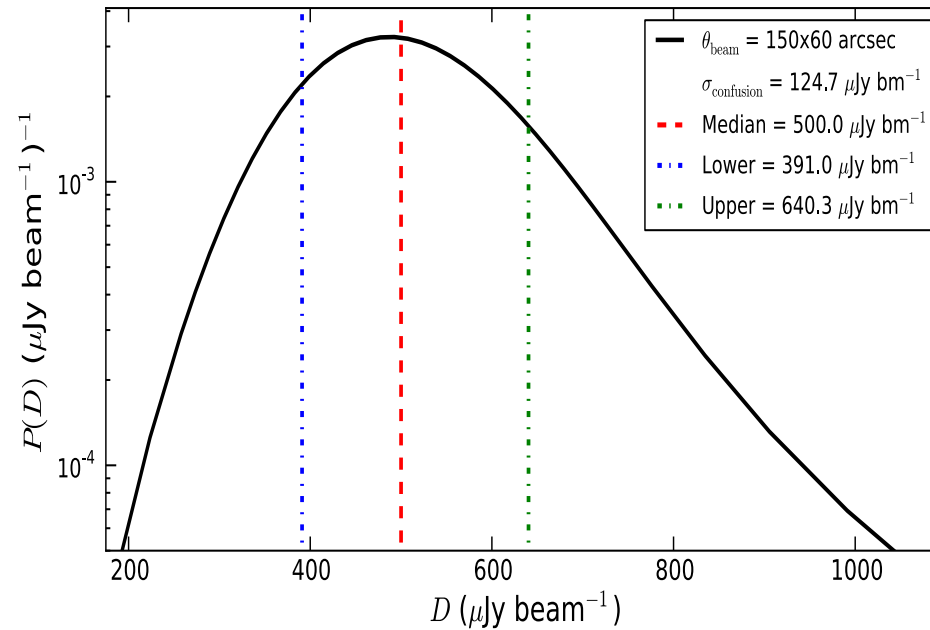
# Confusion Diffuse Emission - Data

- Can try to statistically detect presence of sources too faint or diffuse to be detected normally
- Subtract point sources or use discrete source count model
- Example: ATCA
  - ELAIS S1
  - 7 pointing mosaic
  - 1.7 GHz
  - 2.5' x 1' beam
  - RMS ~ 50  $\mu$ Jy
  - Subtraction limit ~150  $\mu$ Jy
- Use ATLAS point source models to subtract bright sources and JVLA discrete count for un-subtracted sources



# Confusion Diffuse Emission - Results

- Can try to statistically detect presence of sources too faint or diffuse to be detected normally
- Subtract point sources or use discrete source count model
- Example: ATCA
  - ELAIS S1
  - 7 pointing mosaic
  - 1.7 GHz
  - 2.5' x 1' beam
  - RMS ~ 50  $\mu\text{Jy}$
  - Subtraction limit ~150  $\mu\text{Jy}$
- Use ATLAS point source models to subtract bright sources and JVLA discrete count for un-subtracted sources



Model P(D) of faint sources

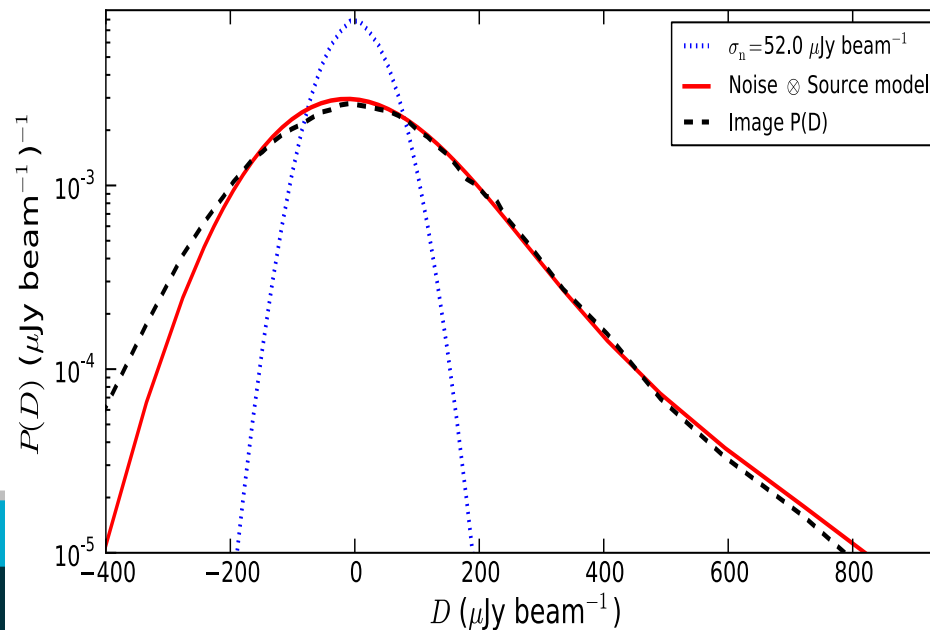
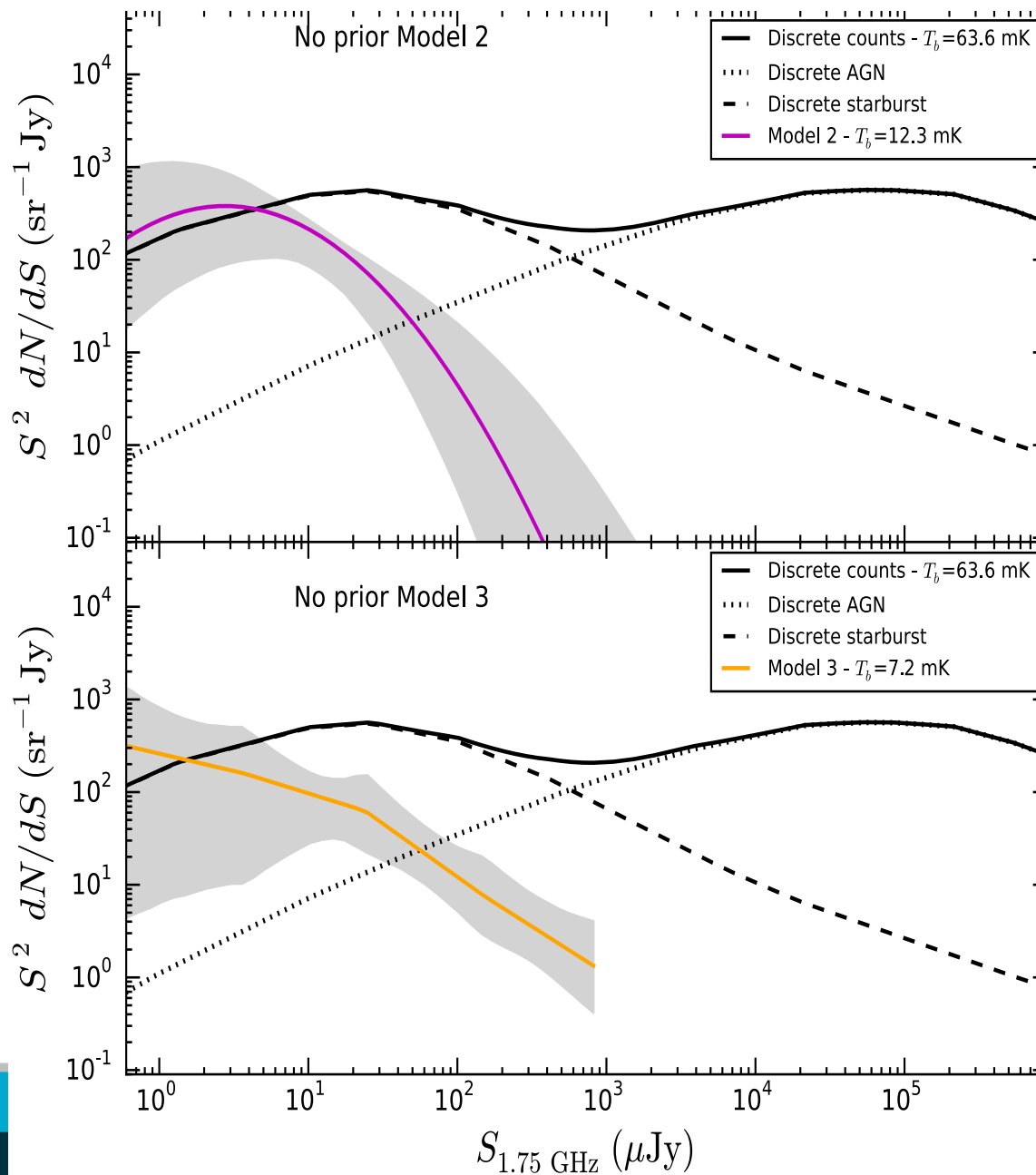


Image P(D) compared to model  
 $\leftarrow 3\sigma$  difference

# Confusion Diffuse Emission - Results

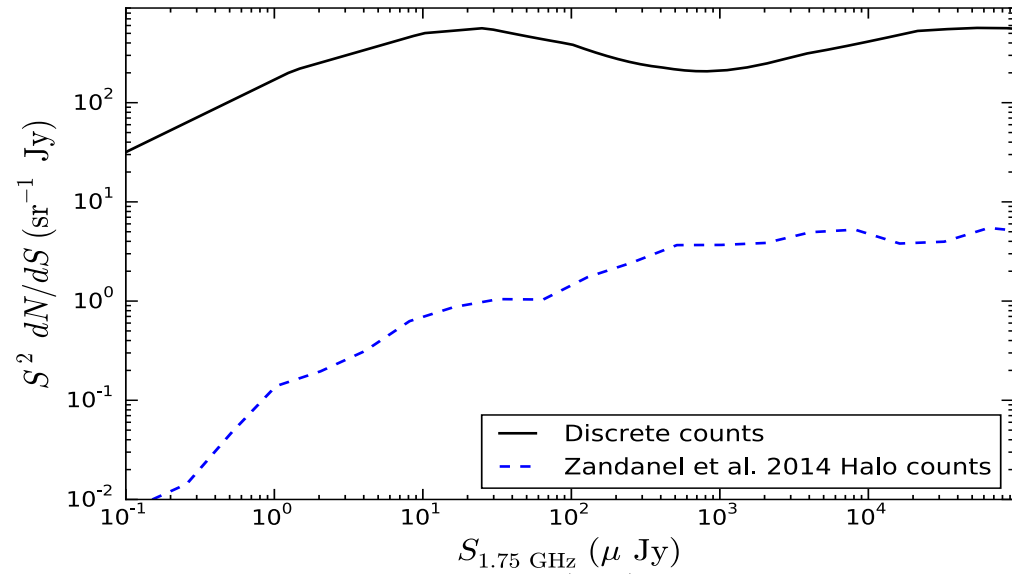
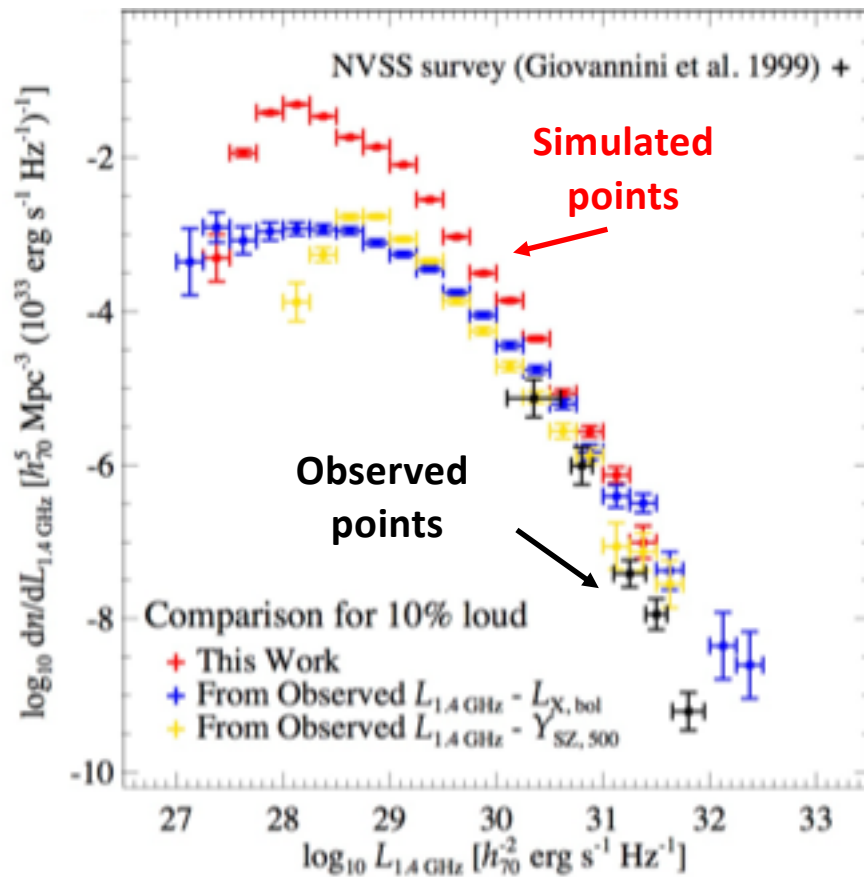
Model:  
Parabola



Model:  
Nodes

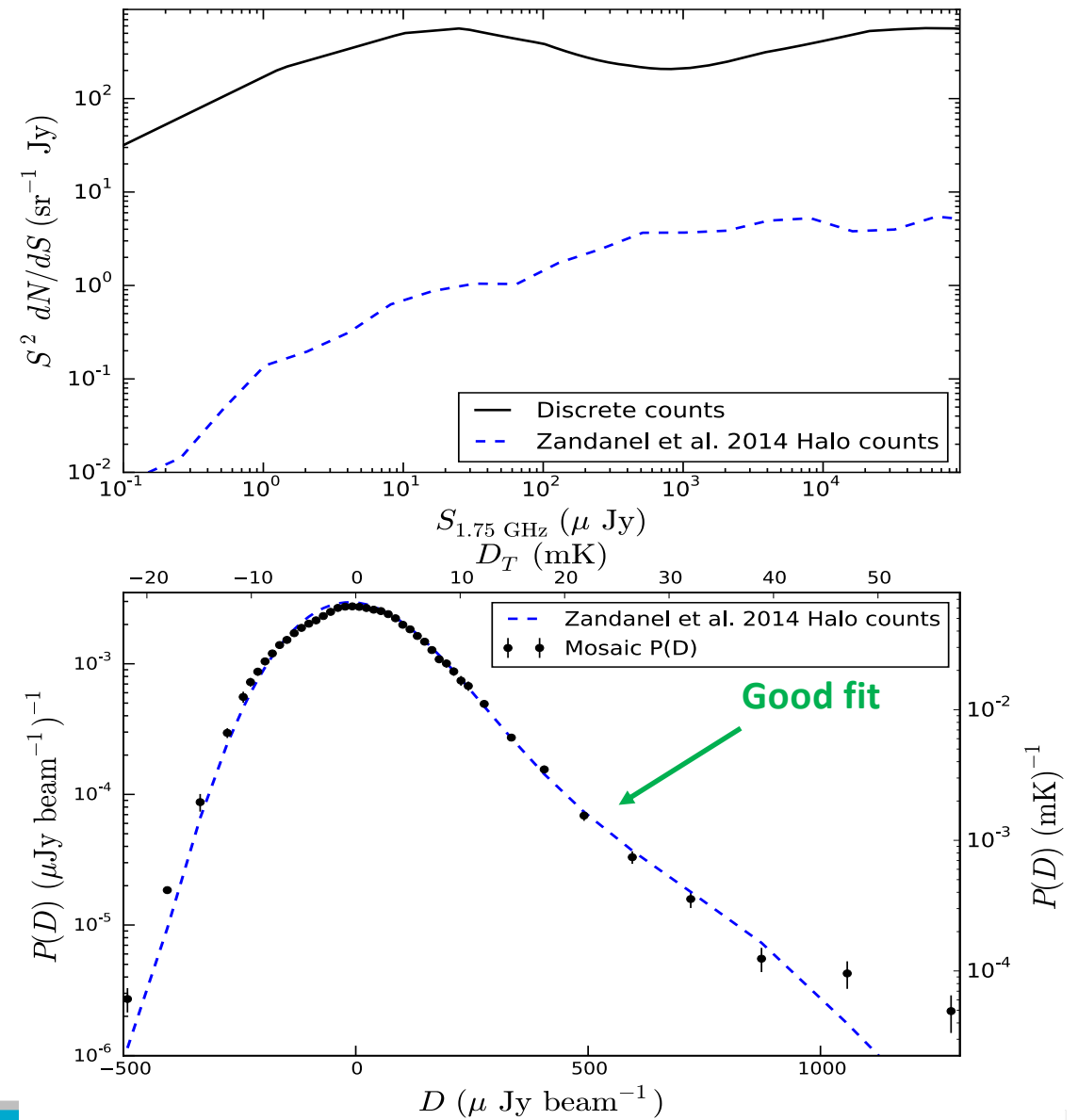
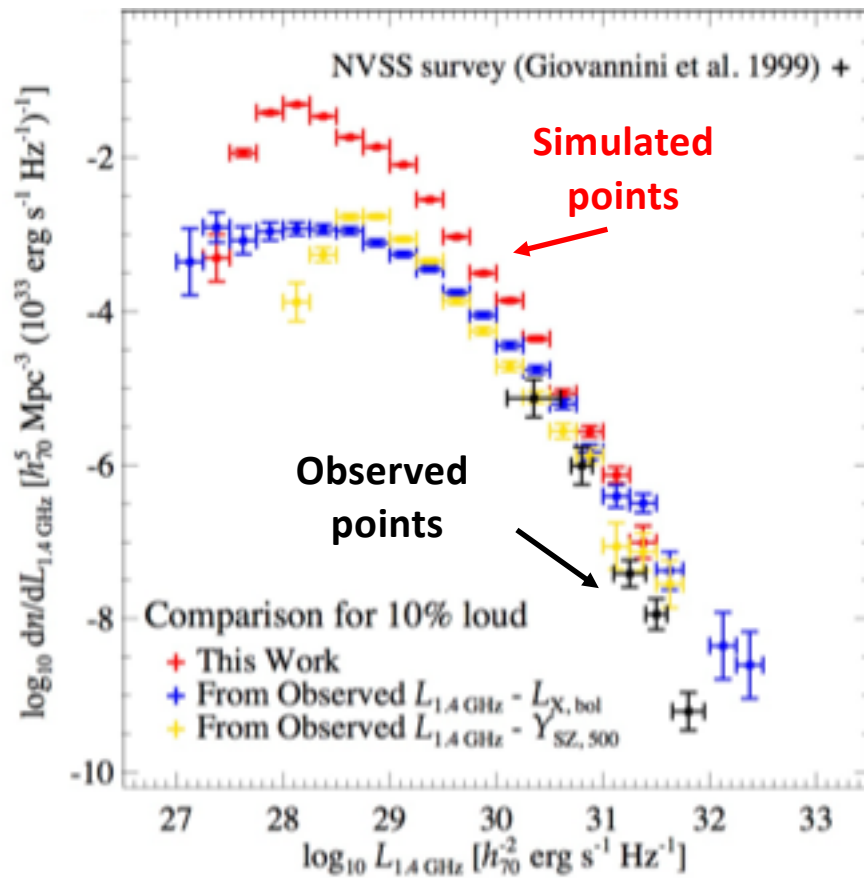
# Confusion Diffuse Emission - Models

- Simulated model from Zandanel et al 2014 of cluster haloes



# Confusion Diffuse Emission - Models

- Simulated model from Zandanel et al 2014 of cluster haloes



# Confusion Diffuse Emission

## Advantages:

- Detection of emission below confusion level
- Possible to constrain models of cluster emission

## Disadvantages / Caveats:

- Assumes emission smaller than (or roughly equal to) the beam size
- Requires point source subtraction and/or model for point sources
- Need to know beam shape(s) and noise properties well

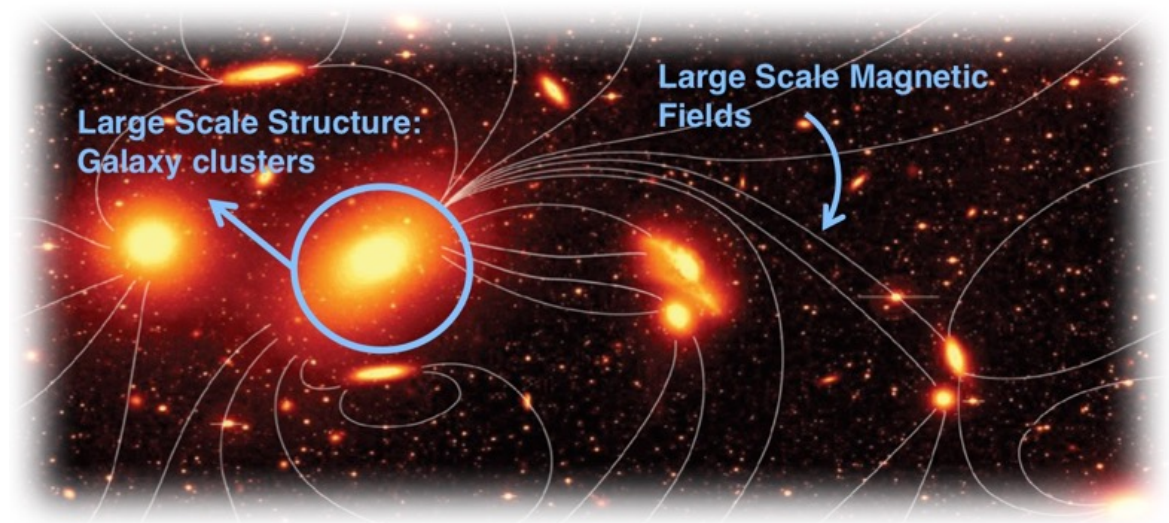
## Future work / Continuations:

- Repeat with different / larger area
- Compare results for regions with and without known diffuse emission
- Different (lower) frequency



# How can we detect it?

- ~~Direct imaging~~
- **Statistical methods:**
  - Confusion
  - Cross Correlation
  - Stacking
- **Polarization:**
  - Faraday rotation from background AGN
  - Dispersion from fast radio bursts

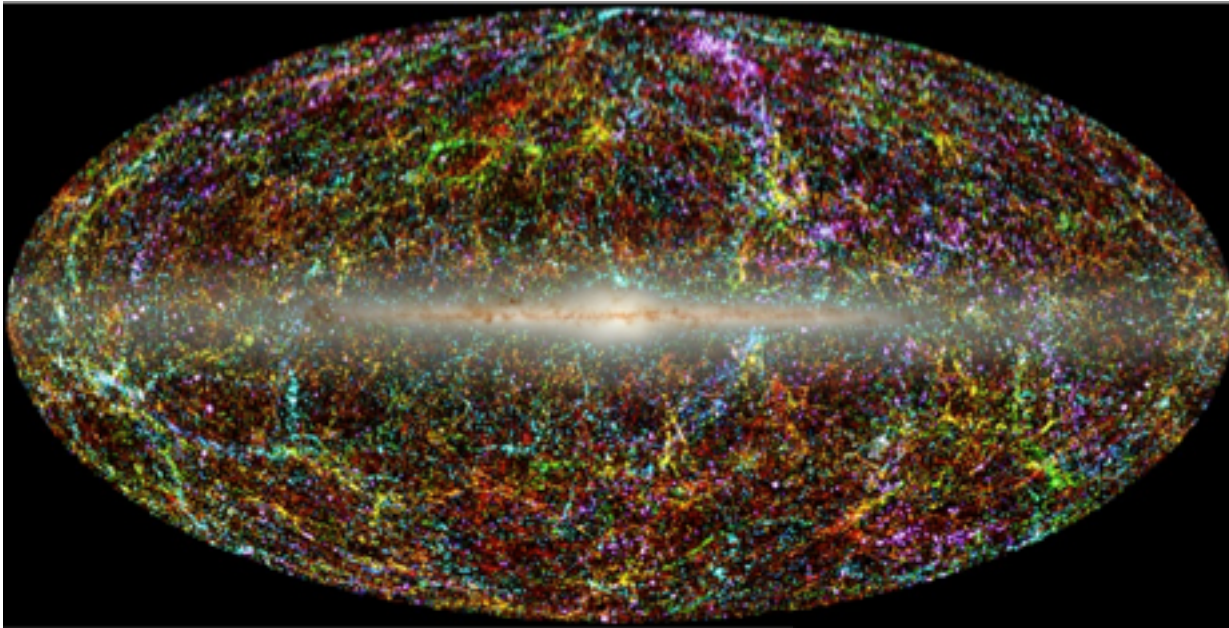


# Cosmic Web - Cross Correlation

- Galaxy number density  $\rightarrow$  traces thermal baryon distribution  $\rightarrow$  should correlate with diffuse synchrotron

# Cosmic Web - Cross Correlation

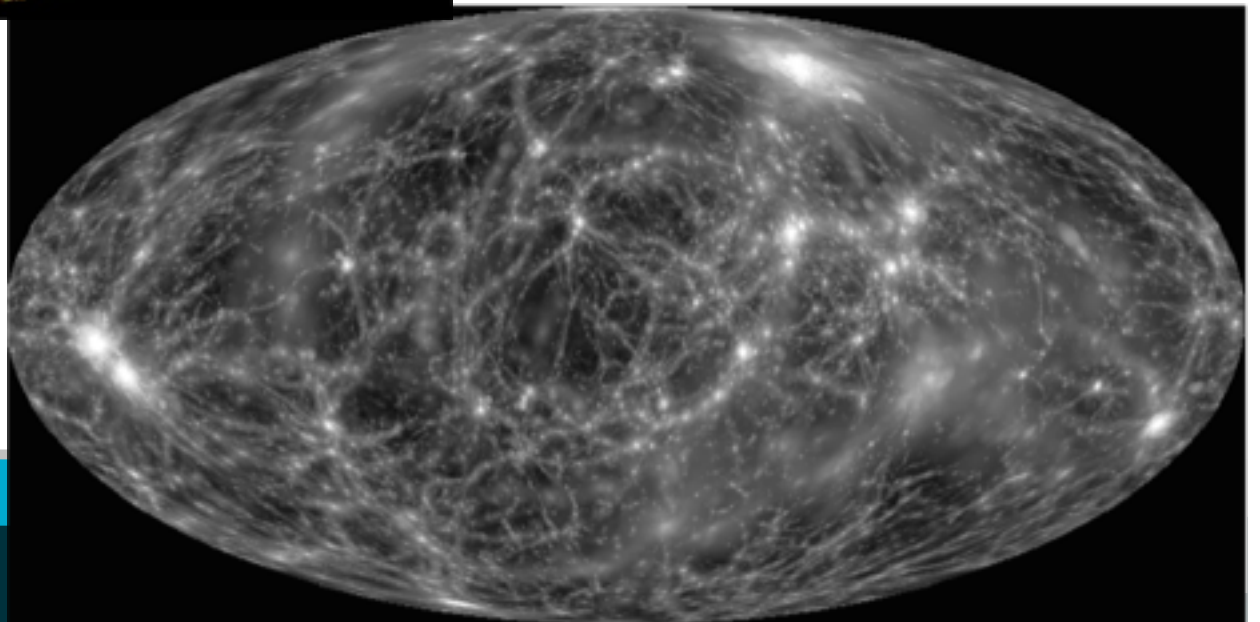
- Galaxy number density  $\rightarrow$  traces thermal baryon distribution  $\rightarrow$  should correlate with diffuse synchrotron



2MASS Galaxy Distribution coded by redshift

(photo credit :Thomas Jarrett (IPAC/Caltech))

Simulated radio synchrotron  
(credit: Klaus Dolag)



# Cosmic Web - Cross Correlation

- Galaxy number density → traces thermal baryon distribution → should correlate with diffuse synchrotron
- How correlated as a function of distance or angular scale?
  - Unknown
- How correlated?
  - Unknown
- Reasons for a **positive** correlation:
  - AGN (core)
  - Starbursts and disk emission
  - AGN (WAT and NAT associated with clusters)
  - Cluster halos
  - Cluster relics
  - Synchrotron cosmic web
- Reasons for a **negative** correlation:
  - Galactic extinction (galaxy number counts down, synchrotron up)



Increasing angular  
scale

# Cross Correlation with MWA

## The MWA:

- Frequency range: 80 – 300 MHz
- 2048 dual polarization dipoles
- Number of antenna tiles: 128
- Number of baselines: 8128
- Collecting area: 2000 sq. meters
- FOV: 15 - 50 deg. (200 - 2500 sq. deg.)
- Polarization: I, Q, U, V

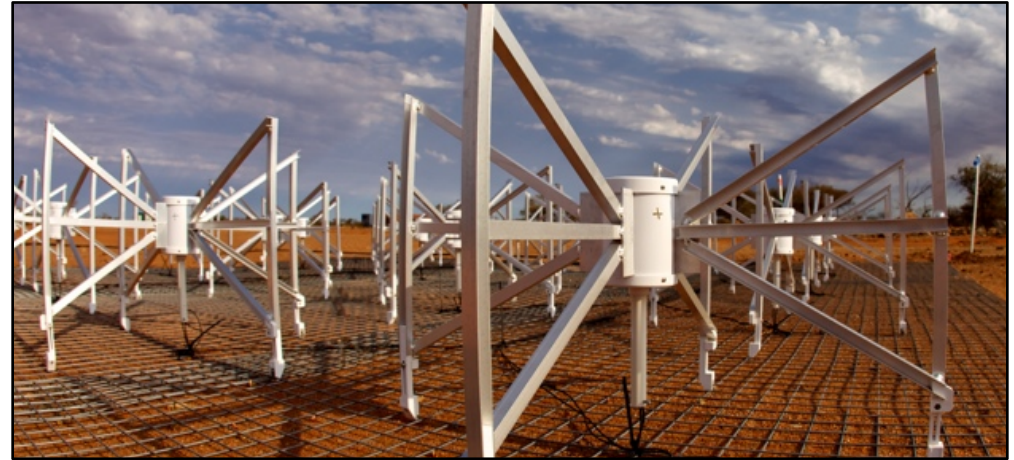


Photo credit: Natasha Hurley-Walker

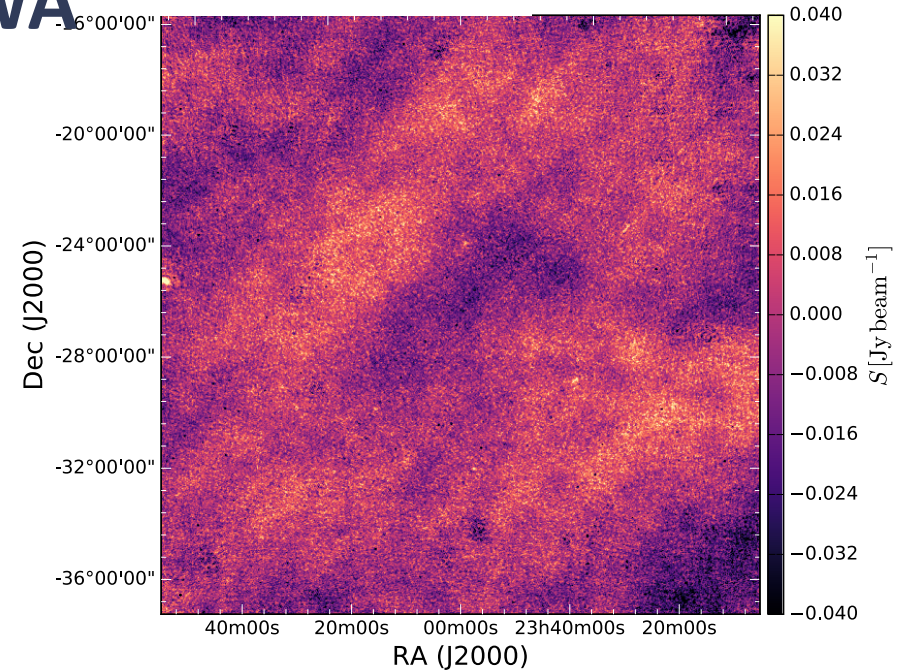


Good sensitivity to large angular scales,  
low frequency, large field of view

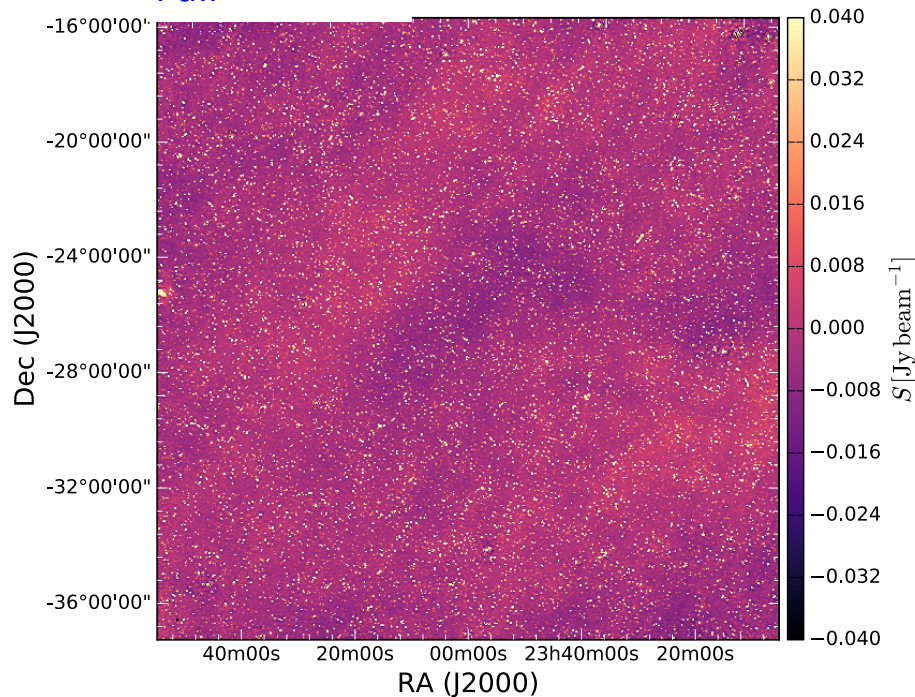
# Cross Correlation with MWA

- Field: EoR0 RA=0 Dec= -27
- $\nu = 180$  MHz
- Beam 2.3' – 2.9'
- $\sigma_n = 0.6 - 0.96$  mJy beam<sup>-1</sup>
- $\sigma_c = 4.4 - 9.5$  mJy beam<sup>-1</sup>
- Subtraction limit  $\sim 50$  mJy

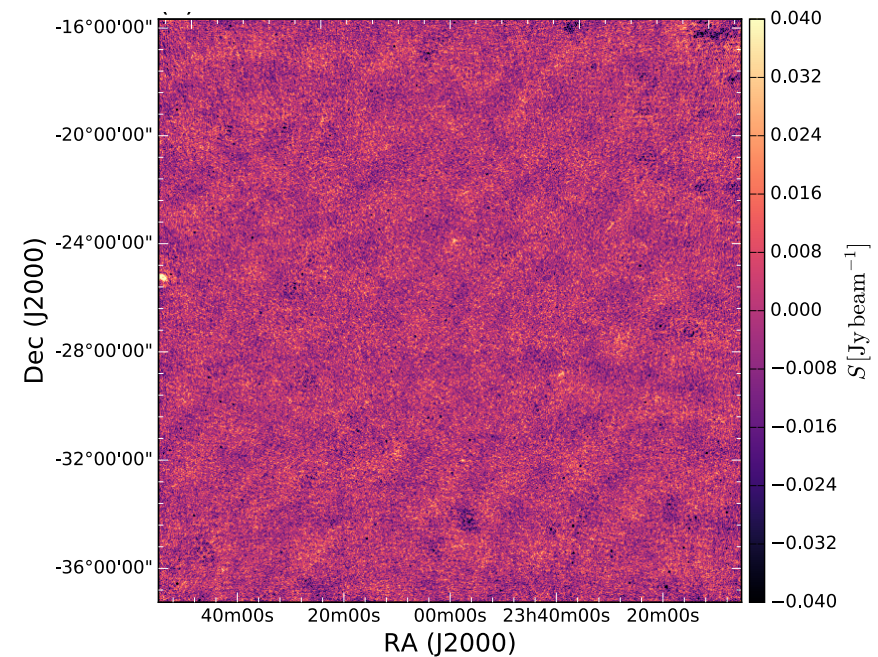
Point source sub



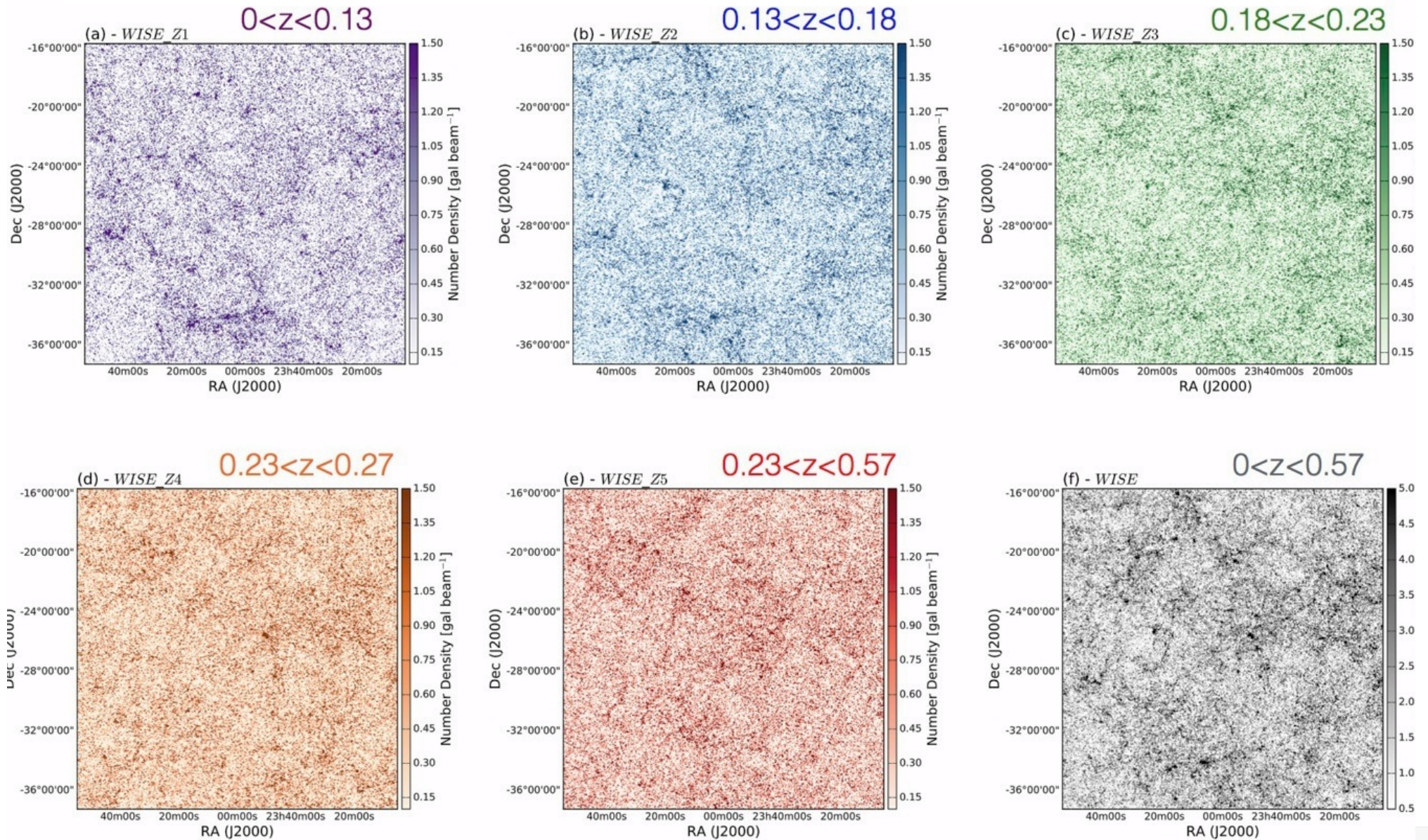
Full



Point source & Galaxy sub

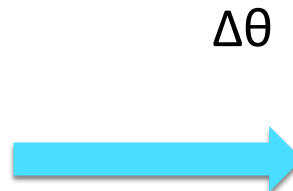
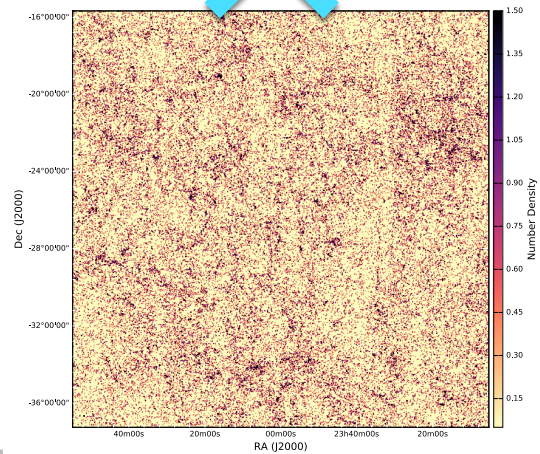
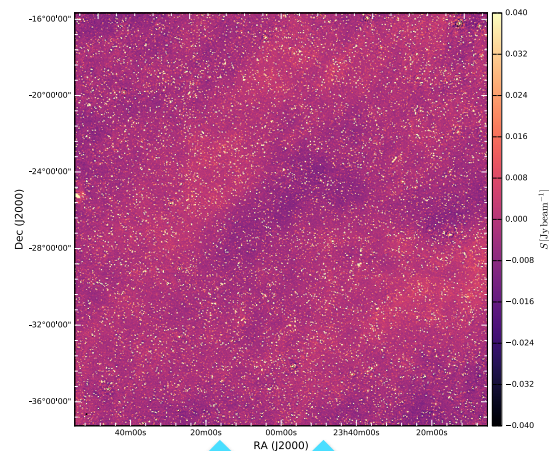


# Cross Correlation with MWA - WISE Number Density



# Cross Correlation with MWA

$$|CCF(xshift, yshift) = \frac{1}{n} \sum (R_{i,j} - \bar{R})(G_{i,j} - \bar{G})|$$



Take radial average

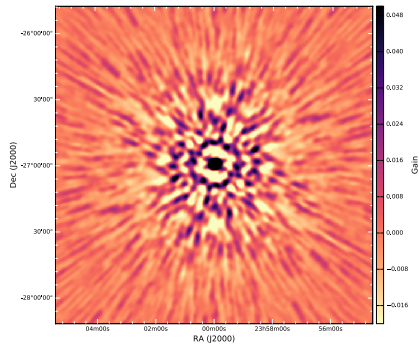




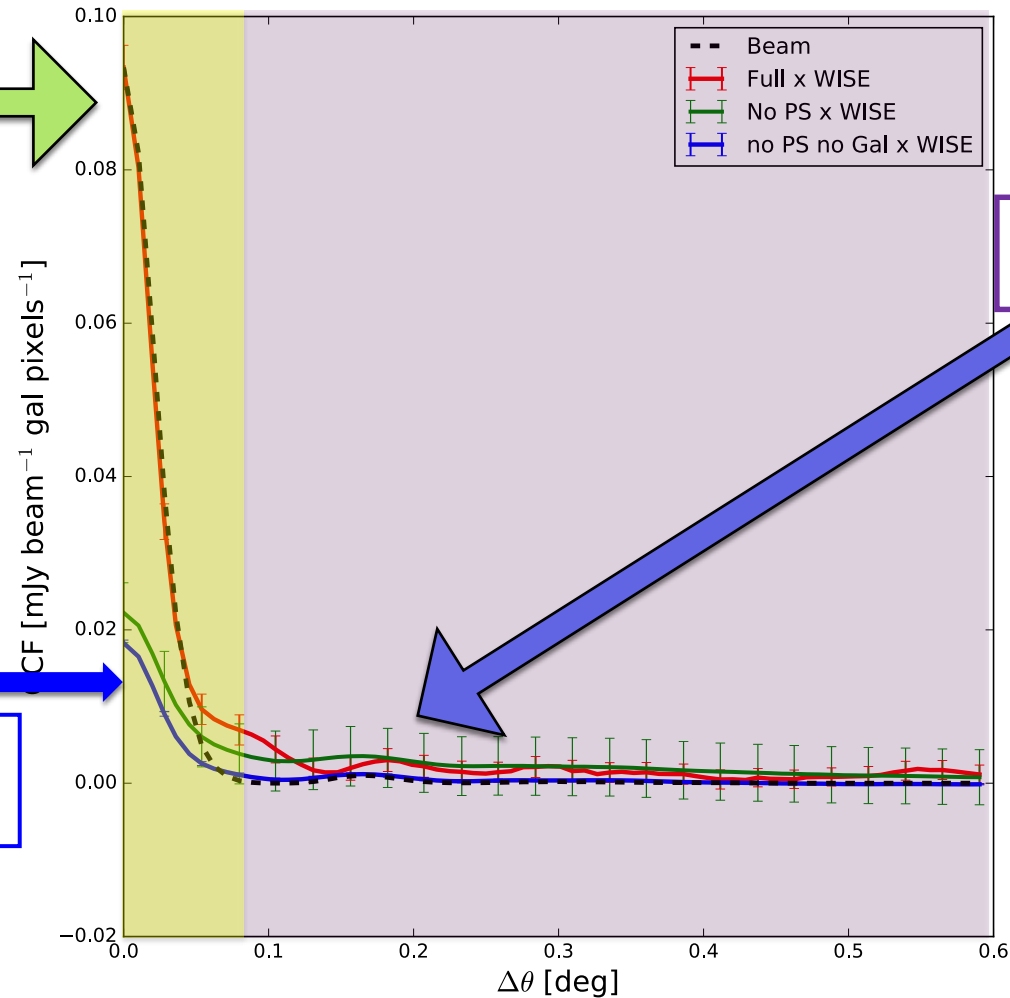
# Cross Correlation with MWA

$$|CCF(xshift, yshift) = \frac{1}{n} \sum (R_{i,j} - \bar{R})(G_{i,j} - \bar{G})|$$

Point Sources →  
smaller than beam



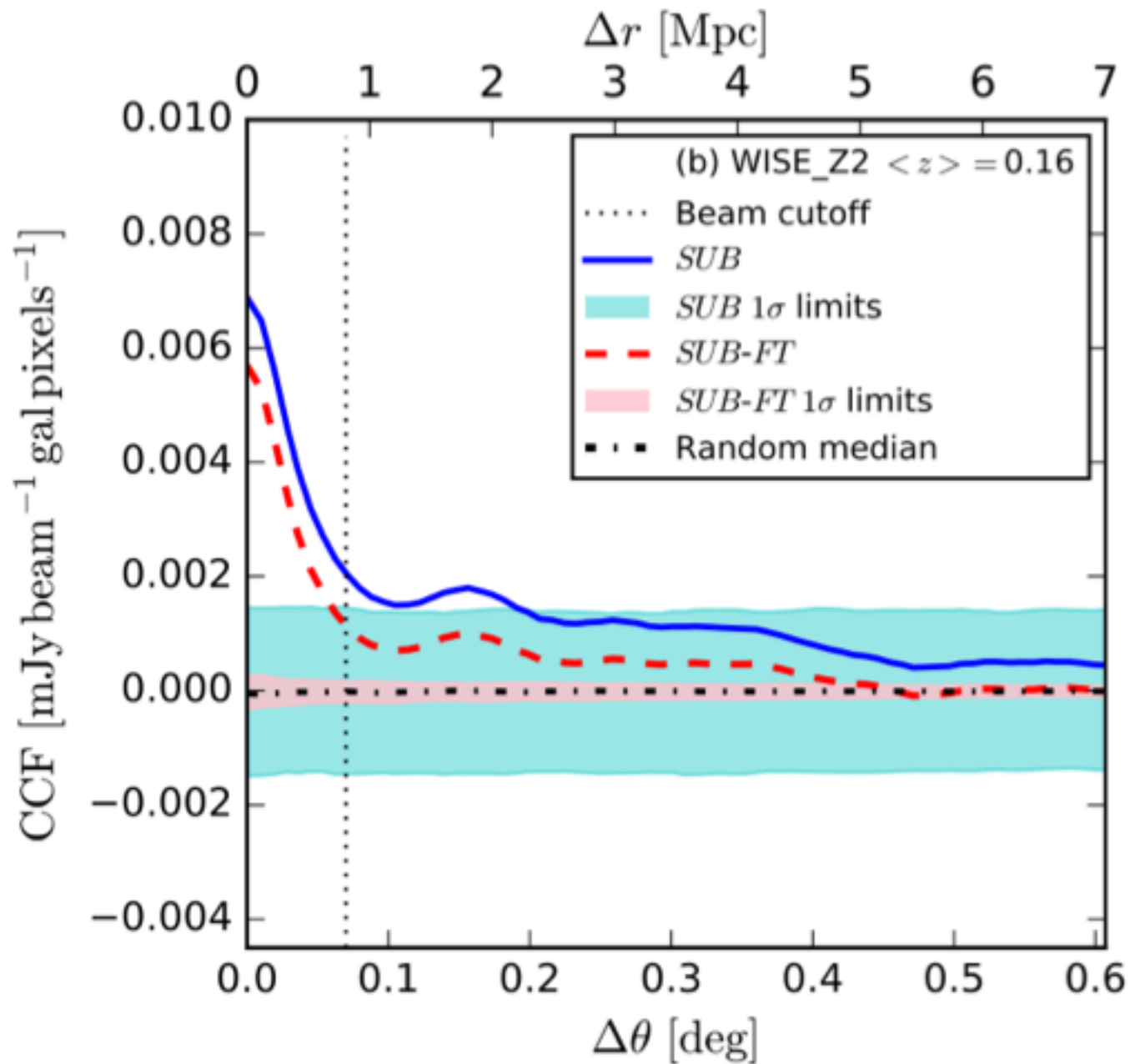
Still some point  
source contribution



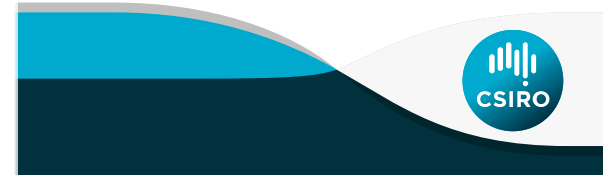
Diffuse emission  
→ larger than beam

So how much diffuse  
is there ???

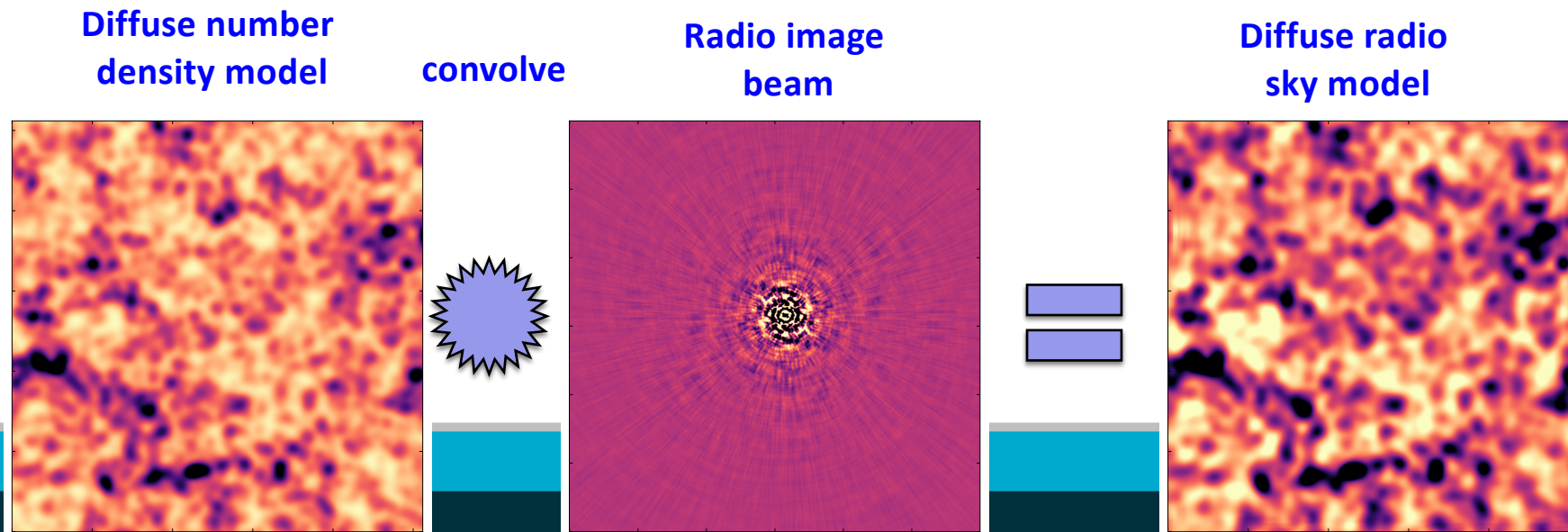
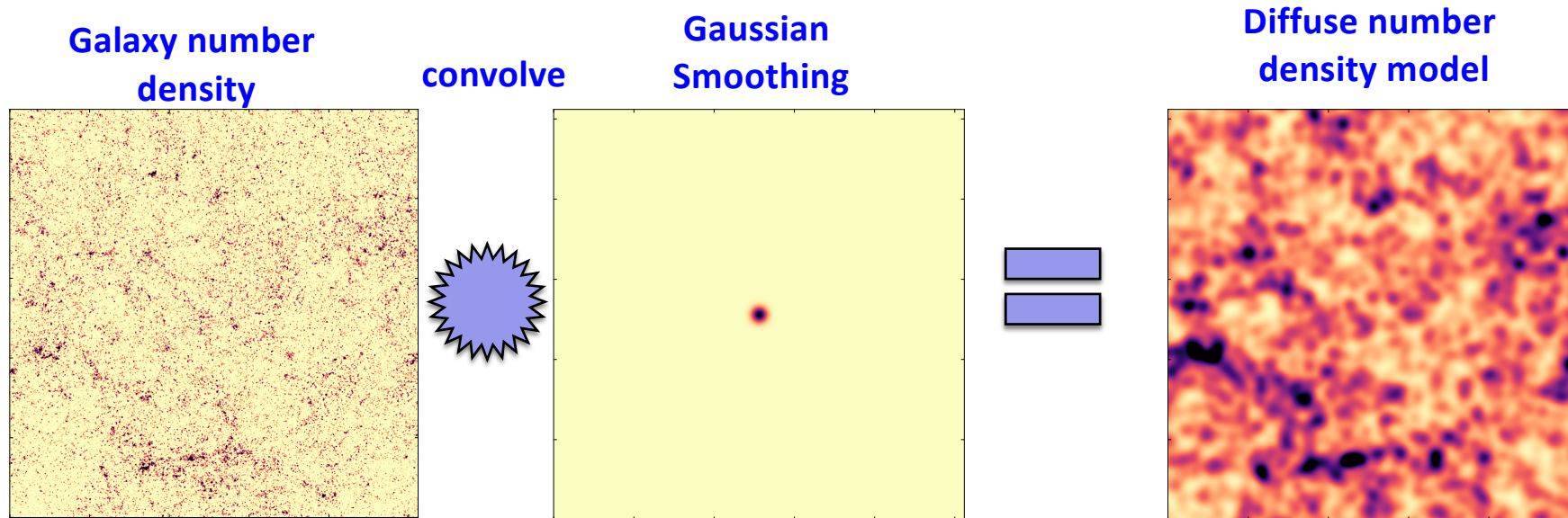
# Cross Correlation with MWA



20 total CCFs  
(2 radio images x  
10 number density maps)



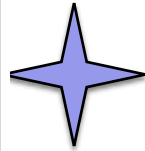
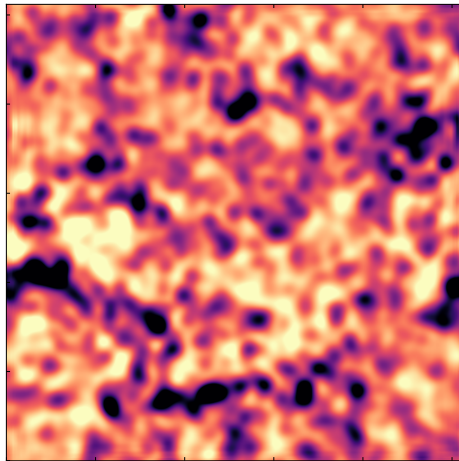
# Cross Correlation with MWA – Emission Upper Limits



# Cross Correlation with MWA – Emission Upper Limits

Diffuse radio  
sky model

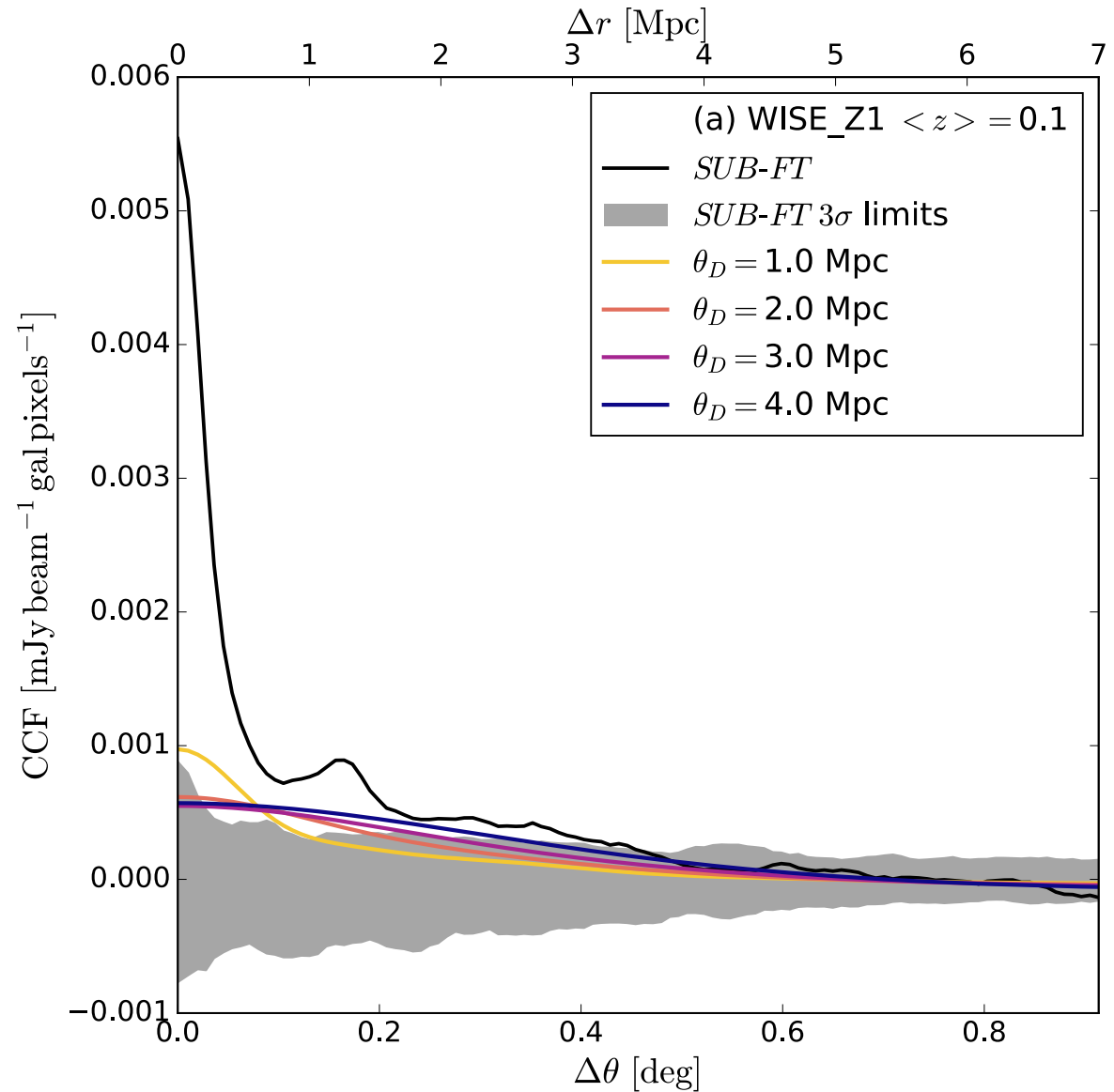
Cross correla



Scale CCF until  $> 3\sigma$

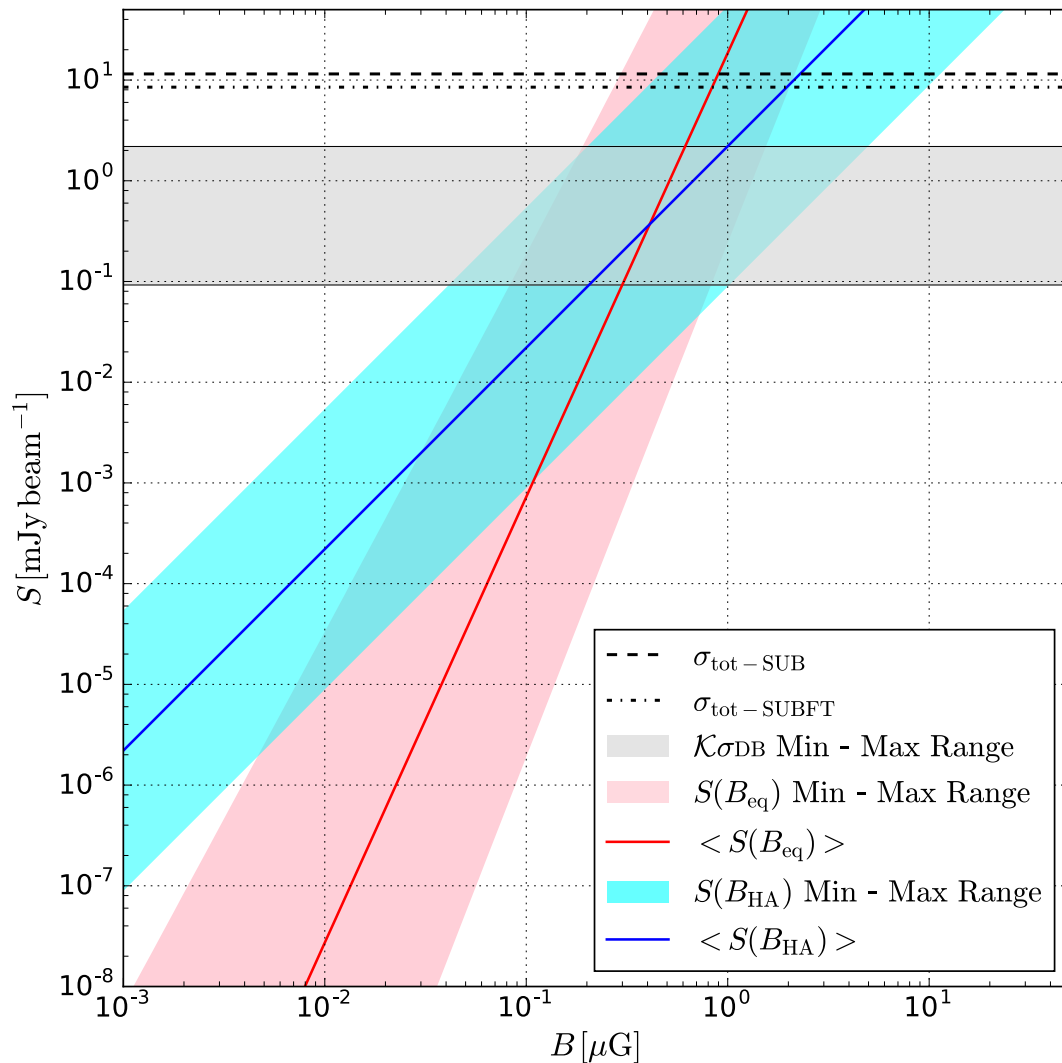
$$0.09 < S [\text{mJy beam}^{-1}] < 2.2$$

$$0.01 < S [\text{mJy arcmin}^{-2}] < 0.3$$



# Cross Correlation with MWA – Magnetic Field Limits

$$B_{\text{eq}} = \left[ \frac{4\pi(1-2\alpha)(K_0+1)E_p^{1+2\alpha}(\nu/2c_1)^{-\alpha}I_\nu(1+z)^{3-\alpha}}{(-2\alpha-1)c_2(\alpha)l\eta c_4(i)} \right]^{1/(3-\alpha)}$$



$1 < K_0 < 300$   $0.01 < \eta < 1$   $-0.6 < \alpha < -2.25$

- $0.03 < B_{\text{eq}} [\mu\text{G}] < 1.98$

$K_0=100$   $\eta=1.0$   $\alpha = -1.25$

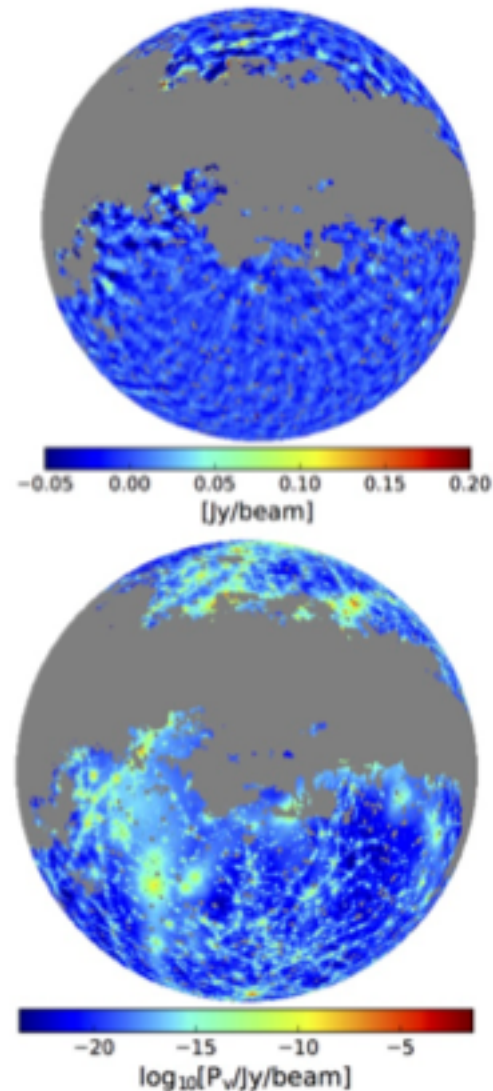
- $0.22 < B_{\text{eq}0} [\mu\text{G}] < 0.62$

$$B_{\text{HA}} \simeq 0.05 \mu\text{G} \sqrt{\frac{I_{\text{WHIM}}}{5 \times 10^{-3} \text{ Jy deg}^{-2} \left(\frac{100 \text{ MHz}}{\nu}\right)^\alpha \left(\frac{\xi}{10^{-3}}\right)}}$$

Vazza et al., 2015

# Cross Correlation S-PASS

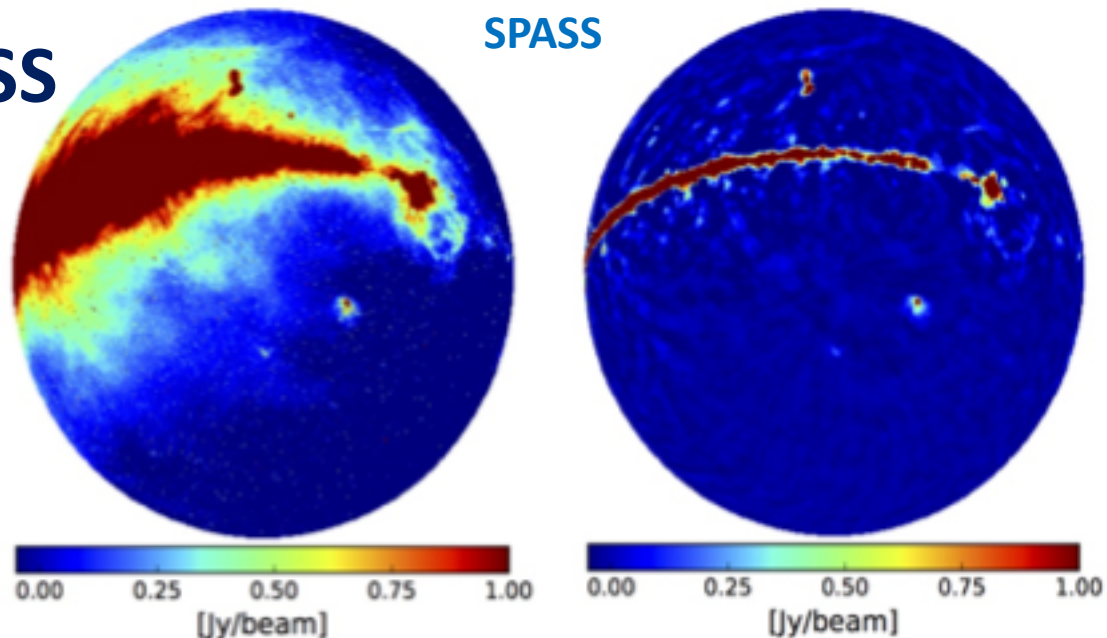
- Single Dish 2.3 GHz All Sky
- Cross correlate with MHD simulation (Dolag)
  - Brown et al., 2017



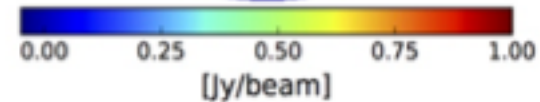
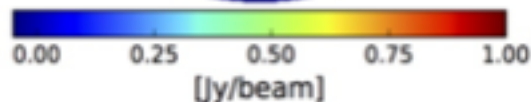
SPASS

Masked

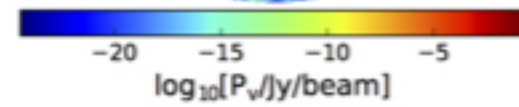
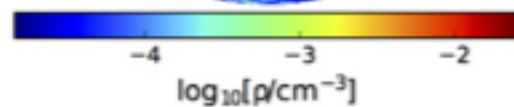
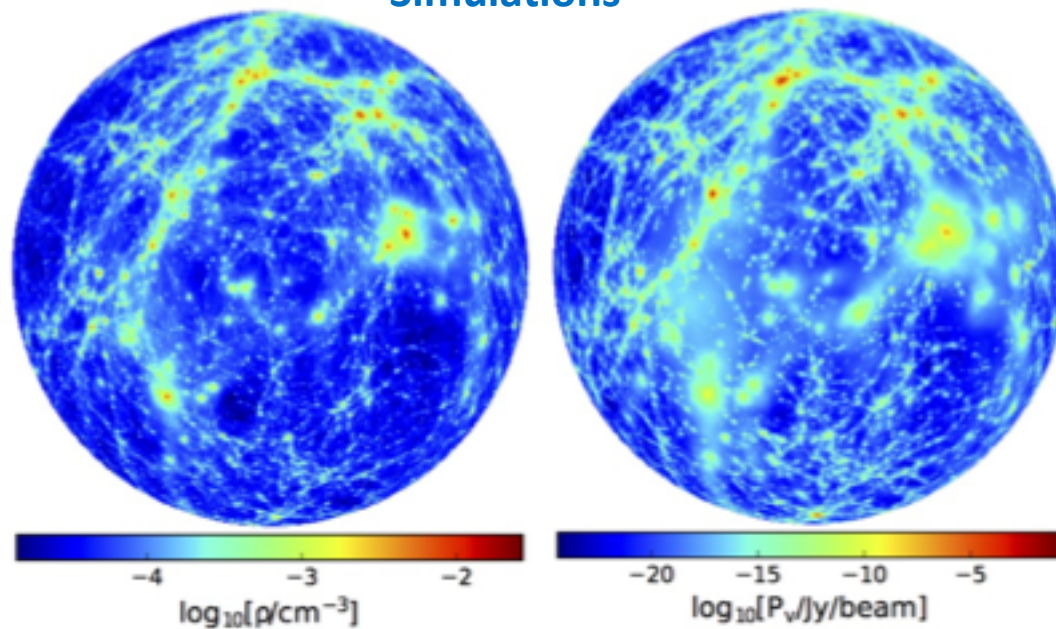
Sim



SPASS



Simulations



Electron density

Synchrotron

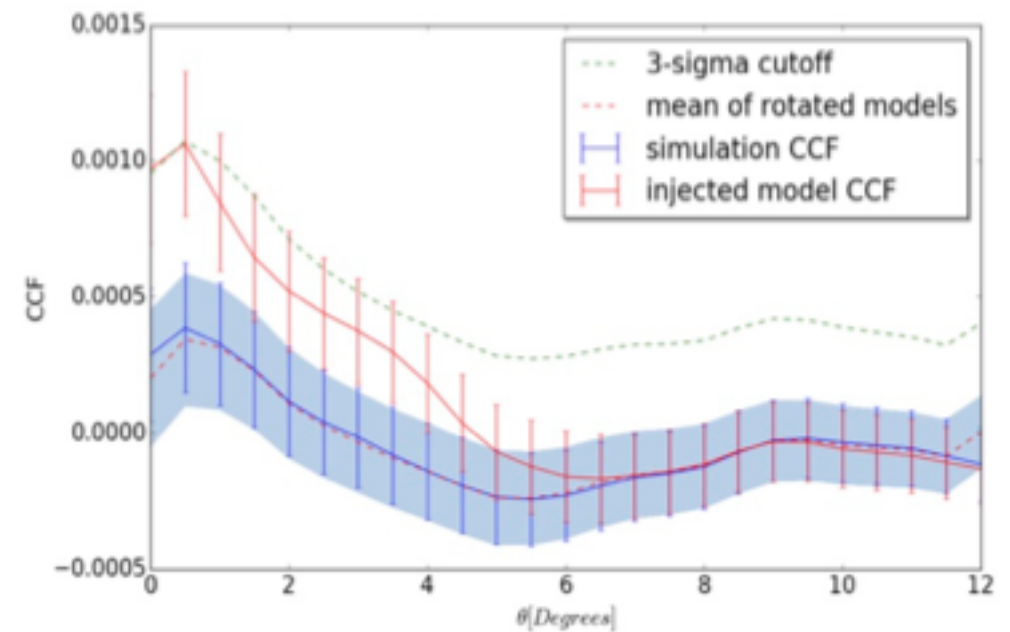
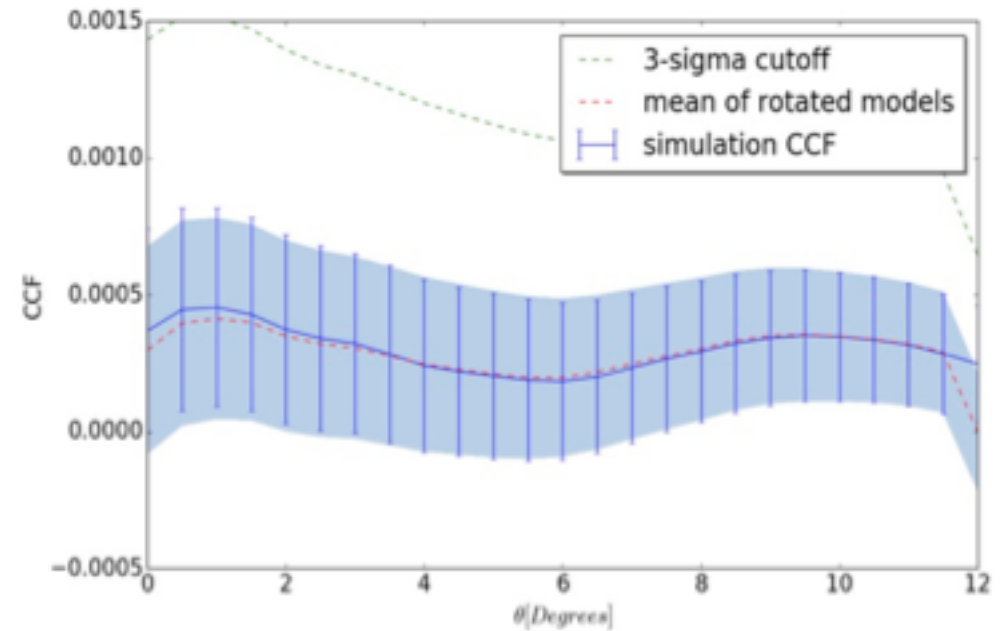


# Cross Correlation S-PASS

- Single Dish 2.3 GHz All Sky
- Cross correlate with MHD simulation (Dolag)
  - Brown et al., 2017

Flux upper limit:  
**0.16 mJy arcmin<sup>-2</sup>**

Magnetic field upper limit:  
**0.13  $\mu$ G**



# Cross Correlation

## Advantages:

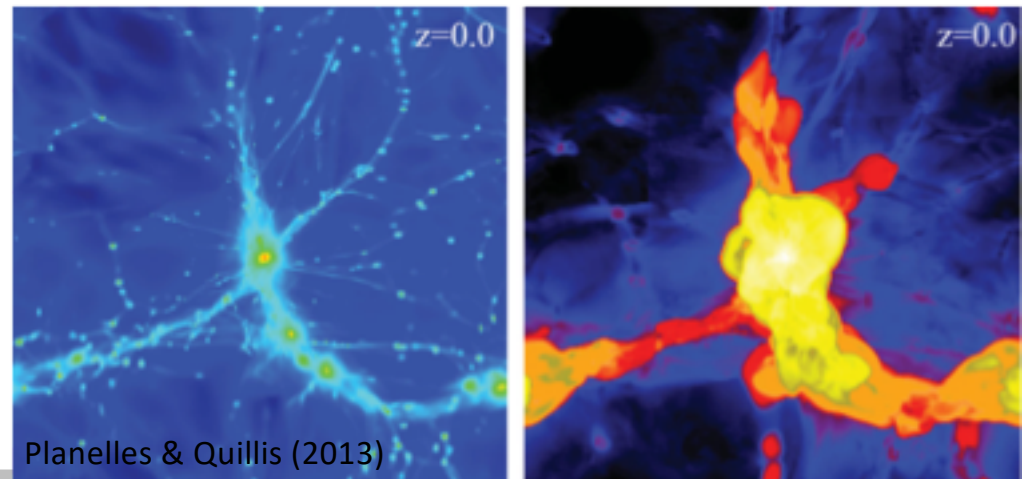
- Enhance signals hidden in the noise

## Caveats:

- Need models to interpret results physically
- Need to know (dirty) beam shape well
- Requires point source subtraction and/or model for point sources
- Galactic emission can interfere over large areas

## Future Work

- Repeat with different data
- New MHD simulations
- Model for point sources





# Other Methods

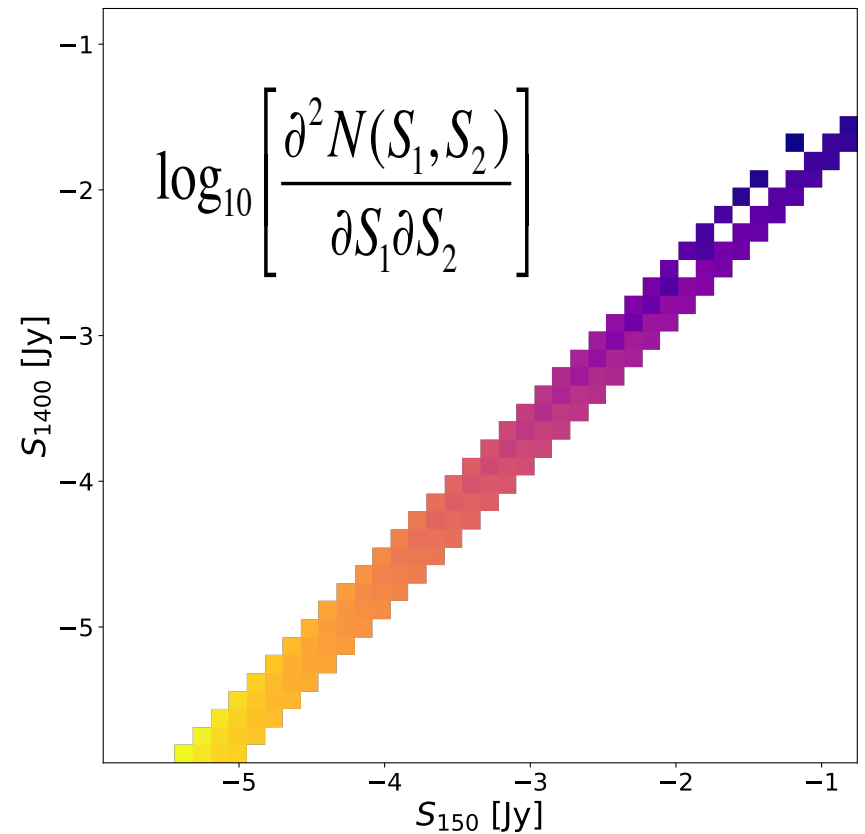
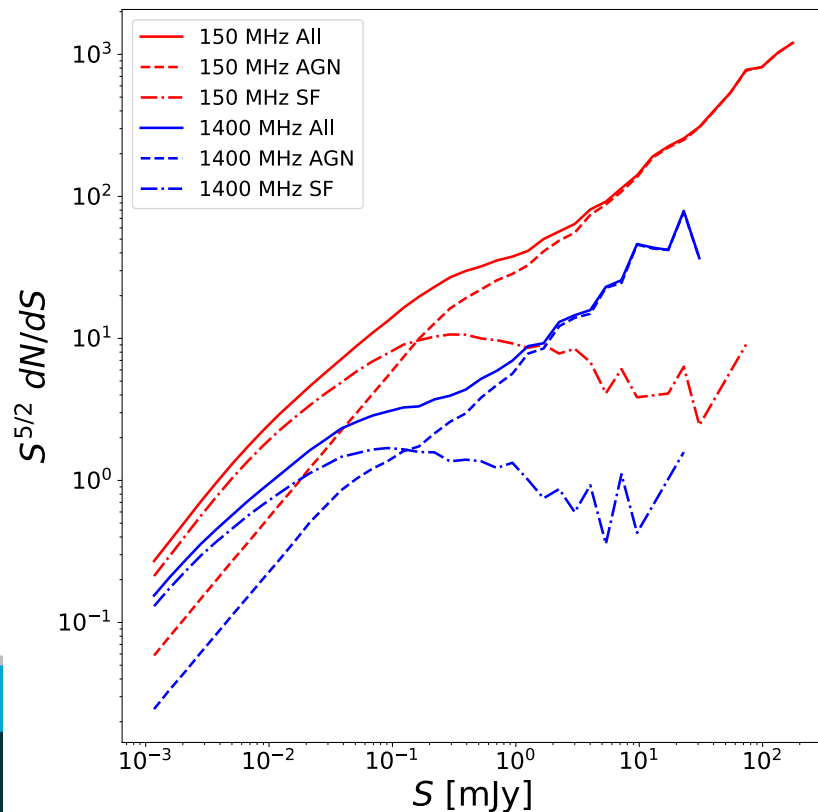
- 2D P(D) analysis
- Fit 2D source count to 2D histogram
- Can be two frequencies, two resolutions, Stokes I and polarised intensity
- Provides tighter constraints, uses more data, breaks degeneracies

Two populations:

- AGN  $\alpha = -0.85$
- Star-forming  $\alpha = -0.55$

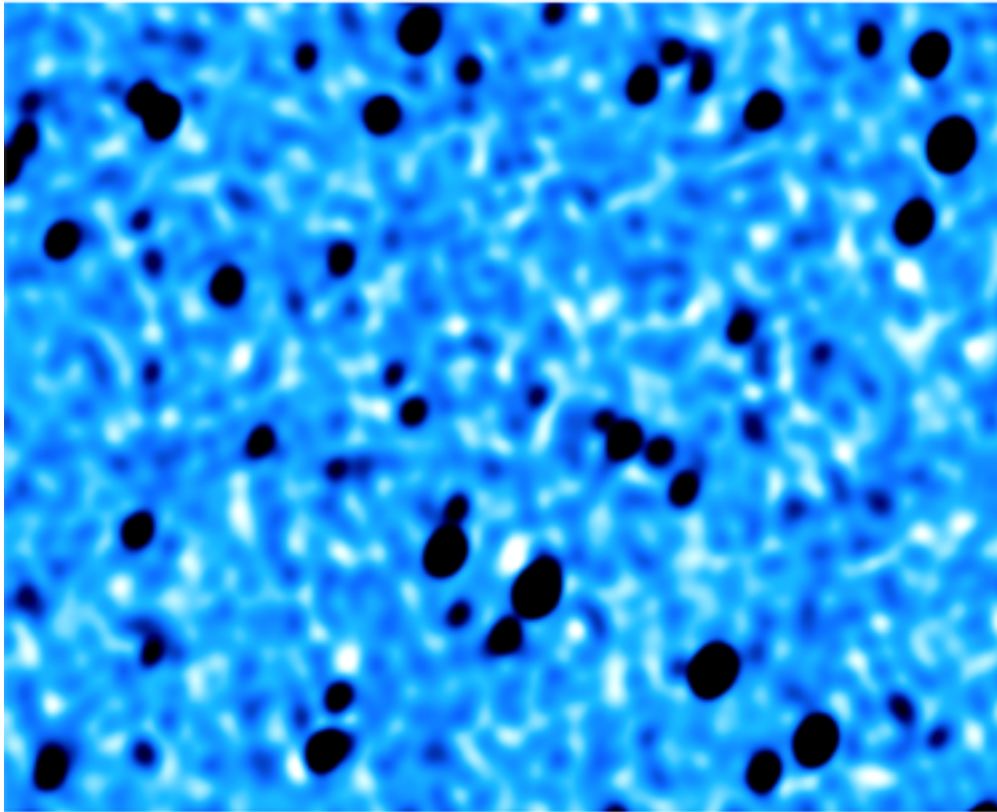
Two Frequencies:

- 150 MHz (MWA)
- 1400 MHz (ASKAP)

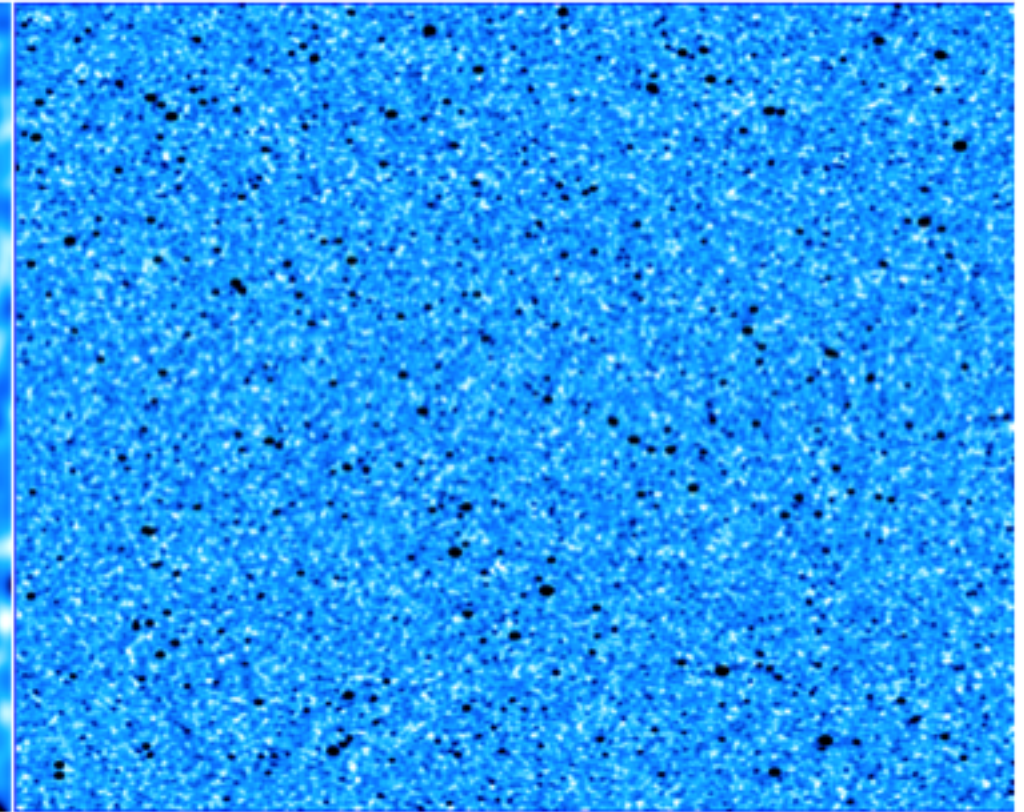


# Other Methods

- 2D P(D) analysis
- Fit 2D source count to 2D histogram
- Can be two frequencies, two resolutions, Stokes I and polarised intensity
- Provides tighter constraints, uses more data, breaks degeneracies



MWA PH 2 – 150 MHz – 55" beam –  
400 microJy instrumental noise



ASKAP – 1.4 GHz – 10" beam –  
10 microJy instrumental noise

# Other Methods

- 2D P(D) analysis

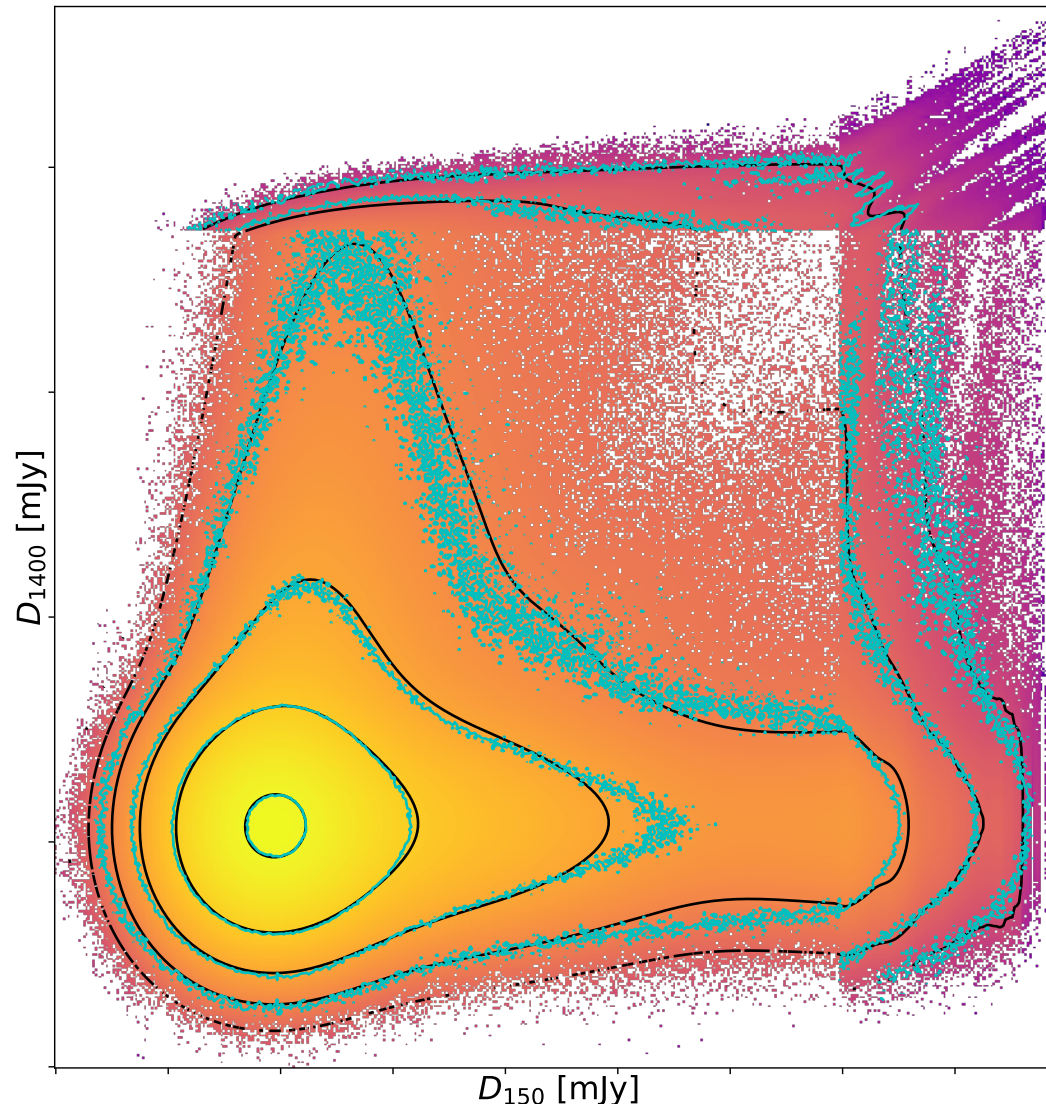
- Fit 2D source count to 2D histogram
- Can be two frequencies, two resolutions, Stokes I and polarised intensity
- Provides tighter constraints, uses more data, breaks degeneracies

Two populations:

- AGN  $\alpha = -0.85$
- Star-forming  $\alpha = -0.55$

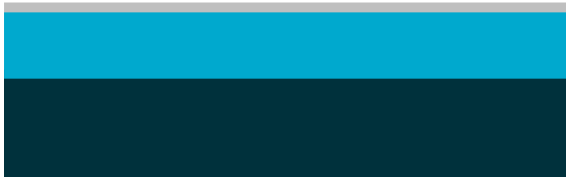
Two Frequencies:

- 150 MHz (MWA)
- 1400 MHz (ASKAP)



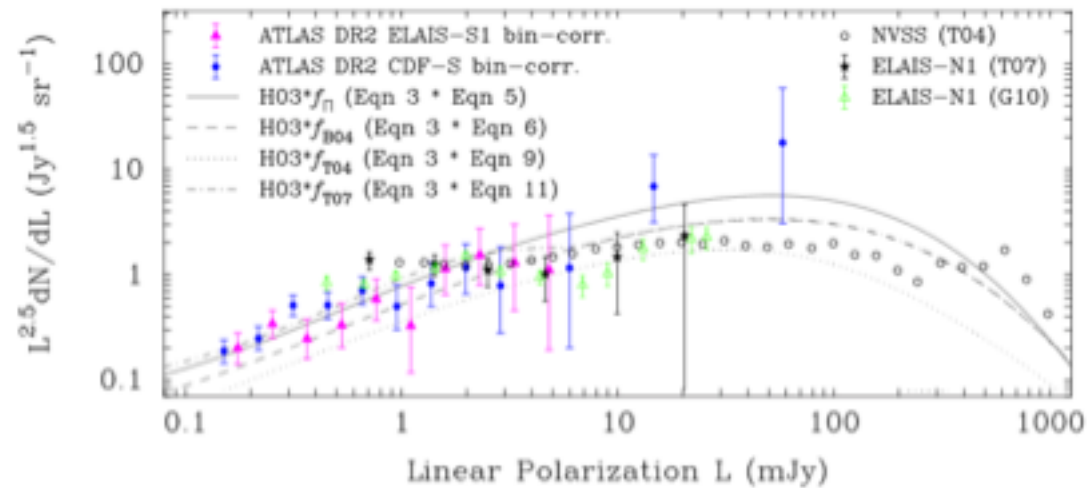
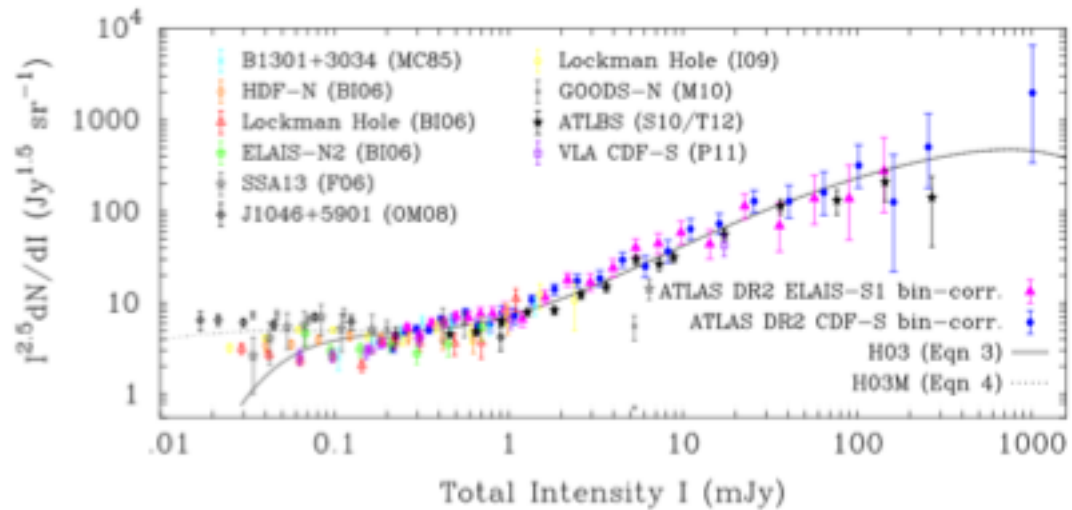
Cyan – Image  
P(D) Contours

Black Lines –  
Model P(D)  
Contours



# Other Methods

- 2D P(D) analysis
- Fit 2D source count to 2D histogram
- Can be two frequencies, two resolutions, Stokes I and polarised intensity
- Provides tighter constraints, uses more data, breaks degeneracies



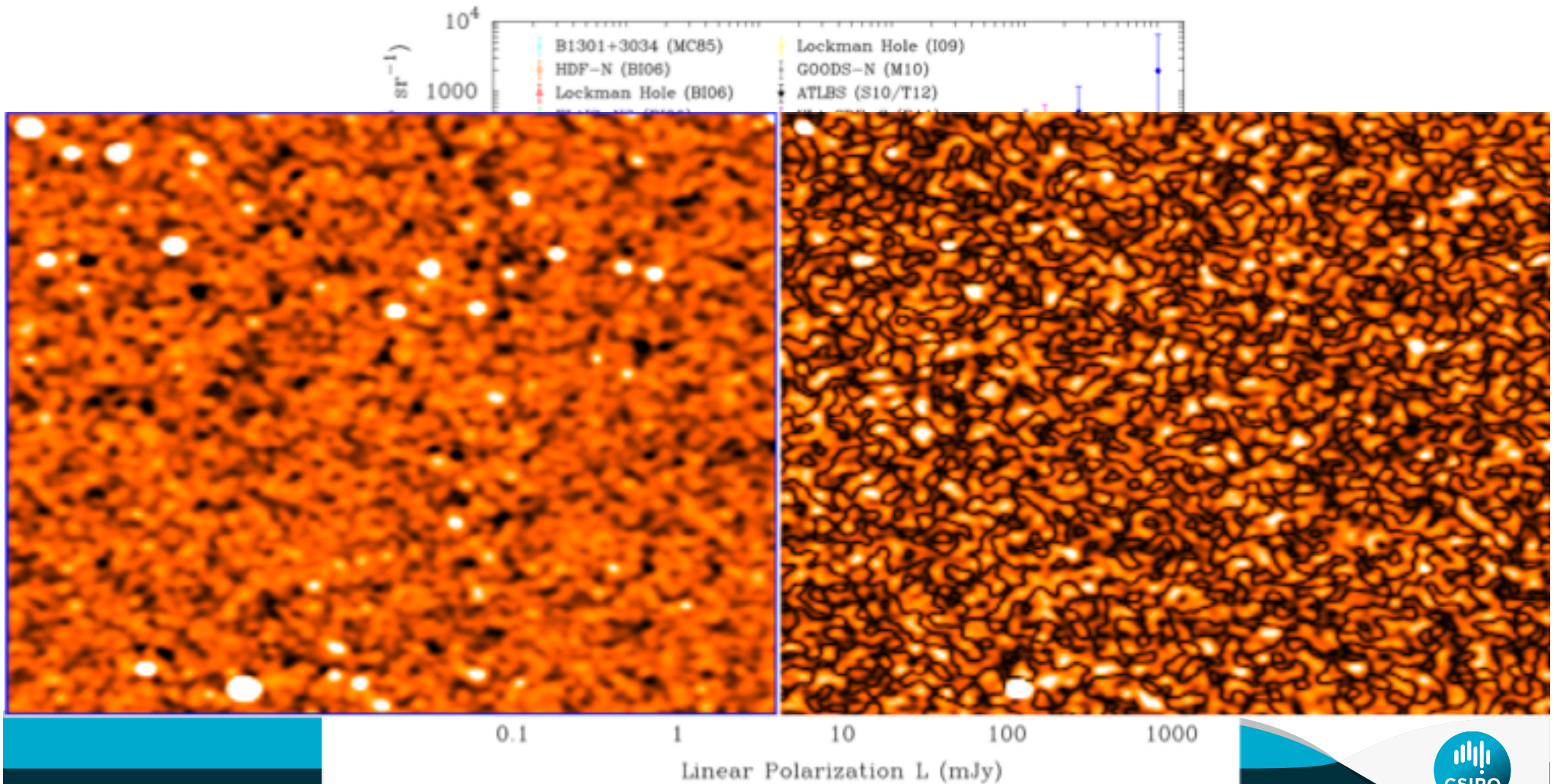
Not as deep or as constrained

Hales et al., 2014



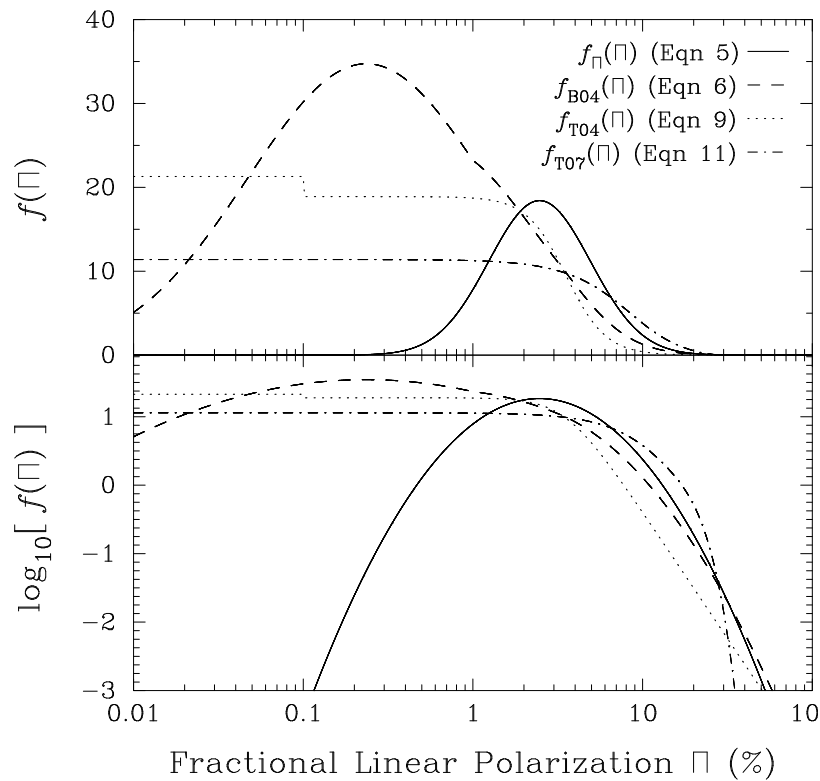
# Other Methods

- 2D P(D) analysis
- Fit 2D source count to 2D histogram
- Can be two frequencies, two resolutions, Stokes I and polarised intensity
- Provides tighter constraints, uses more data, breaks degeneracies

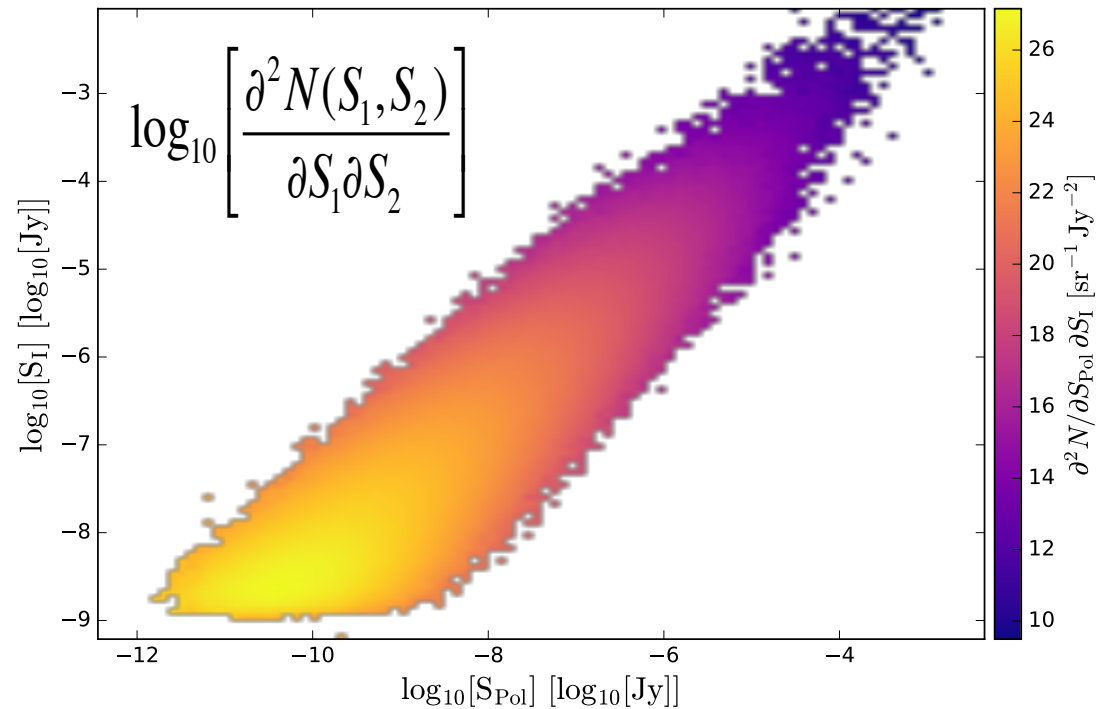


# Other Methods

- 2D P(D) analysis
- Fit 2D source count to 2D histogram
- Can be two frequencies, two resolutions, Stokes I and polarised intensity
- Provides tighter constraints, uses more data, breaks degeneracies



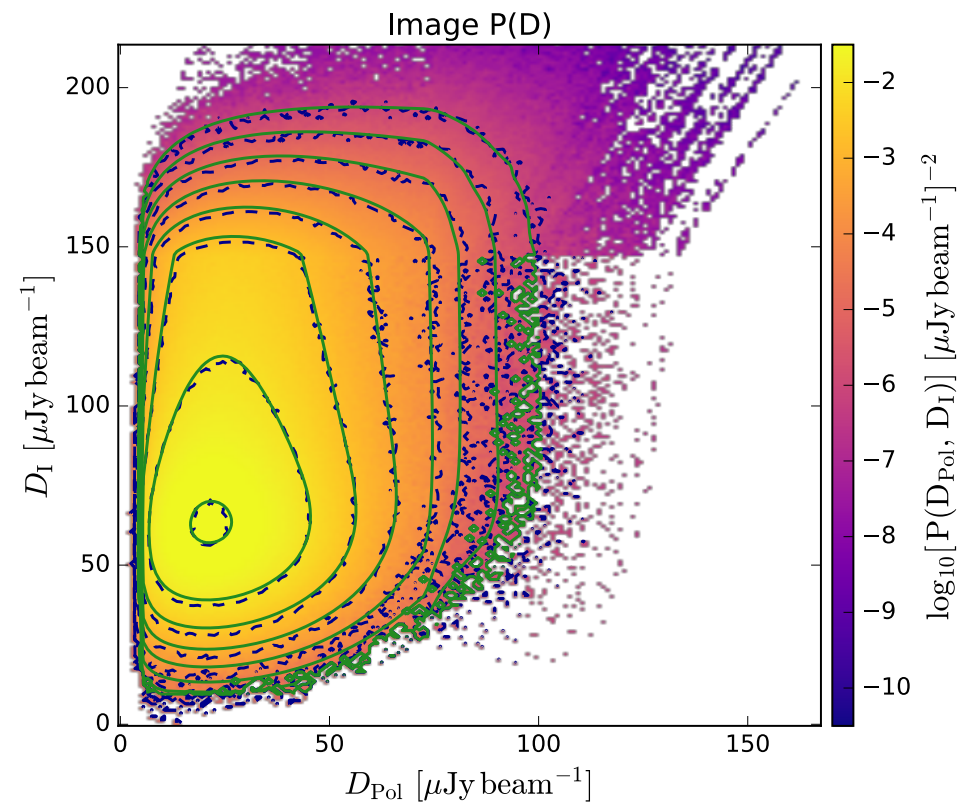
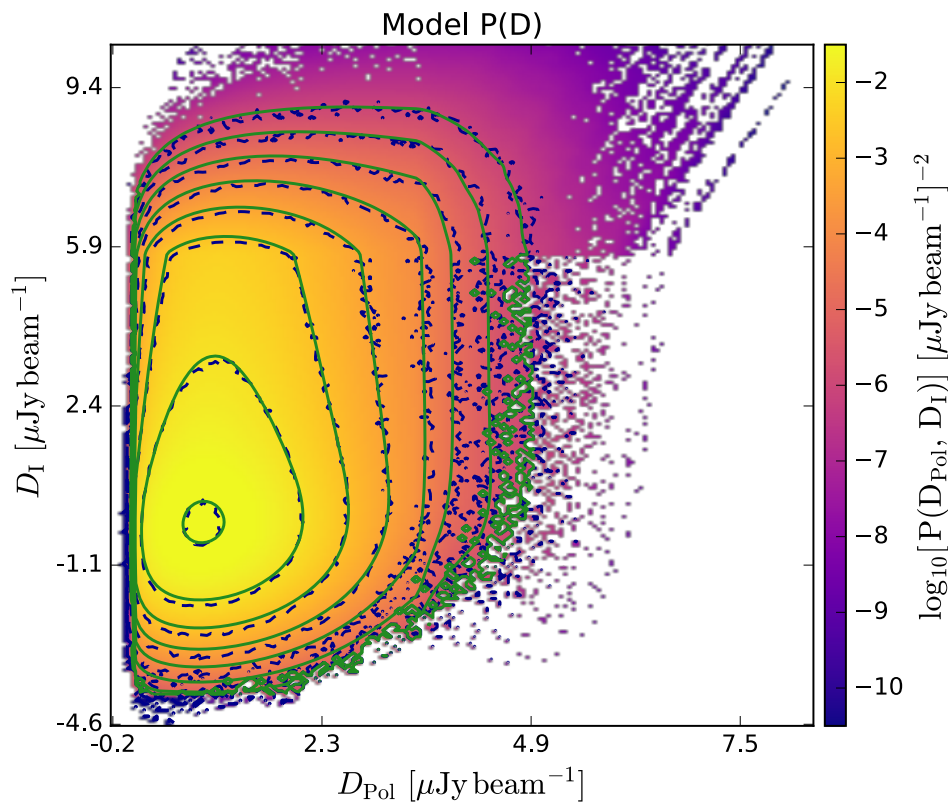
$$f_{\Pi}(\Pi) = \frac{1}{\Pi \sigma_{10} \ln(10) \sqrt{2\pi}} \exp \left\{ -\frac{[\log_{10}(\Pi/\Pi_0)]^2}{2\sigma_{10}^2} \right\}$$



# Other Methods

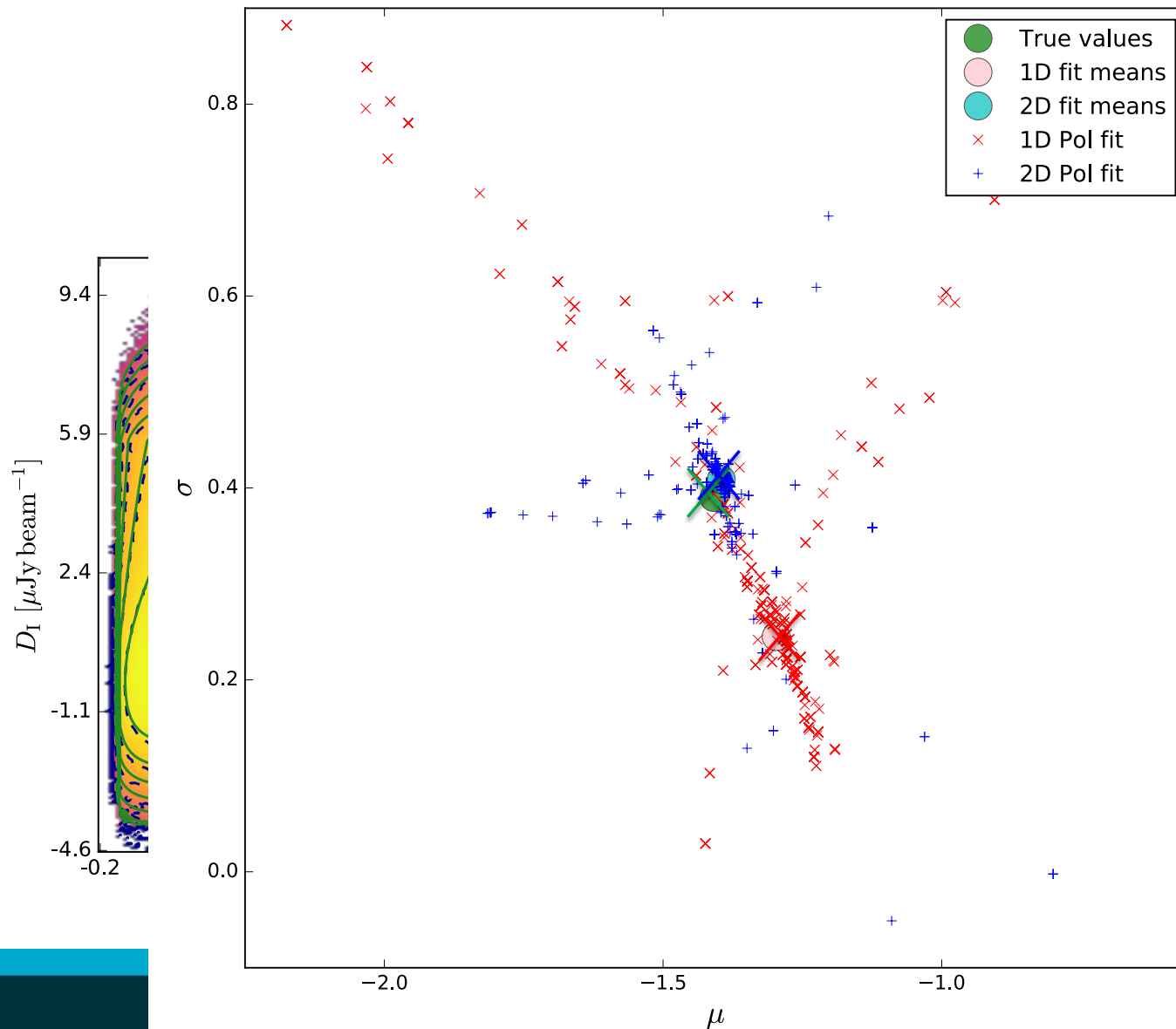
- 2D P(D) analysis
- Fit 2D source count to 2D histogram
- Can be two frequencies, two resolutions, Stokes I and polarised intensity
- Provides tighter constraints, uses more data, breaks degeneracies

$$f_{\Pi}(\Pi) = \frac{1}{\Pi \sigma_{10} \ln(10) \sqrt{2\pi}} \exp \left\{ -\frac{[\log_{10}(\Pi/\Pi_0)]^2}{2\sigma_{10}^2} \right\}$$



# Other Methods

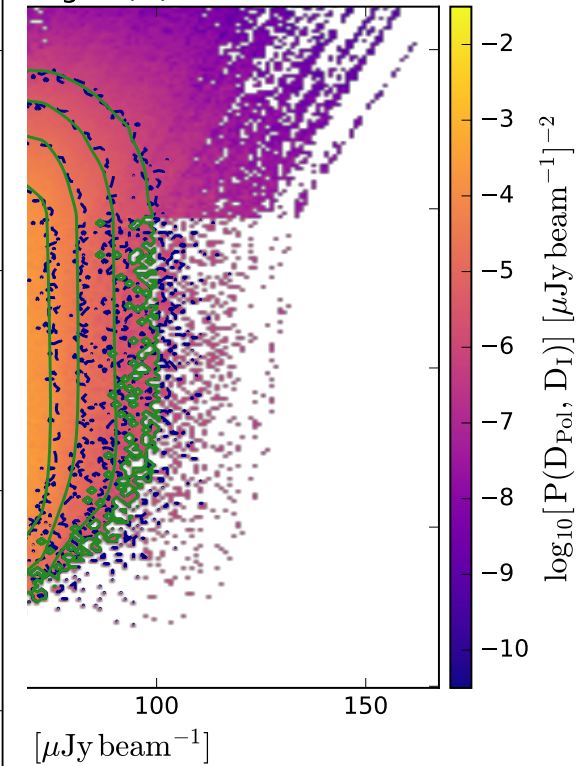
- 2D P(D) analysis
- Fit 2D source count to 2D histogram
- Can be two frequencies, two resolutions, Stokes I and polarised intensity



ata, breaks degeneracies

$$\exp \left\{ \frac{-[\log_{10}(\Pi/\Pi_0)]^2}{2\sigma_{10}^2} \right\}$$

image P(D)





# Other Methods

- 2D P(D) analysis
- Stacking (point sources and diffuse/filaments)
- Radio to X-ray correlation
- Cross power spectrum
- Wavelet covariance
- 2D Angular power spectrum
- Combinations, e.g. confusion analysis + cross correlation

# Summary & Conclusions

- **Confusion can be a hindrance or a tool**
  - **Can use it to get constraints on counts below confusion and instrumental noise limits**
  - **Excess diffuse emission can be detected via confusion analysis**
  - **Can be extended to multiple dimensions**
- **Cross correlation technique can enhance signals below the noise**
  - **Need more / better models to interpret results**
- **Need to understand noise and beams well**
- **Statistical techniques can be powerful tools for reaching below the noise**
- **Understanding current and developing new techniques crucial for fully utilizing new large surveys**

# Thank you

**Business Unit Name**

Presenter Name

Presenter Title

**t** +61 2 9123 4567

**e** [firstname.surname@csiro.au](mailto:firstname.surname@csiro.au)

**w** [www.csiro.au/lorem](http://www.csiro.au/lorem)

**Business Unit Name**

Presenter Name

Presenter Title

**t** +61 2 9123 4567

**e** [firstname.surname@csiro.au](mailto:firstname.surname@csiro.au)

**w** [www.csiro.au/lorem](http://www.csiro.au/lorem)

**ADD BUSINESS UNIT/FLAGSHIP NAME**

[www.csiro.au](http://www.csiro.au)

