

VILA DO CONDE,
PORTUGAL,
29-31 MARCH, 2016

11th Iberian Cosmology Meeting

IBERICOS 2016

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SERIES OF MEETINGS WHICH AIM
TO ENCOURAGE INTERACTIONS
AND COLLABORATIONS BETWEEN
RESEARCHERS WORKING IN
COSMOLOGY AND RELATED
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Scalar field dark matter and the Higgs field

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PhD student under the supervision of
Prof. João Rosa and Prof. Orfeu Bertolami

arXiv: 1603.06242

30 March 2016



Introducing the problem

- **Dark matter (DM) - 26.8 %** of the mass-energy content of the Universe [Planck Collaboration 2015];

What is dark matter made of?

- We propose: oscillating scalar field as DM candidate, coupled to the Higgs boson;
- Previous works: “Higgs-portal” DM models: abundance of DM is set by the decoupling and freeze-out from thermal equilibrium $\Rightarrow m \sim GeV - TeV$ (Weakly Interacting Massive Particles - WIMPs) [Silveira, Zee 1985; Bento, Bertolami, Rosenfeld 2001; Burgess, Pospelov, ter Veldhuis 2001; Tenkanen 2015];

Oscillating scalar field as dark matter candidate

Our proposal

- Oscillating scalar field, ϕ , as DM candidate;
- ϕ acquires mass through the Higgs mechanism;
- ϕ starts to oscillate when $m_\phi \sim H$, after the electroweak phase transition;
- Weakly interactions with the Higgs boson $\Rightarrow m_\phi \ll eV$, extremely small self-interactions $\Rightarrow$ oscillating scalar condensate that is never in thermal equilibrium.

Oscillating scalar field as dark matter candidate

Energy density

$$\rho_{\phi,0} = \frac{1}{2} \frac{m_{\phi}^2}{a_0^3} \phi_i^2$$

$$H_{EW} \sim 10^{-5} \text{ eV}$$

DM abundance

$$\Omega_{\phi,0} \equiv \frac{\rho_{\phi,0}}{\rho_{c,0}}$$

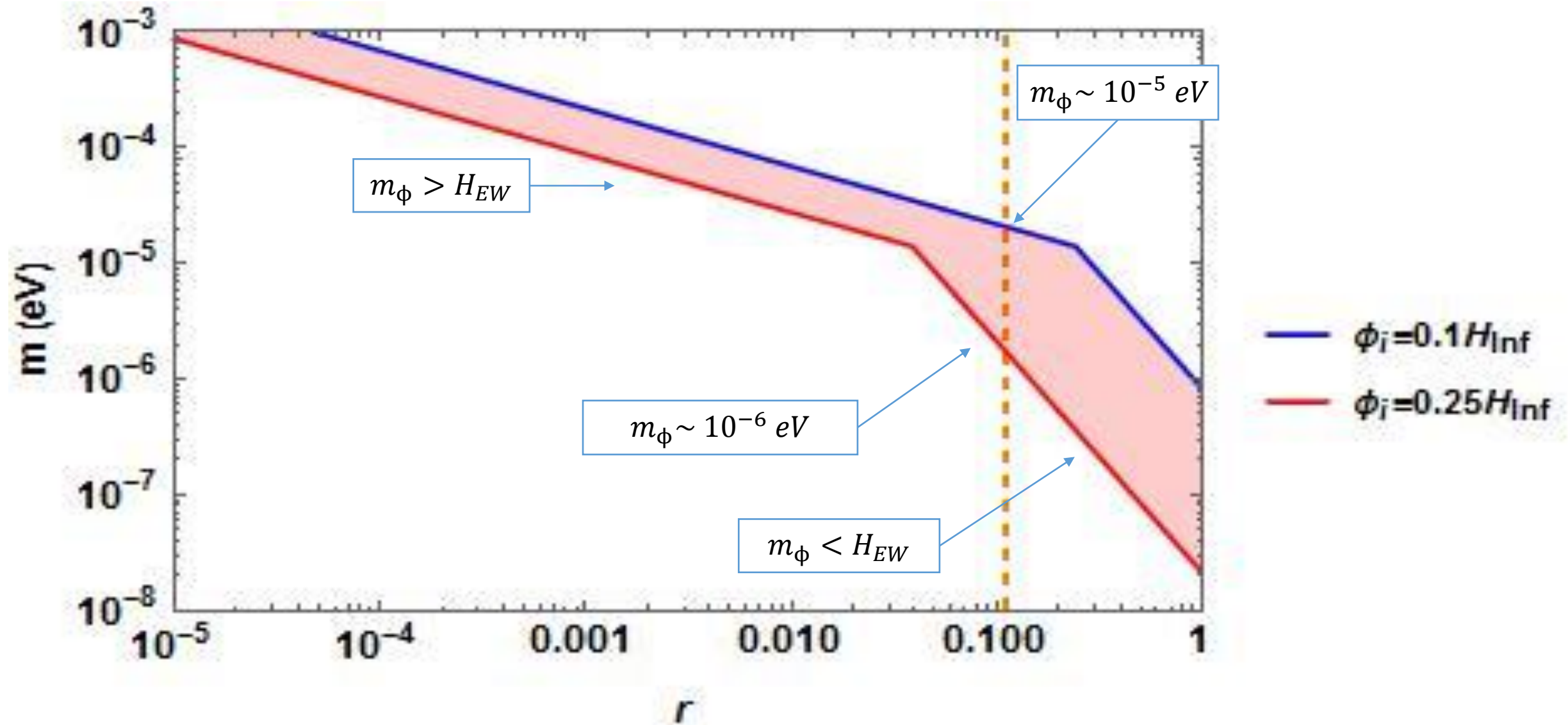
$$m_{\phi}(\phi_i) = \begin{cases} 2 \times 10^{-5} \left(\frac{g_*}{100} \right)^{1/2} \left(\frac{\phi_i}{10^{13} \text{ GeV}} \right)^{-4} \text{ eV}, & m_{\phi} > H_{EW}. \\ 3 \times 10^{-5} \left(\frac{g_*}{100} \right)^{1/2} \left(\frac{\phi_i}{10^{13} \text{ GeV}} \right)^{-4} \text{ eV}, & m_{\phi} < H_{EW}. \end{cases}$$

Initial conditions

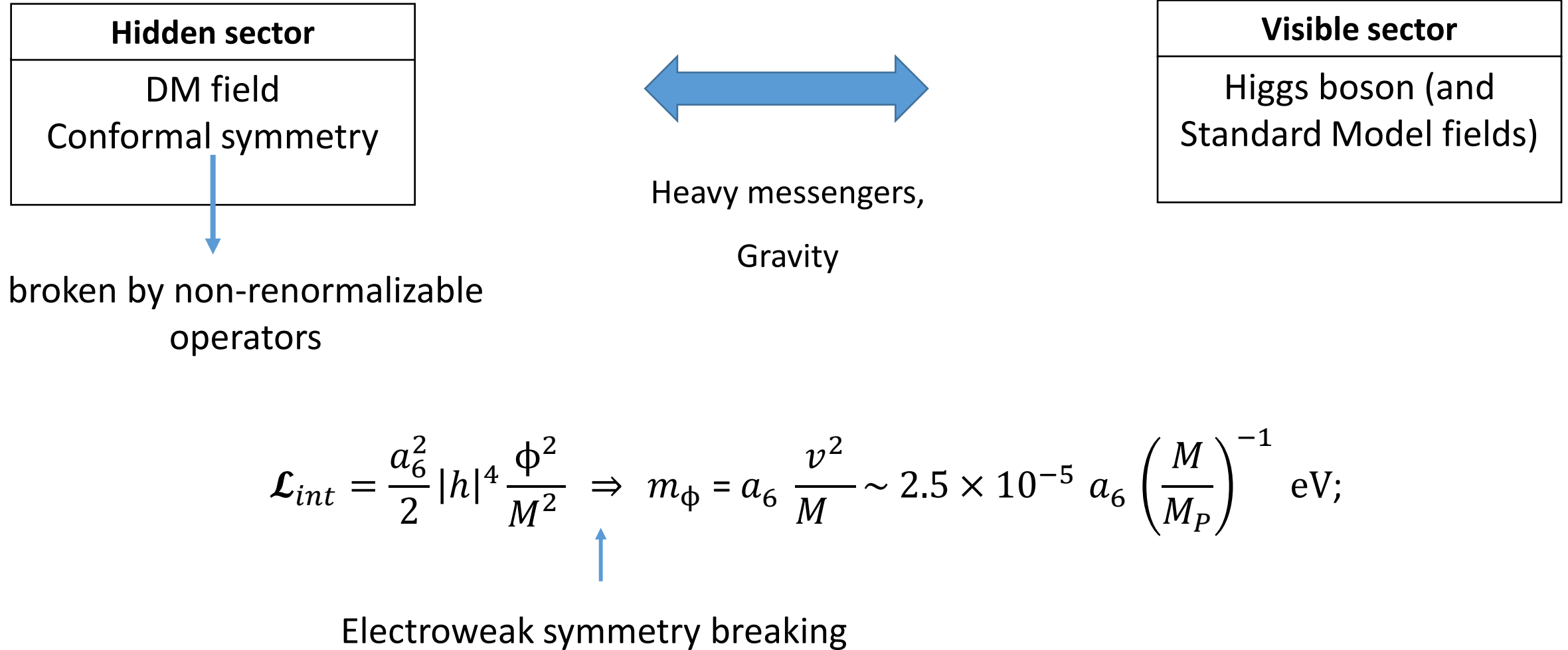
- Light fields during inflation $\Rightarrow$ quantum fluctuations do not respect the limit of the Cold Dark Matter (CDM) isocurvature perturbations.
- Gravitational interactions during inflation $\Rightarrow \mathcal{L}_{int} = \frac{c}{2} \frac{\phi^2 V(\chi)}{M_{Pl}^2} \Rightarrow m_\phi \sim H_{inf} \Rightarrow$ CDM isocurvature perturbations compatible with observations [Planck Collaboration 2015];
- Constraints on CDM isocurvature perturbations lead to: $\phi_i \simeq \alpha H_{inf}, \quad \alpha \simeq 0.1 - 0.25;$
- $H_{inf} \simeq 2.5 \times 10^{13} \left(\frac{r}{0.01} \right)^{\frac{1}{2}} GeV, \quad r < 0.11.$ [Planck Collaboration 2015].

$$r \equiv \frac{\Delta_t^2}{\Delta_{\mathcal{R}}^2}$$

Initial conditions – Results



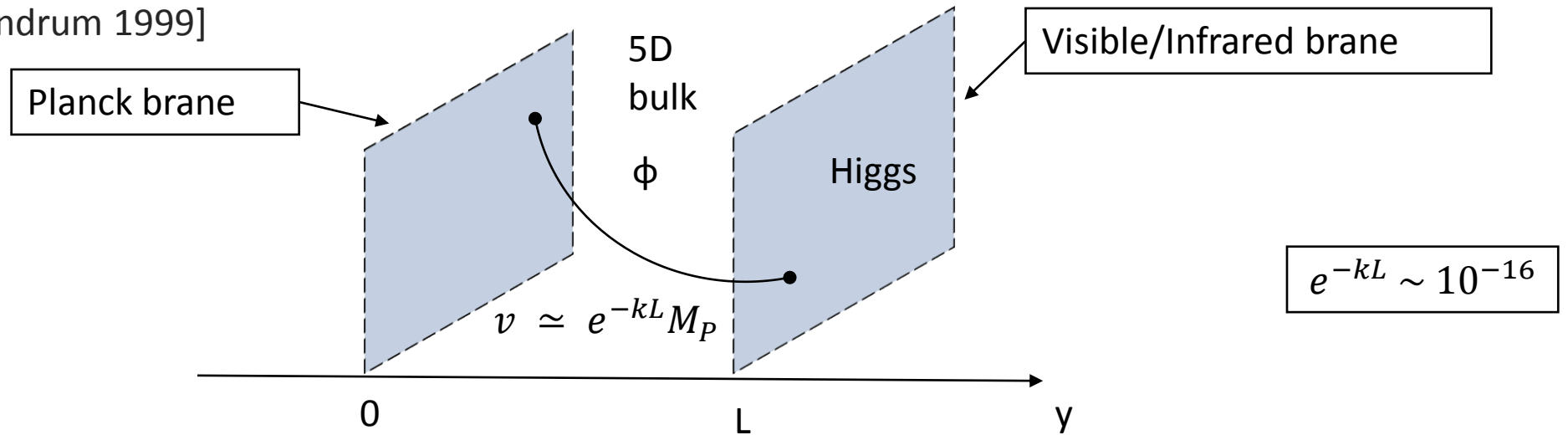
Non-renormalizable interactions model



Warped extra-dimension model

Randall-Sundrum inspired model:

[L. Randall, R. Sundrum 1999]



Metric: $ds^2 = e^{-2k|y|} g_{\mu\nu} dx^\mu dx^\nu + dy^2$

$$S = \int d^4x \int dy \sqrt{-G} \left[\frac{1}{2} G^{MN} \partial_M \Phi \partial_N \Phi - \frac{1}{2} M_\Phi^2 \Phi^2 + \delta(y-L) \left(G^{MN} \partial_M h^\dagger \partial_N h - V(h) + \frac{1}{2} g_5^2 \Phi^2 h^2 \right) \right]$$

Warped extra-dimension model

- Decompose Φ in Kaluza-Klein modes: $\Phi(x^\mu, y) = \frac{1}{\sqrt{2L}} \sum_{n=0}^{\infty} \phi_n(x^\mu) f_n(y)$;

- $\Phi_0(x^\mu, L) = \frac{1}{\sqrt{2L}} \phi_0(x^\mu) \sqrt{2kL}$

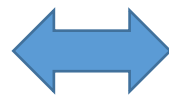
 $\mathcal{L}_{int} = \frac{1}{2} g_5^2 k e^{-2kL} \phi_0^2 h^2$


 $g_4 \sim g_5^2 k e^{-2kL} \simeq \mathcal{O}(1) \times \frac{v}{M_P} \sim 10^{-16}$

$$m_\phi \sim \frac{v^2}{M_P} \sim 10^{-5} \text{ eV}$$

Mass in the required range;
In agreement with non-renormalizable interactions model.

Planck-suppressed non-renormalizable operator



Renormalizable interaction in a higher-dimensional warped geometry.

Conclusions

- DM candidate: oscillating scalar field ϕ , which acquires mass through the Higgs mechanism.
- Lower bound: $m_\phi \gtrsim 10^{-6} - 10^{-5} \text{ eV} ;$
- $m_\phi \sim \frac{v^2}{M_P} \sim 10^{-5} \text{ eV}$ obtained through either non-renormalizable interactions between ϕ and the Higgs field or through a warped extra-dimension model.

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Scalar field inflation in the presence of a non-minimal matter-curvature coupling

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IberiCos 2016, Vila do Conde, 30 March 2016

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Fundação para a Ciência e a Tecnologia, SFRH/BD/102820/2014

Contents

1. Inflation

2. Alternative theories of gravity

The non-minimal coupling between matter and curvature (NMC)

3. Scalar field inflation with a matter-curvature NMC



Why Inflation?

Hot Big Bang model:

- Evolutionary Universe;
- CMB;
- BBN...

Leaves some conundrums:

- Large scale homogeneity and isotropy (horizon problem);
- Flatness problem;
- Absence of observed topological defects (monopole problem);
- Origin of the energy density fluctuations,...

Cosmic Inflation (paradigm, not theory) provides a suitable solution for the above problems by a mechanism of accelerated expansion of the Universe at early times (between Planck and GUT epochs).

Scalar field inflation

Real scalar field with:

$$\ddot{\phi} + 3H\dot{\phi} + V'(\phi) = 0 \quad (1)$$

Inflation occurs in the so-called slow-roll approximation:

○

$$V \gg \dot{\phi}^2/2 \implies \rho \approx V(\phi) \quad (2)$$

○

$$V \approx \text{const.} \quad (3)$$

This is the same as stating that the slow-roll parameters are:

$$\epsilon_{\phi} = \frac{M_P^2}{2} \left(\frac{V'}{V} \right)^2 \ll 1 \quad (4)$$

$$\eta_{\phi} = M_P^2 \frac{V''}{V} \ll 1 \quad (5)$$

Why to go beyond GR?

Successes:

- Solar System constraints;
- GPS;

But there were still some conundrums:

- Not compatible with quantum mechanics;
- Existence of singularities;
- Cosmological constant problem;
- Large scale data requires DM and DE;
- Astrophysical data requires DM.

Alternative theories of gravity:

- $f(R)$
- Horndeski gravity;
- Jordan-Brans-Dicke;
- NMC [Bertolami, Böhmer, Harko, Lobo 2007]...

Alternative theories of gravity: the NMC

Generalisation of $f(R)$ theories

[Bertolami, Bohmer, Harko, Lobo, 2007]:

$$S = \int [\kappa f_1(R) + f_2(R) \mathcal{L}] \sqrt{-g} d^4x \quad , \quad (6)$$

where $\kappa = M_P^2/2 = 1/16\pi G$.

Varying the action relatively to the metric $g_{\mu\nu}$:

$$\begin{aligned} 2(\kappa F_1 - F_2\rho) \left(R_{\mu\nu} - \frac{1}{2}g_{\mu\nu}R \right) = & f_2 T_{\mu\nu} + \kappa(f_1 - F_1 R) g_{\mu\nu} + \\ & + F_2 \rho R g_{\mu\nu} + 2\Delta_{\mu\nu}(\kappa F_1 - F_2\rho) \end{aligned} \quad (7)$$

One recovers GR by setting $f_1(R) = R$ and $f_2(R) = 1$.

Using the Bianchi identities, one finds the non-covariant conservation of the energy-momentum tensor:

$$\nabla_{\mu} T^{\mu\nu} = \frac{F_2}{f_2} (g^{\mu\nu} \mathcal{L} - T^{\mu\nu}) \nabla_{\mu} R \quad (8)$$

For a perfect fluid, the extra force due to the NMC can be expressed as:

$$f^{\mu} = \frac{1}{\rho + p} \left[\frac{F_2}{1 + f_2} (\mathcal{L}_m - p) \nabla_{\nu} R + \nabla_{\nu} p \right] h^{\mu\nu}, \quad (9)$$

with $h^{\mu\nu} = g^{\mu\nu} + u^{\mu} u^{\nu}$ being the projection operator.

Degeneracy-lifting of the Lagrangian choice [O. Bertolami, F. S. N. Lobo, J. Páramos, 2008]

Mimicking Dark Matter (galaxies, clusters) [O. Bertolami, J. Páramos, 2010; O. Bertolami, P. Frazão, J. Páramos, 2013]

Cosmological Perturbations [O. Bertolami, P. Frazão, J. Páramos, 2013]

Preheating scenario after inflation [O. Bertolami, P. Frazão, J. Páramos, 2011]

Modified Friedmann equation [O. Bertolami, J. Páramos, 2013]

Modified Layzer-Irvine equation and virial theorem [O. Bertolami, C. Gomes, 2014]

...

Scalar field inflation in the presence of a non-minimal matter-curvature curvature

At first approximation:

$$\ddot{\phi} + 3H\dot{\phi} + V'(\phi) \approx 0 \quad (10)$$

In the slow-roll regime, and for $f_1(R) = R$, we have a modified Friedmann equation:

$$H^2 \approx \frac{f_2}{1 + \frac{2F_2\rho}{M_P^2}} \frac{\rho}{3M_P^2} \quad (11)$$

Choosing the non-minimal coupling function to be:

$$f_2(R) = 1 + \left(\frac{R}{R_n} \right)^n \quad (12)$$

we find that for the large density limit:

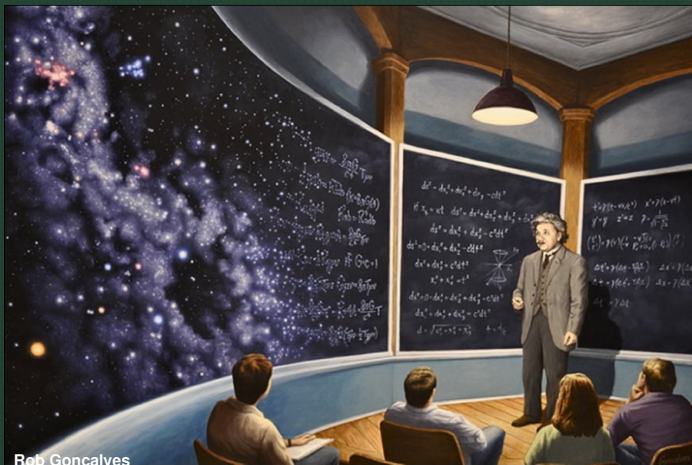
- $n = 2$ we retrieve the Friedmann equation as in GR
- $n \geq 3$ the modified Friedmann equation becomes ($A_n, B_n \in \mathbb{R}$)

$$H^2 = A_n - \frac{B_n}{\rho} \quad (13)$$

whilst in the low density regime, this model gives a small correction to the Friedmann's equation.

We further note that modifications of the Friedmann equation have been well studied in the literature: brane models, loop quantum cosmology, ...

Thank you for your attention!



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Disformal couplings

Let us consider the action

$$\mathcal{S} = \mathcal{S}_{\text{grav}}(g_{\mu\nu}, \phi) + \mathcal{S}_{\text{matter}}(\tilde{g}_{\mu\nu}^{(m)}) + \mathcal{S}_{\text{EM}}(A_\mu, \tilde{g}_{\mu\nu}^{(r)})$$

The metrics $\tilde{g}_{\mu\nu}^{(m)}$ and $\tilde{g}_{\mu\nu}^{(r)}$ are related to $g_{\mu\nu}$ via a disformal transformation:

$$\tilde{g}_{\mu\nu}^{(m)} = C_m(\phi)g_{\mu\nu} + D_m(\phi)\phi_{,\mu}\phi_{,\nu}$$

$$\tilde{g}_{\mu\nu}^{(r)} = C_r(\phi)g_{\mu\nu} + D_r(\phi)\phi_{,\mu}\phi_{,\nu} .$$

C_r and C_m are conformal factors

D_r and D_m are disformal factors

We can also write,

$$\tilde{g}_{\mu\nu}^{(r)} = \frac{C_r}{C_m} \tilde{g}_{\mu\nu}^{(m)} + \left(D_r - \frac{C_r D_m}{C_m} \right) \phi_{,\mu}\phi_{,\nu} \equiv A \tilde{g}_{\mu\nu}^{(m)} + B \phi_{,\mu}\phi_{,\nu}$$

Electromagnetic sector

The action

$$\mathcal{S}_{\text{EM}} = -\frac{1}{4} \int d^4x \sqrt{-\tilde{g}^{(r)}} h(\phi) \tilde{g}^{\mu\nu}_{(r)} \tilde{g}^{\alpha\beta}_{(r)} F_{\mu\alpha} F_{\nu\beta} - \int d^4x \sqrt{-\tilde{g}^{(m)}} \tilde{g}^{\mu\nu}_{(m)} j_\mu A_\nu$$

- $F_{\mu\nu}$ is Faraday tensor; j^μ is the four-current;
- $h(\phi)$ is the coupling between the electromagnetism and ϕ .

In the frame in which matter is decoupled from the scalar field

$$\begin{aligned} \mathcal{S}_{\text{EM}} = & -\frac{1}{4} \int d^4x \sqrt{-\tilde{g}^{(m)}} h Z \left[\tilde{g}^{\mu\nu}_{(m)} \tilde{g}^{\alpha\beta}_{(m)} - 2\gamma^2 \tilde{g}^{\mu\nu}_{(m)} \phi^{,\alpha} \phi^{,\beta} \right] F_{\mu\alpha} F_{\nu\beta} \\ & - \int d^4x \sqrt{-\tilde{g}^{(m)}} \tilde{g}^{\mu\nu}_{(m)} j_\mu A_\nu \end{aligned}$$

where

$$Z = \left(1 + \frac{B}{A} \tilde{g}^{\mu\nu}_{(m)} \partial_\mu \phi \partial_\nu \phi \right)^{1/2}, \quad \gamma^2 = \frac{B}{A + B \tilde{g}^{\mu\nu}_{(m)} \partial_\mu \phi \partial_\nu \phi}$$

The field equation for A_μ

Varying the action with respect to A_μ

$$\tilde{\nabla}_\epsilon (hZF^{\epsilon\rho}) - \tilde{\nabla}_\epsilon \left(hZ\gamma^2\phi^{,\beta} \left(\tilde{g}_{(m)}^{\epsilon\nu}\phi^{,\rho} - \tilde{g}_{(m)}^{\rho\nu}\phi^{,\epsilon} \right) F_{\nu\beta} \right) = j^\rho$$

With $\tilde{g}_{\mu\nu}^{(m)} = \eta_{\mu\nu}$, and $E^i = F^{i0}$

$$\nabla \cdot \mathbf{E} = \frac{Z\rho}{h}$$

where $\rho = j^0$. Integrating this equation over a volume $\mathcal{V}$ using, $\mathbf{E} = -\nabla V$, we get the electrostatic potential

$$V(r) = \frac{ZQ}{4\pi hr} \quad \Rightarrow \quad \boxed{\alpha \propto \frac{Z}{h}}$$

The fine structure constant depends on Z .

The evolution of α

For FLRW Universe,

$$Z = \left(\frac{1 - \frac{D_r}{C_r} \dot{\phi}^2}{1 - \frac{D_m}{C_m} \dot{\phi}^2} \right)^{1/2}$$

Time derivative of α ,

$$\frac{\dot{\alpha}}{\alpha} = \frac{1}{Z} \left(\frac{\partial Z}{\partial \phi} \dot{\phi} + \frac{\partial Z}{\partial \dot{\phi}} \ddot{\phi} \right) - \frac{1}{h} \frac{dh}{d\phi} \dot{\phi}$$

Redshift evolution of α ,

$$\frac{\Delta\alpha}{\alpha}(z) \equiv \frac{\alpha(z) - \alpha_0}{\alpha_0} = \frac{h_0 Z}{h Z_0} - 1$$

Constrains on the evolution of α

- ① Atomic Clocks at $z = 0$,

$$\left. \frac{\dot{\alpha}}{\alpha} \right|_0 = (-1.6 \pm 2.3) \times 10^{-17} \text{ yr}^{-1}$$

- ② Oklo at $z \approx 0.16$,

$$\frac{|\Delta\alpha|}{\alpha} < 1.1 \times 10^{-8}$$

- ③ ^{187}Re meteorite at $z \approx 0.43$,

$$\frac{\Delta\alpha}{\alpha} = (-8 \pm 8) \times 10^{-7}$$

- ④ CMB at $z \simeq 10^3$

$$\frac{\Delta\alpha}{\alpha} = (3.6 \pm 3.7) \times 10^{-3}$$

Astrophysical constraints on the evolution of α

- ① Keck/ HIRES141 absorbers (MM method) [M.T. Murphy et al. 2004]
- ② VLT/ UVES154 absorbers (MM method) [J.A. King et al. 2012]
- ③ Keck/ HIRES Si IV absorption systems (AD method) [M.T. Murphy et al. 2001]
- ④ Comparison of HI 21 cm line with molecular rotational absorption spectra [M.T. Murphy et al. 2001]
- ⑤ 11 UVES absorbers [P. Molaro et al. 2013, T.M. Evans et al. 2014]

Is the evolution of ϕ compatible with constraints on the evolution of α ?

$$\mathcal{S} = \int d^4x \sqrt{-g} \left(\frac{1}{2} R - \frac{1}{2} g^{\mu\nu} \partial_\mu \phi \partial_\nu \phi - V(\phi) \right) + S_{\text{matter}}(\tilde{g}_{\mu\nu}^{(m)})$$

with the equation of motion

$$\begin{aligned} \ddot{\phi} + 3H\dot{\phi} + V' &= Q_m + Q_r, \\ \dot{\rho}_m + 3H(\rho_m + p_m) &= -Q_m\dot{\phi}, \\ \dot{\rho}_r + 3H(\rho_r + p_r) &= -Q_r\dot{\phi}, \end{aligned}$$

where Q_m and Q_r are complicated functions of ρ_m , ρ_r , $\dot{\phi}$, C_r , C_m , D_r , D_m and their field derivatives.

Couplings and parameters

We specify to exponential couplings and potential and to linear direct coupling $h(\phi)$:

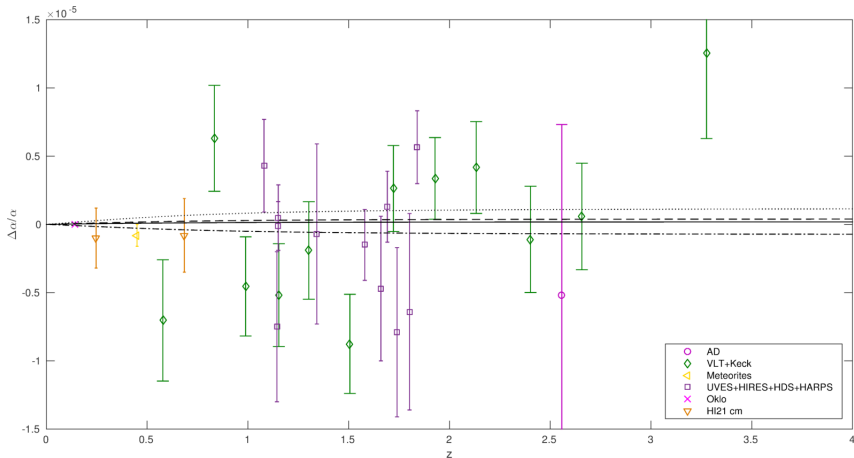
$$\begin{aligned}C_i(\phi) &= \beta_i e^{x_i \phi}, & D_i(\phi) &= M_i^{-4} e^{y_i \phi}, \\h(\phi) &= 1 - \zeta(\phi - \phi_0), & V(\phi) &= M_V^4 e^{-\lambda \phi}.\end{aligned}$$

Parameters x_i , y_i , λ , β_i , M_i , M_V and ζ are tuned such that their are in agreement with constraints on α and on the cosmological parameters from Planck.

Parameter	Estimated value
$w_{0,\phi}$	-1.006 ± 0.045
H_0	$(67.8 \pm 0.9) \text{ km s}^{-1} \text{ Mpc}^{-1}$
$\Omega_{0,m}$	0.308 ± 0.012

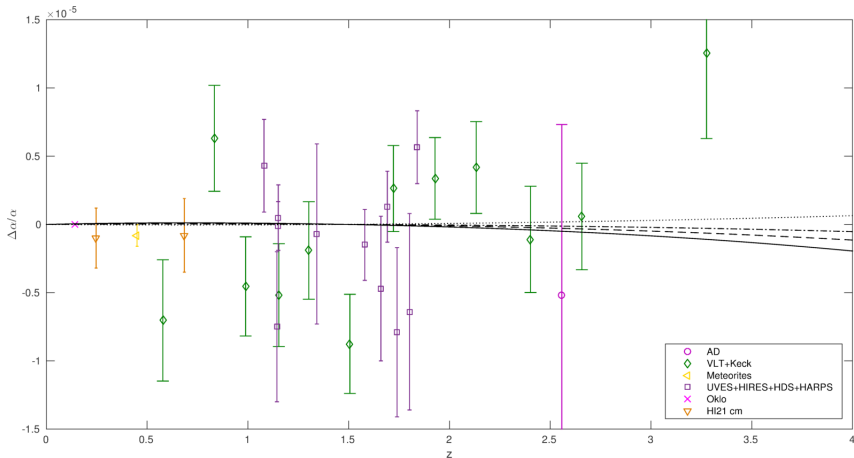
Disformal and electromagnetic couplings

M_r	M_m	M_V	β_m	x_m	$ \zeta $	λ
$\sim 1 \text{ meV}$	$\sim 1 \text{ meV}$	2.69 meV	1	0	$< 5 \times 10^{-6}$	0.45



Disformal and conformal couplings

M_r	M_m	M_V	β_m	x_m	$ \zeta $	λ
25-27 meV	15 meV	2.55 meV	8	0.14	0	0.45



- ① A variation in the fine-structure constant can be induced by disformal couplings provided that the radiation and matter disformal coupling strengths are not identical.
- ② Such a variation is enhanced in the presence of the usual electromagnetic coupling.
- ③ Laboratory measurements with molecular and nuclear clocks are expected to increase their sensitivity to as high as 10^{-21} yr^{-1} .
- ④ Better constrained data is expected from high-resolution ultra-stable spectrographs such as PEPSI at the LBT, ESPRESSO at the VLT and ELT-Hires at the E-ELT.

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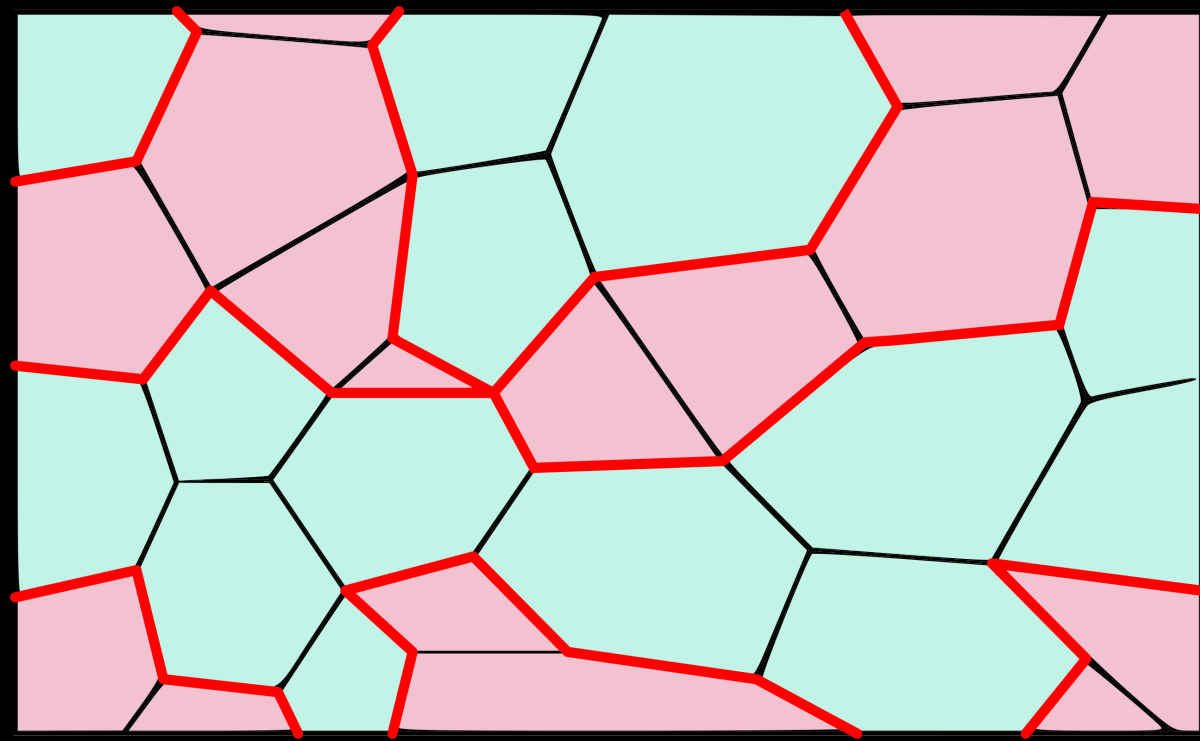
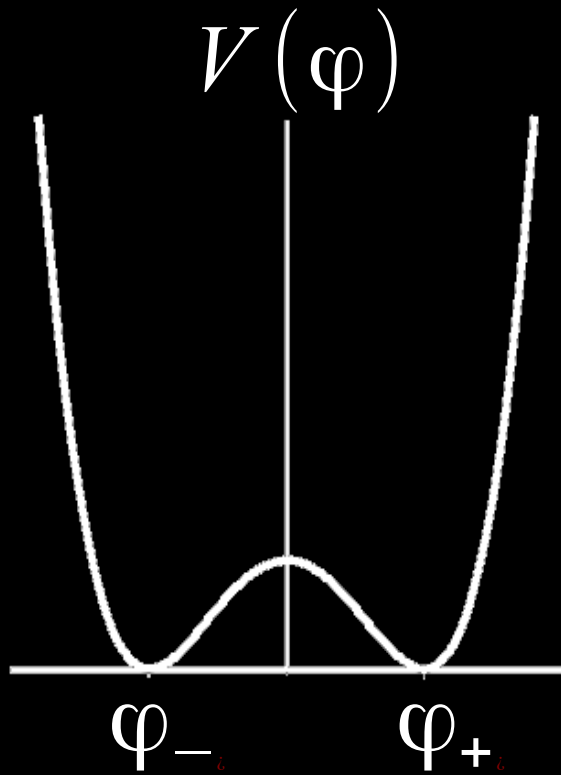
COSMIC MICROWAVE BACKGROUND ANISOTROPIES GENERATED BY DOMAIN WALL NETWORKS

Lara Sousa

Instituto de Astrofísica e Ciências do Espaço

DOMAIN WALLS

DOMAIN WALLS ARE FORMED WHEN DISCRETE SYMMETRIES ARE SPONTANEOUSLY BROKEN IN PHASE TRANSITIONS.



DOMAIN WALLS!

DOMAIN WALL CMB Q&A

WHY?

- FOR EXISTING!
- REPULSIVE GRAVITY

HOW?

ACTIVE GENERATION
OF PERTURBATIONS.

WHAT DOES IS MEAN?
SIGNIFICANT VECTOR
CONTRIBUTIONS

WHERE?

- SUBDOMINANT
CONTRIBUTIONS TO THE
TEMPERATURE AND E-
MODES
- POSSIBLY SIGNIFICANT
B-MODE CONTRIBUTION

CMBACT CODE

PHENOMENOLOGICAL APPROACH:

ENERGY-MOMENTUM TENSOR IS CALCULATED USING THE **UNCONNECTED SEGMENT MODEL**:

- SET OF UNCORRELATED STRAIGHT STRING SEGMENTS;
- RANDOMLY DISTRIBUTED AND MOVING IN RANDOM DIRECTIONS;
- A FRACTION OF SEGMENTS DECAY IN EACH EPOCH (ENERGY LOSS DUE TO INTERACTIONS);
- LENGTH AND VELOCITY OF THE SEGMENTS ARE DEFINED USING THE VOS MODEL;

CMBACT CODE

PHENOMENOLOGICAL APPROACH:

ENERGY-MOMENTUM TENSOR IS CALCULATED USING THE **UNCONNECTED SECTION MODEL**:

- SET OF UNCORRELATED **FLAT AND SQUARE DOMAIN WALL SECTIONS**;
- RANDOMLY DISTRIBUTED AND MOVING IN RANDOM DIRECTIONS;
- A FRACTION OF **SECTIONS** DECAY IN EACH EPOCH (ENERGY LOSS DUE TO INTERACTIONS);
- **AREA** AND VELOCITY OF THE **SECTIONS** ARE DEFINED USING THE VOS MODEL;

ENERGY-MOMENTUM TENSOR

WE NEED TO COMPUTE THE ENERGY-MOMENTUM TENSOR FOR EACH OF THESE SECTIONS.

WORLD-VOLUME

$$x^\mu = x^\mu(\xi^a), \quad \text{WITH } a=0,1,2$$

NAMBU-GOTO ACTION: $S = -\sigma \int d^3\xi \sqrt{-h}$



$$T_{\mu\nu} \sqrt{-g} = \sigma \int d^3\xi \delta^4[x^\mu - x^\mu(\xi^a)] \sqrt{-h} h^{ab} x_{,a}^\mu x_{,b}^\nu$$

ENERGY-MOMENTUM TENSOR

FORTUNATELY, IN THIS CASE

$$\underline{x} = \underline{x}_0 + \xi_1 \hat{x}'^{(1)} + \xi_2 \hat{x}'^{(2)} + v \tau \dot{\underline{x}}$$

ANALYTICAL SOLUTIONS:

$$\theta_{00} = 4 \sigma \gamma \sqrt{2} \cos(\underline{k} \cdot \underline{x} + v k \tau) \frac{\sin(k l \hat{x}_3'^{(1)} / 2) \sin(k l \hat{x}_3'^{(2)} / 2)}{k^2 \hat{x}_3'^{(1)} \hat{x}_3'^{(2)}}$$

$$\theta_{ij} = \theta_{00} [v^2 \dot{\hat{x}}_i \dot{\hat{x}}_j - (1 - v^2) \hat{x}_i'^{(1)} \hat{x}_j'^{(1)} + \hat{x}_i'^{(2)} \hat{x}_j'^{(1)}]$$

ENERGY-MOMENTUM TENSOR

WE NOW HAVE 3 OF THE E-M COMPONENTS
REQUIRED BY CMBFAST:

$$2\theta_s = \theta_{00} \left[v^2 (3 \dot{\hat{x}}_3 \dot{\hat{x}}_3 - 1) - (1 - v^2) (3 \hat{x}_3'^{(1)} \hat{x}_3'^{(1)} + 3 \hat{x}_3'^{(2)} \hat{x}_3'^{(2)} - 2) \right]$$

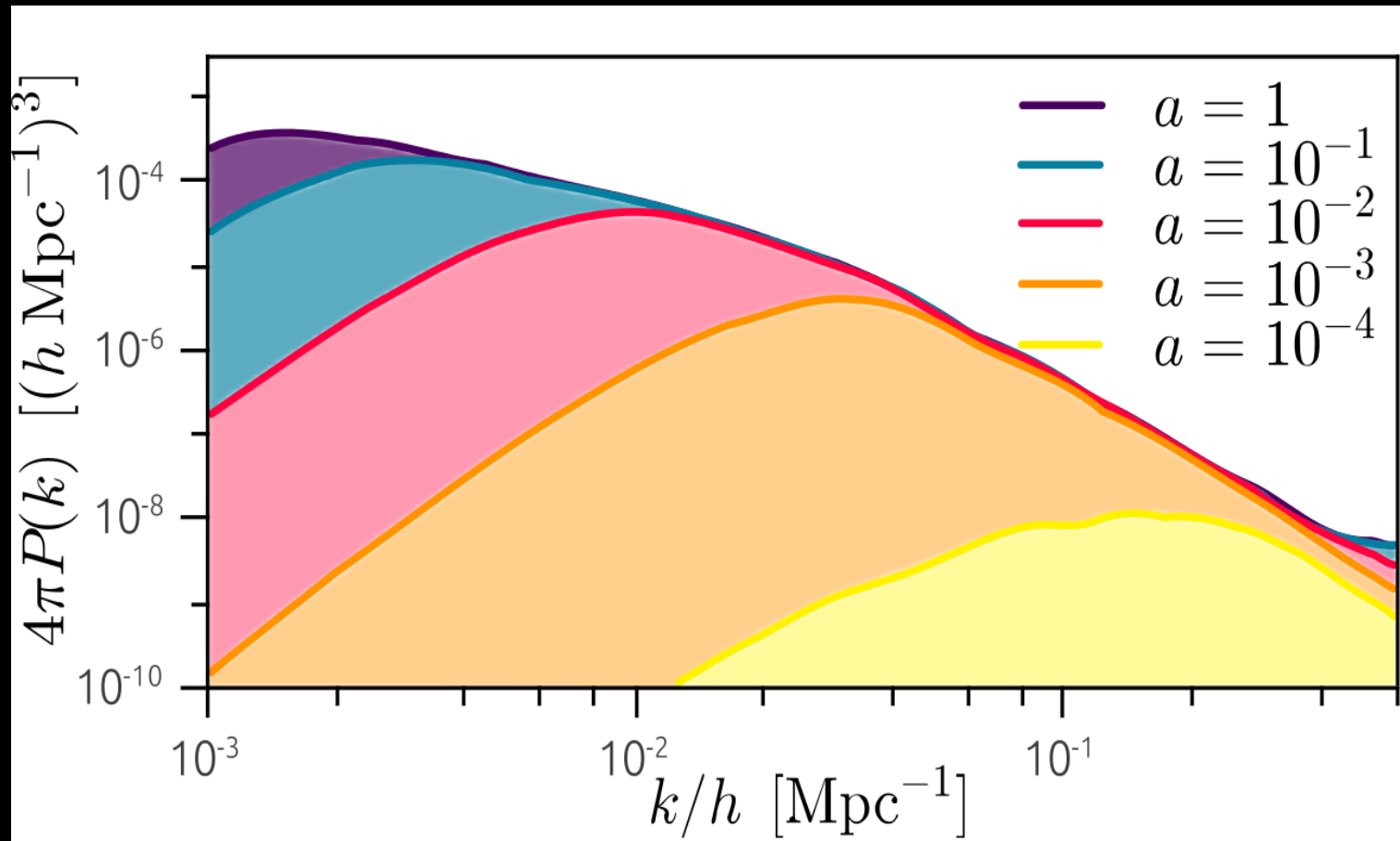
$$\theta_V = \theta_{00} \left[v^2 \dot{\hat{x}}_1 \dot{\hat{x}}_3 - (1 - v^2) (\hat{x}_1'^{(1)} \hat{x}_3'^{(1)} + \hat{x}_1'^{(2)} \hat{x}_3'^{(2)}) \right]$$

$$\theta_T = \theta_{00} \left[v^2 \dot{\hat{x}}_1 \dot{\hat{x}}_2 - (1 - v^2) (\hat{x}_1'^{(1)} \hat{x}_2'^{(1)} + \hat{x}_1'^{(2)} \hat{x}_2'^{(2)}) \right]$$

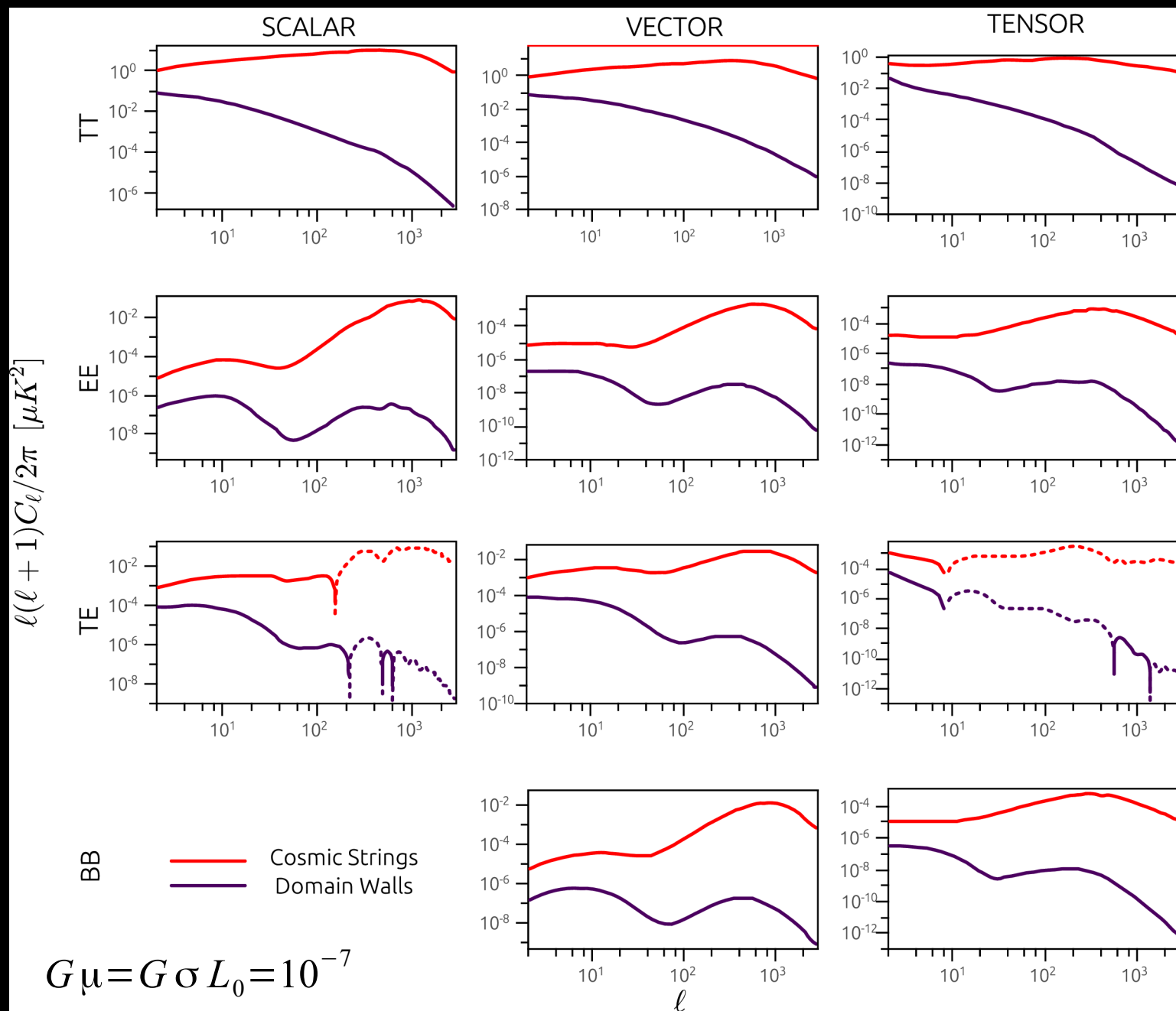
THE REST FOLLOWS FROM E-M CONSERVATION...

THE RESULTS: CDM POWER SPECTRUM

DOMAIN WALLS CONTRIBUTE MOSTLY ON LARGE SCALES...



THE RESULTS: CMB SPECTRA



THE RESULTS: CONSTRAINTS

THERE IS STILL OBSERVATIONAL ROOM FOR
DOMAIN WALLS:

FRACTIONAL
CONTRIBUTION TO THE TT-
POWER SPECTRUM

$$f_{dw} < 0,2$$

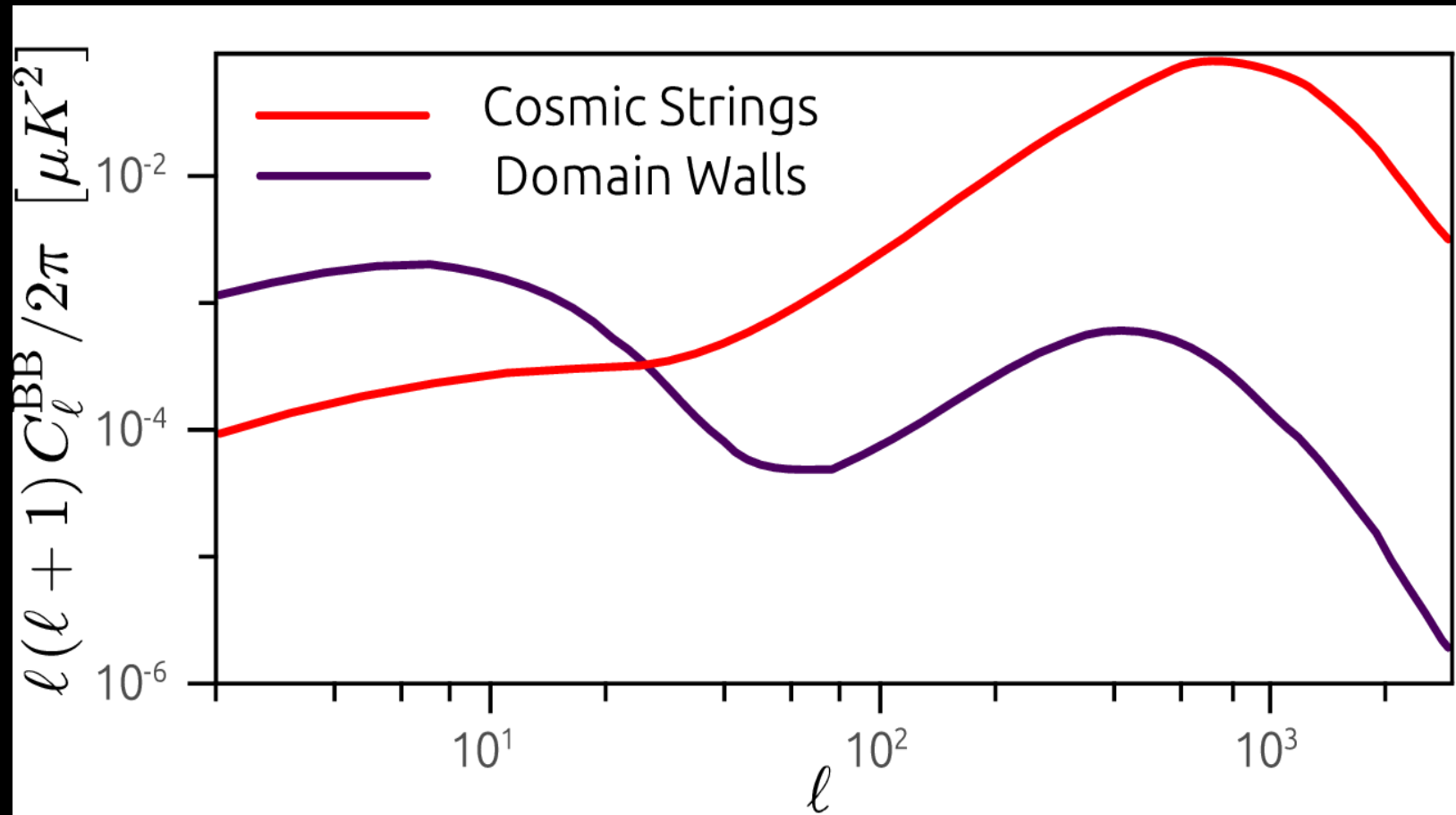


ENERGY SCALE OF THE
DOMAIN-WALL-FORMING
PHASE TRANSITION

$$\eta < 0,92 \text{ MeV}$$

THE RESULTS: CONSTRAINTS

... AND THEY MAY PRODUCE SIGNIFICANT B-MODES!



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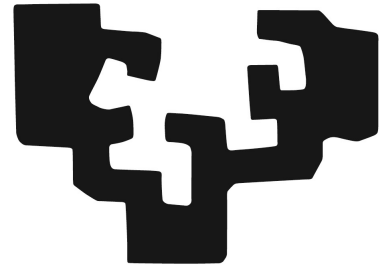
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ZTF-FCT

Evolution of Semilocal String Networks:

Segment Evolution

Asier Lopez-Eiguren (UPV/EHU)

Vila do Conde, 30/03/16

In collaboration with: A.Achúcarro, A.Avgoustidis, C.J.A.P. Martins, A.S. Nunes, J. Urrestilla

Evolution of String Networks

TWO methods to analyse the evolution:

NUMERICAL SIMULATIONS

- Evolve true eom
- High computational cost
- Limited dynamical range

ANALYTIC MODELS

- Approximate models
- Simple
- More tractable
- Need input from Num. Sim.

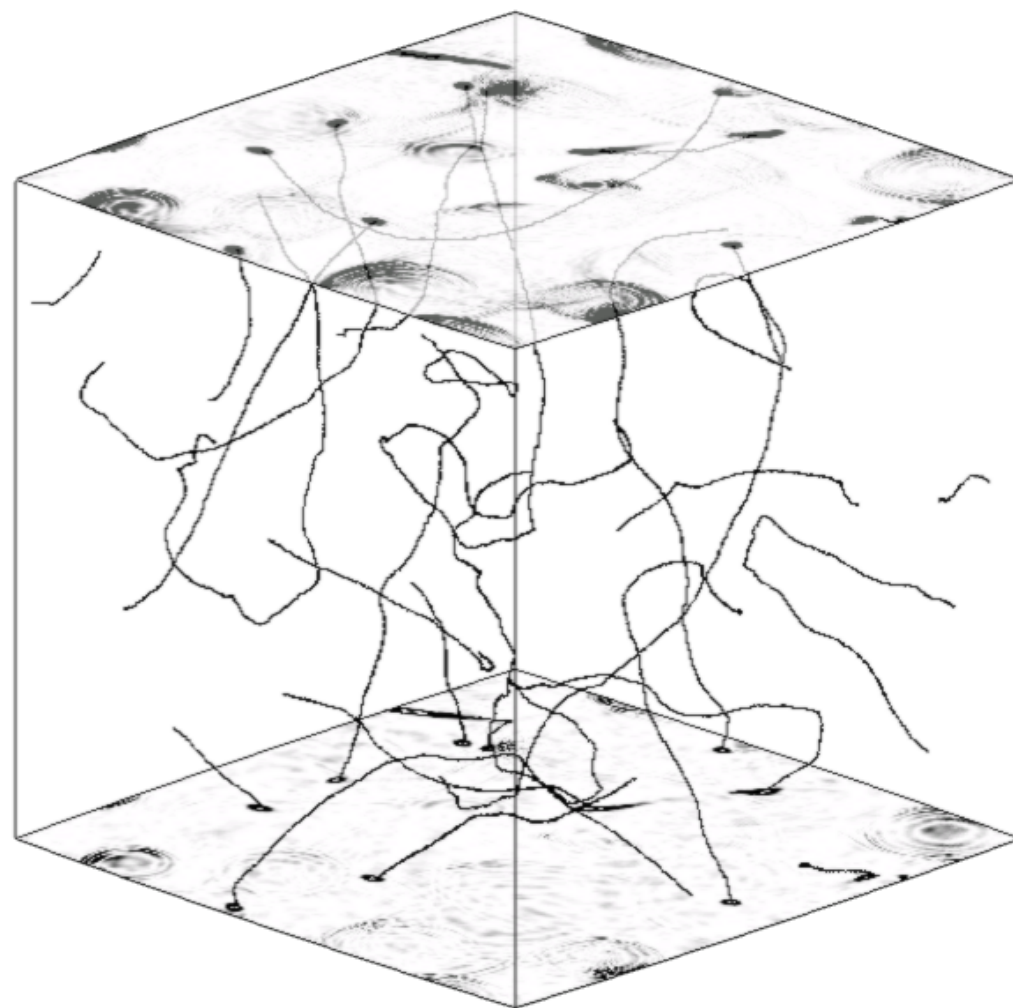
OBJECTIVE: CALIBRATE analytic models for SL

Semilocal Strings

(A. Achúcarro & Vachaspati 1999)

- Extension of Abelian-Higgs (AH):
 $U(1)_I \rightarrow SU(2)_g \times U(1)_I$
- They are not topological
 - They can have ends
- Their ends are effectively global monopoles

Abelian-Higgs



Semilocal

Semilocal Strings

(A. Achúcarro & Vachaspati 1999)

$$\mathcal{S} = \int d^4x \left\{ \left[\left(\partial_\mu - iA_\mu \right) \Phi \right]^2 - \frac{1}{4} F^2 - \frac{\beta}{4} (\Phi^\dagger \Phi - \eta^2)^2 \right\}$$

$$\Phi = (\phi, \psi), F^2 = F_{\mu\nu} F^{\mu\nu} \text{ and } F_{\mu\nu} = (\partial_\mu A_\nu - \partial_\nu A_\mu)$$

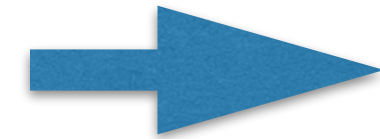
- The stability of the strings depends on the parameter $\beta = m_{\text{scalar}}^2/m_{\text{gauge}}^2$:
 - $\beta > 1$ Unstable
 - $\beta = 1$ Neutrally stable
 - $\beta < 1$ Stable
- For lower β they behave more like AH

Velocity-one-scale Model

(Martins & Shellard 1996,2002)

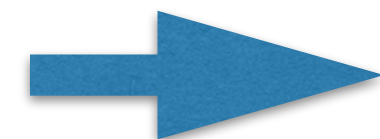
- Two variables:

RMS VELOCITY



$$\frac{dv}{dt} = (1 - v^2) \left(\frac{k}{L} - \frac{v}{l_d} \right)$$

TYPICAL LENGTH SCALE
INTERDEFECT DISTANCE



$$(4 - n) \frac{dL}{dt} = (4 - n) H L + v^2 \frac{L}{l_d} + cv$$

$n = \text{dim. of defect}$

$$L^{4-n} = \frac{M}{\rho} \quad M \sim \rho^n$$

Damping scale

$$\frac{1}{l_d} = nH + \frac{1}{l_f}$$

particle friction

Semilocal VOS Models

Hybrid Networks: strings + monopoles

$$\frac{dl_s}{dt} = Hl_s - v_s^2 \frac{l_s}{l_d} + \sigma \left(1 - \frac{L}{l_s}\right) v_m^2$$

$$\frac{dv_s}{dt} = (1 - v_s^2) \left[\frac{k}{l_s} + f_s - \frac{v_s}{l_d} \right]$$

Model A

$$\frac{dl_s}{dt} = Hl_s - v_s^2 \frac{l_s}{l_d} + \left(d \frac{v_s l_s}{L} - k_1 \right)$$

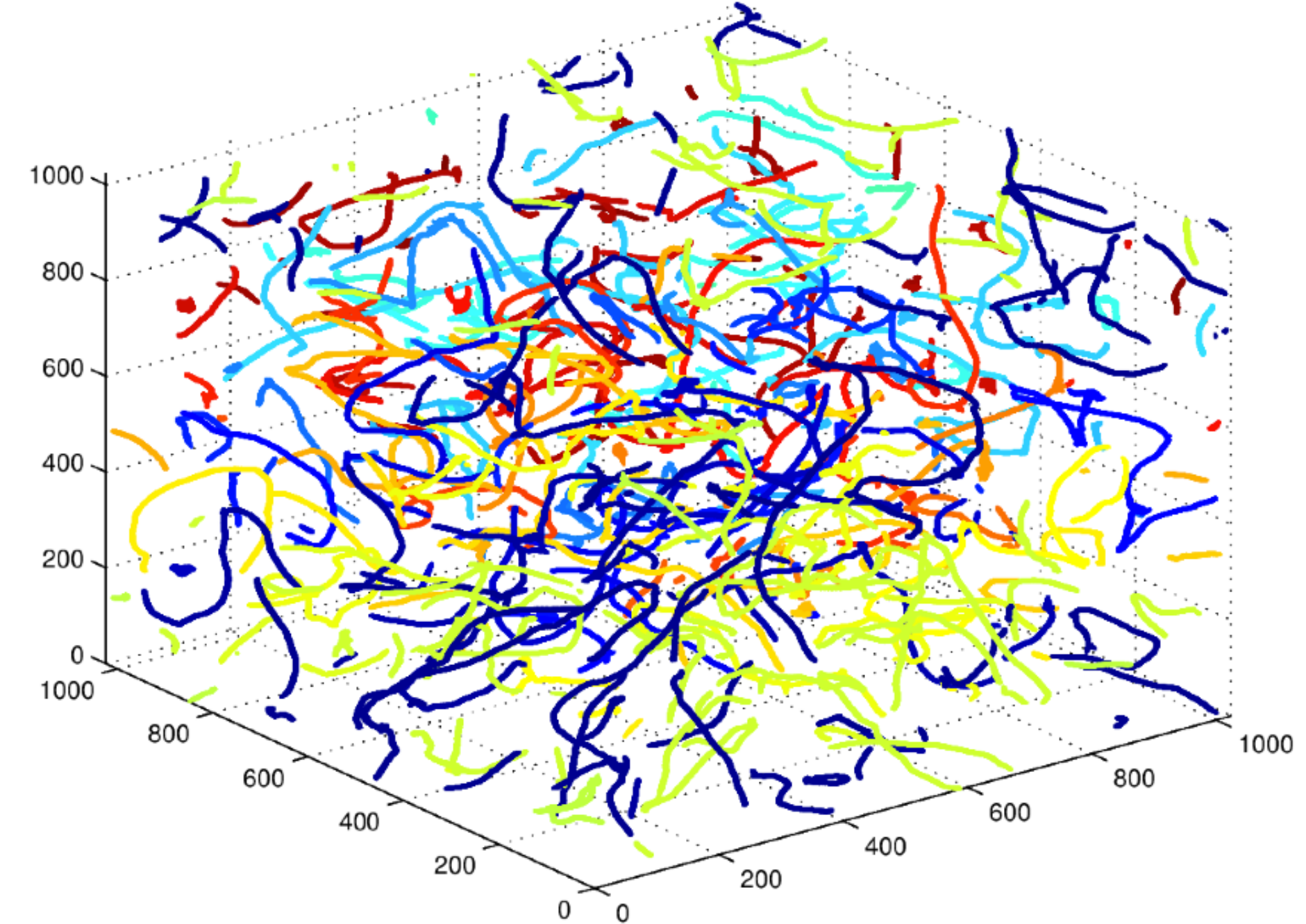
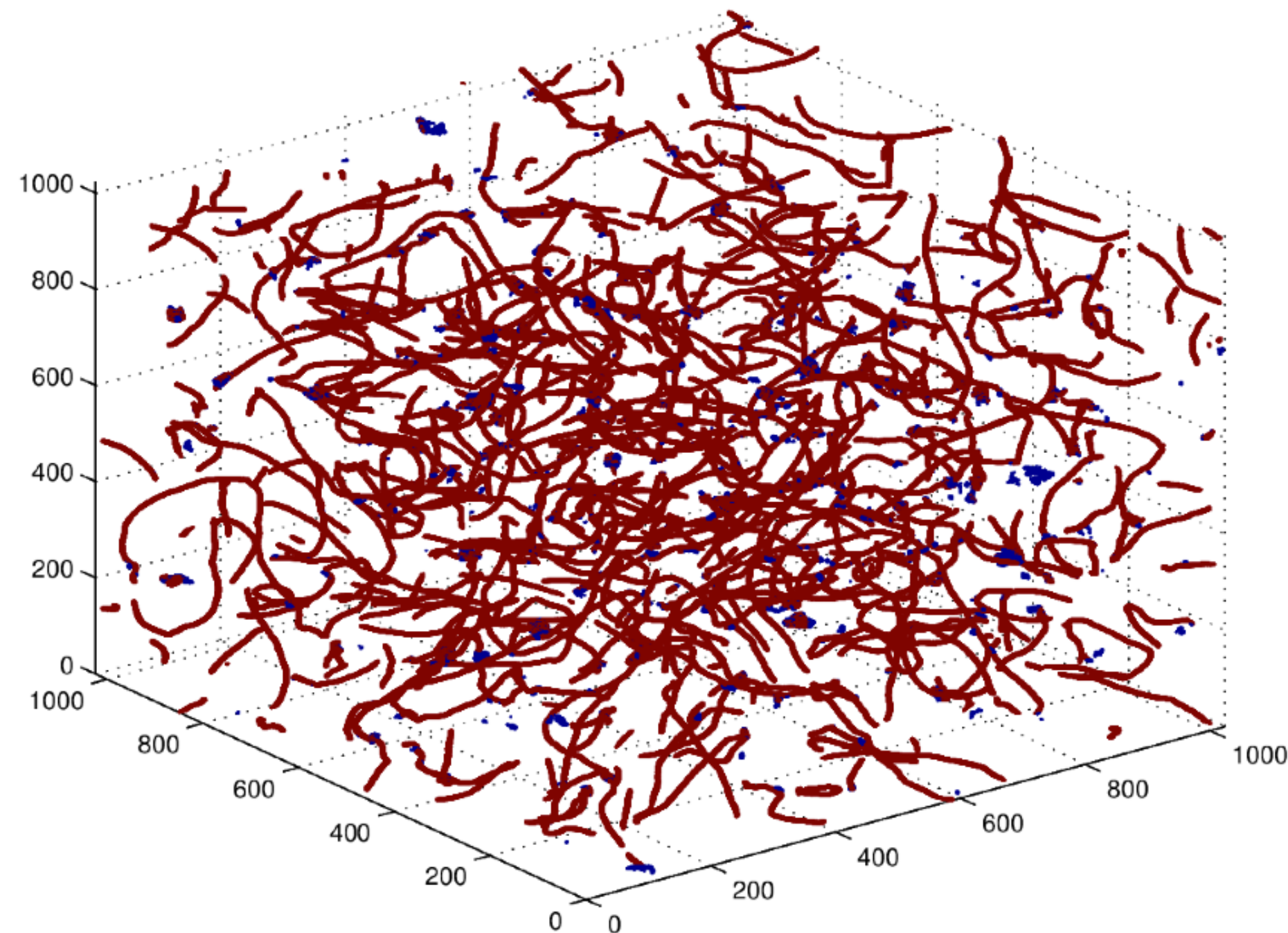
$$\frac{dv_s}{dt} = (1 - v_s^2) \left[\frac{k}{l_s} - \frac{v_s}{l_d} \right]$$

Model B

- Compare simulations with analytic models
- Obtain the best values for the parameters

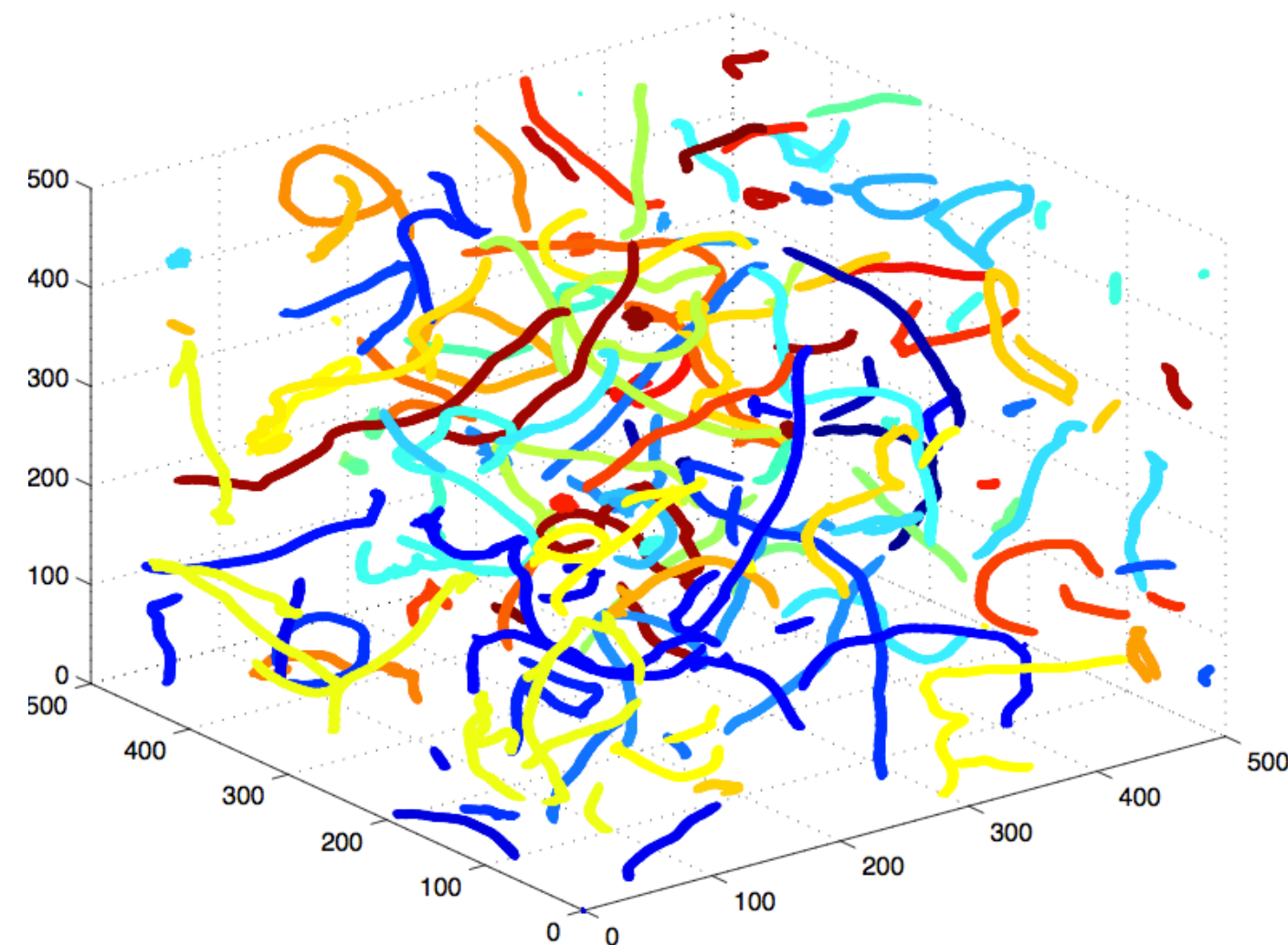
Field Theory Simulations

- 1024^3 lattices in radiation and matter eras in expanding universe
- Magnetic energy to detect strings

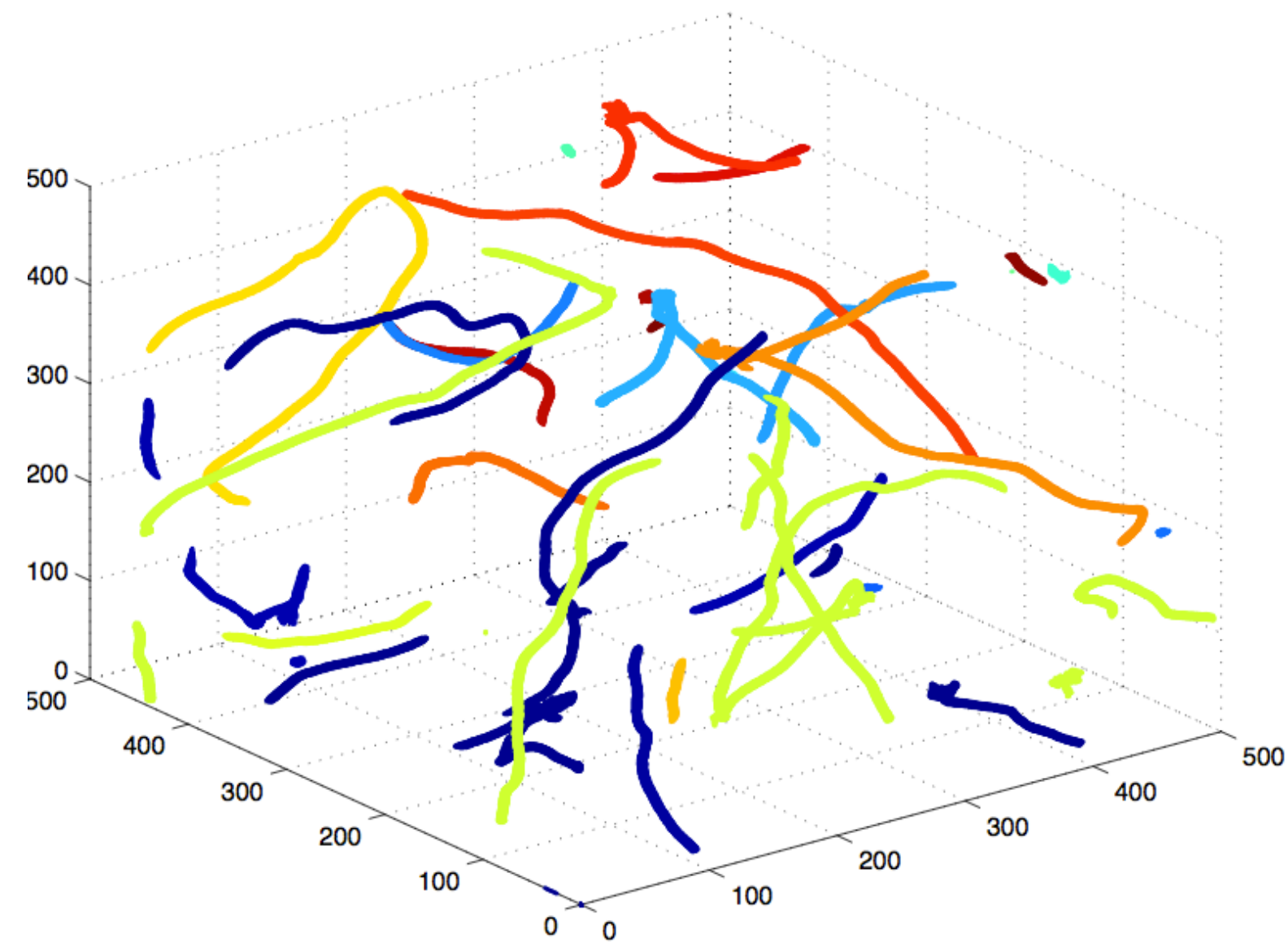


[arXiv:1312.2123/PhysRevD.89.063503](https://arxiv.org/abs/1312.2123):
Large Scale properties were analysed

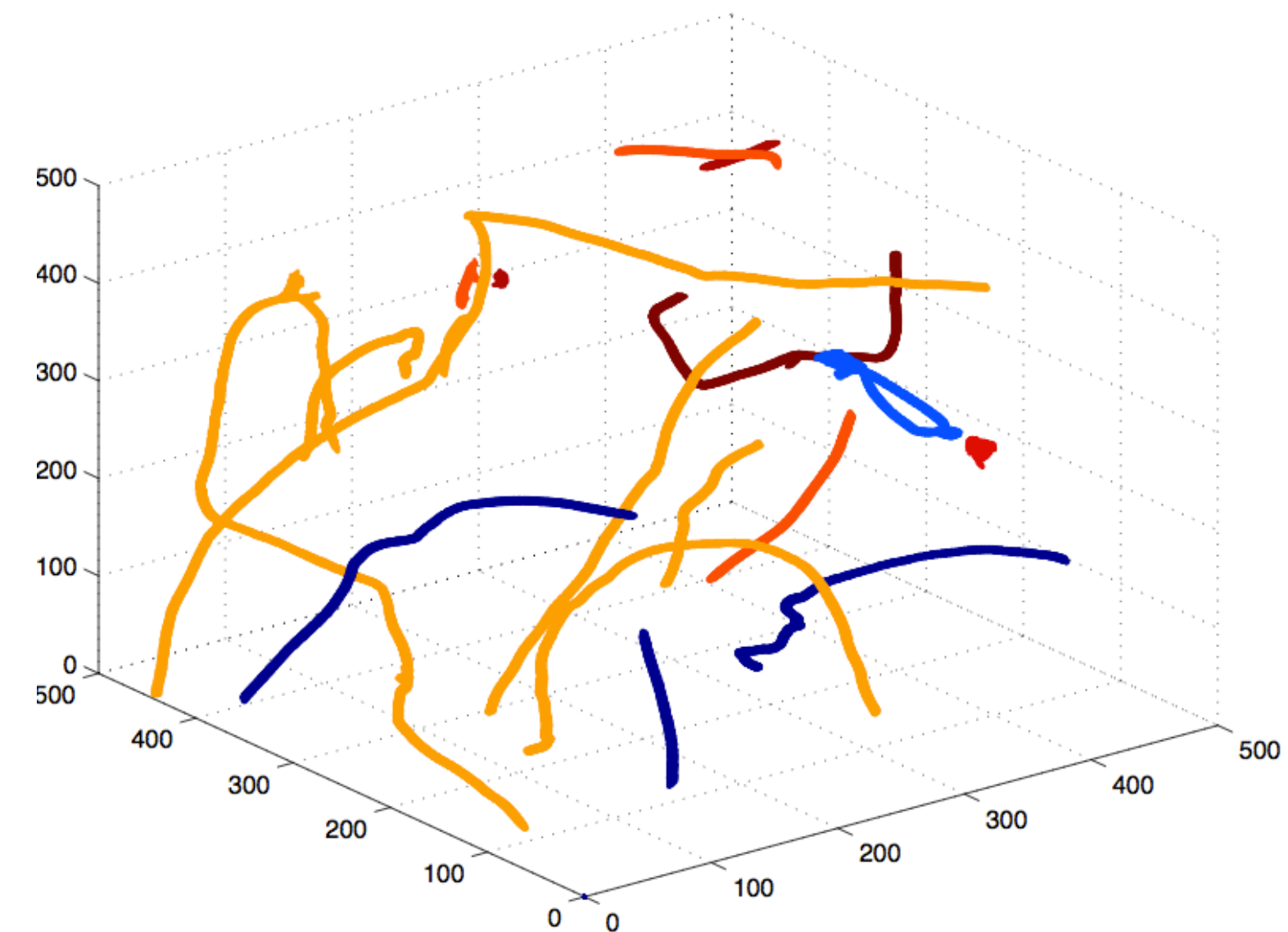
Field Theory Simulations



$\tau=150$



$\tau=300$



$\tau=450$

Segment Distribution

Initial I_s seed from **simulations**

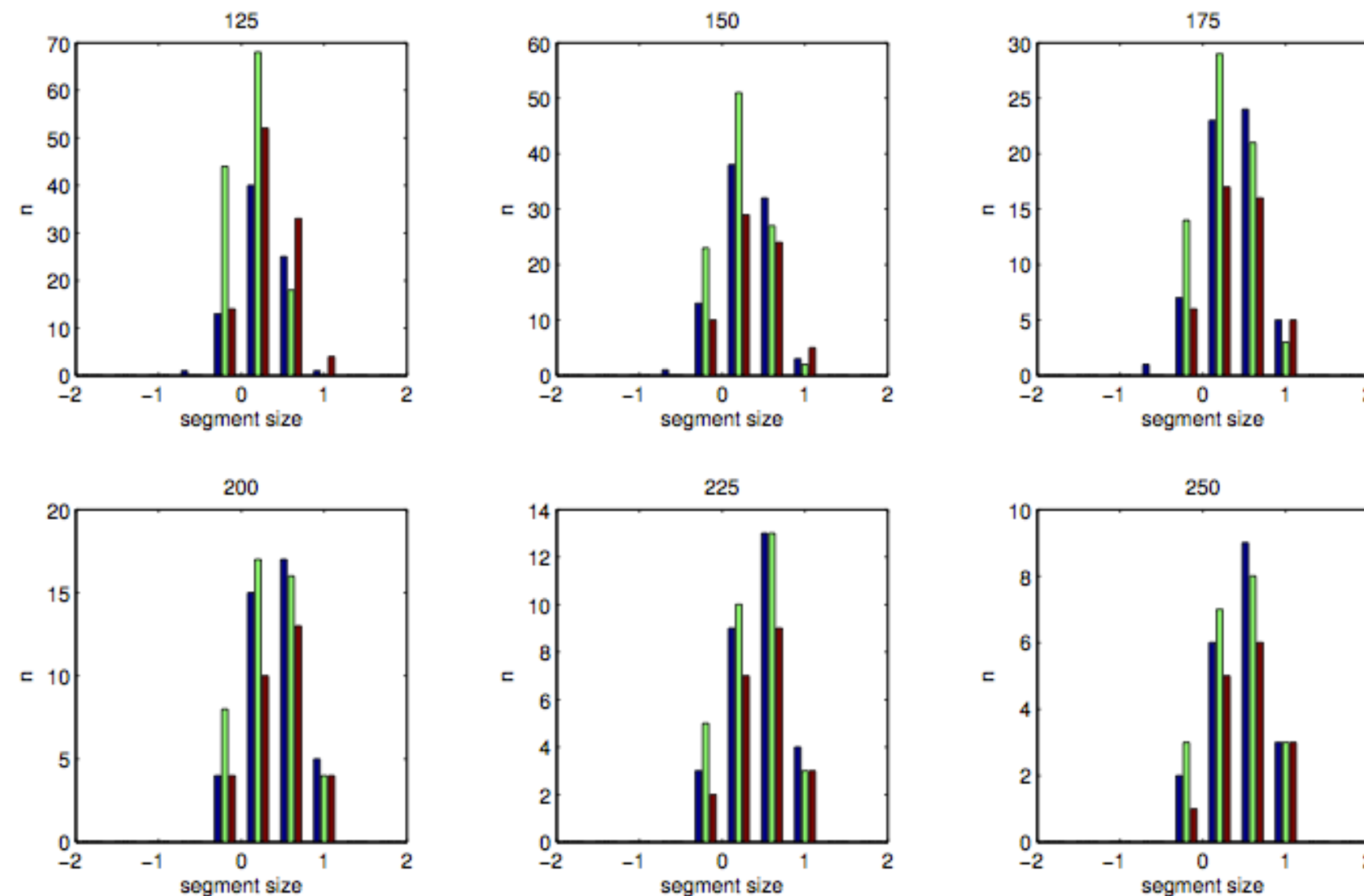
Phenomenological v_s distribution

Evolve VOS models

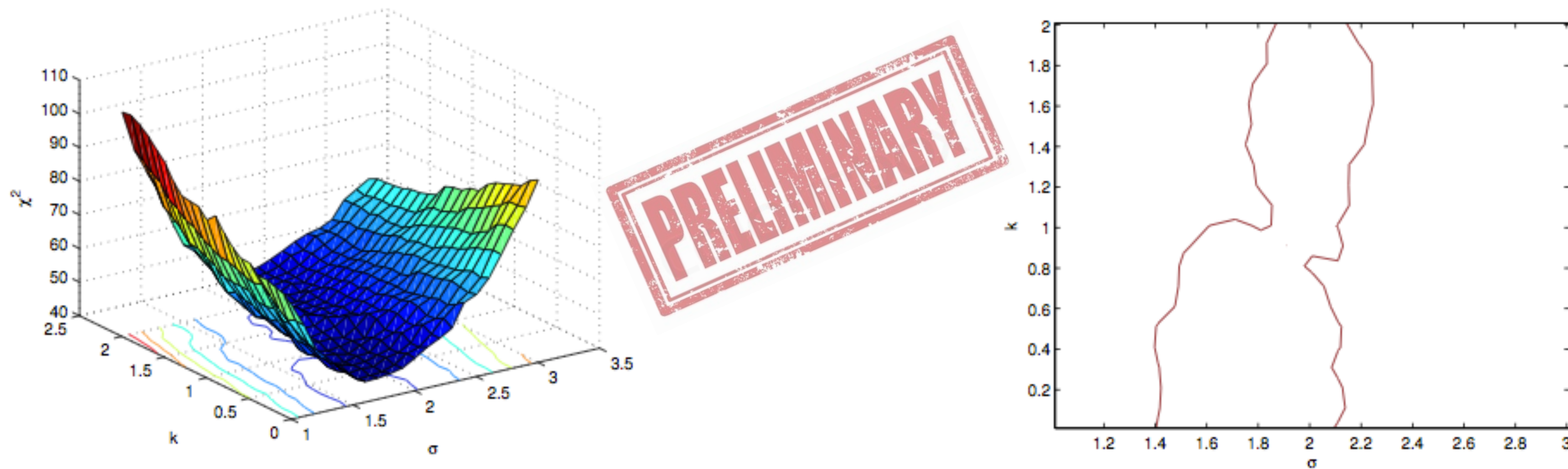
Model A

Model B

Simulations



Segment Distribution



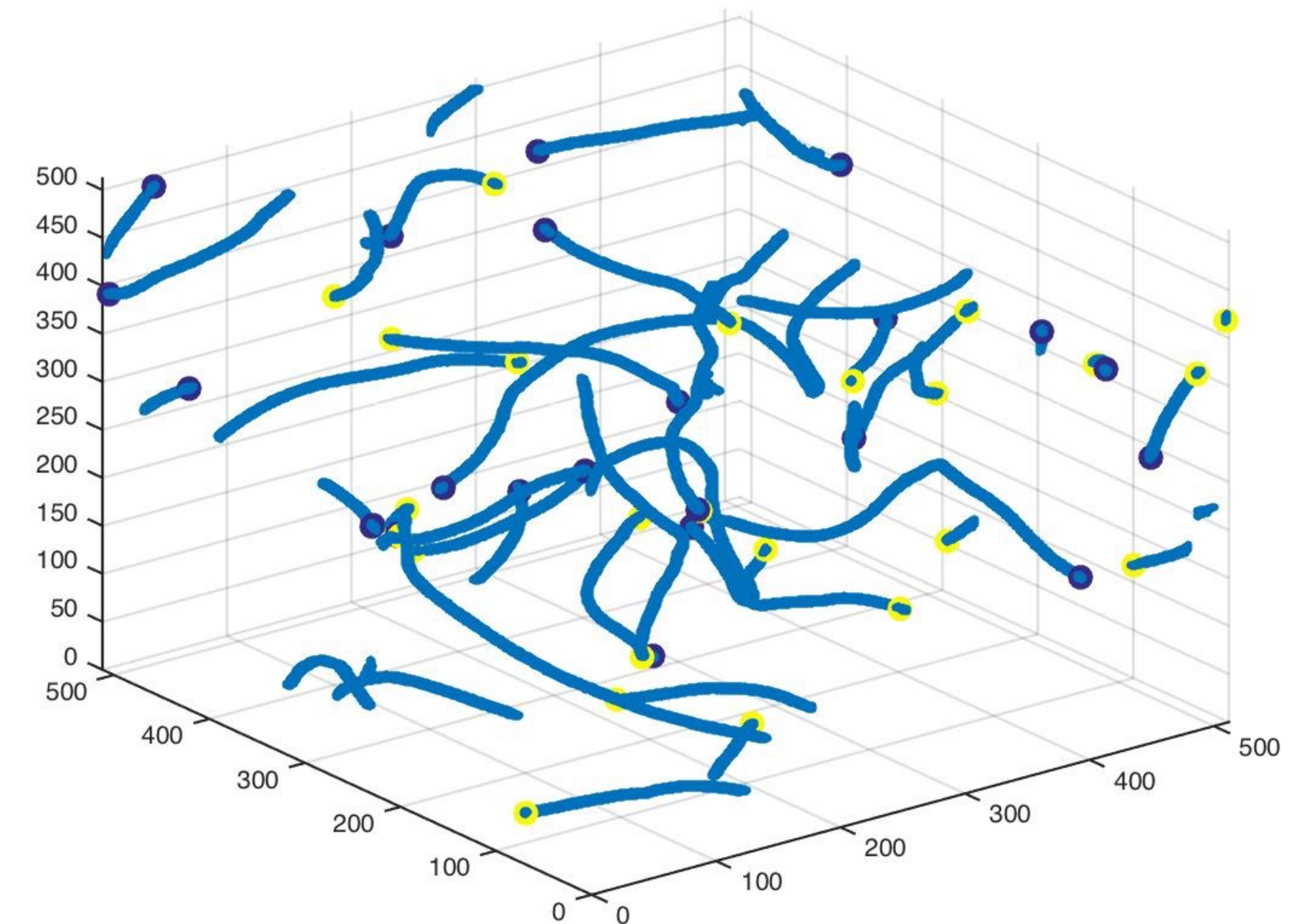
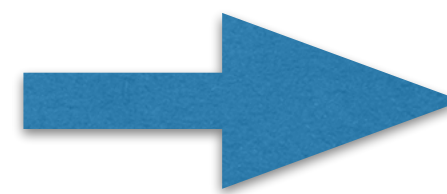
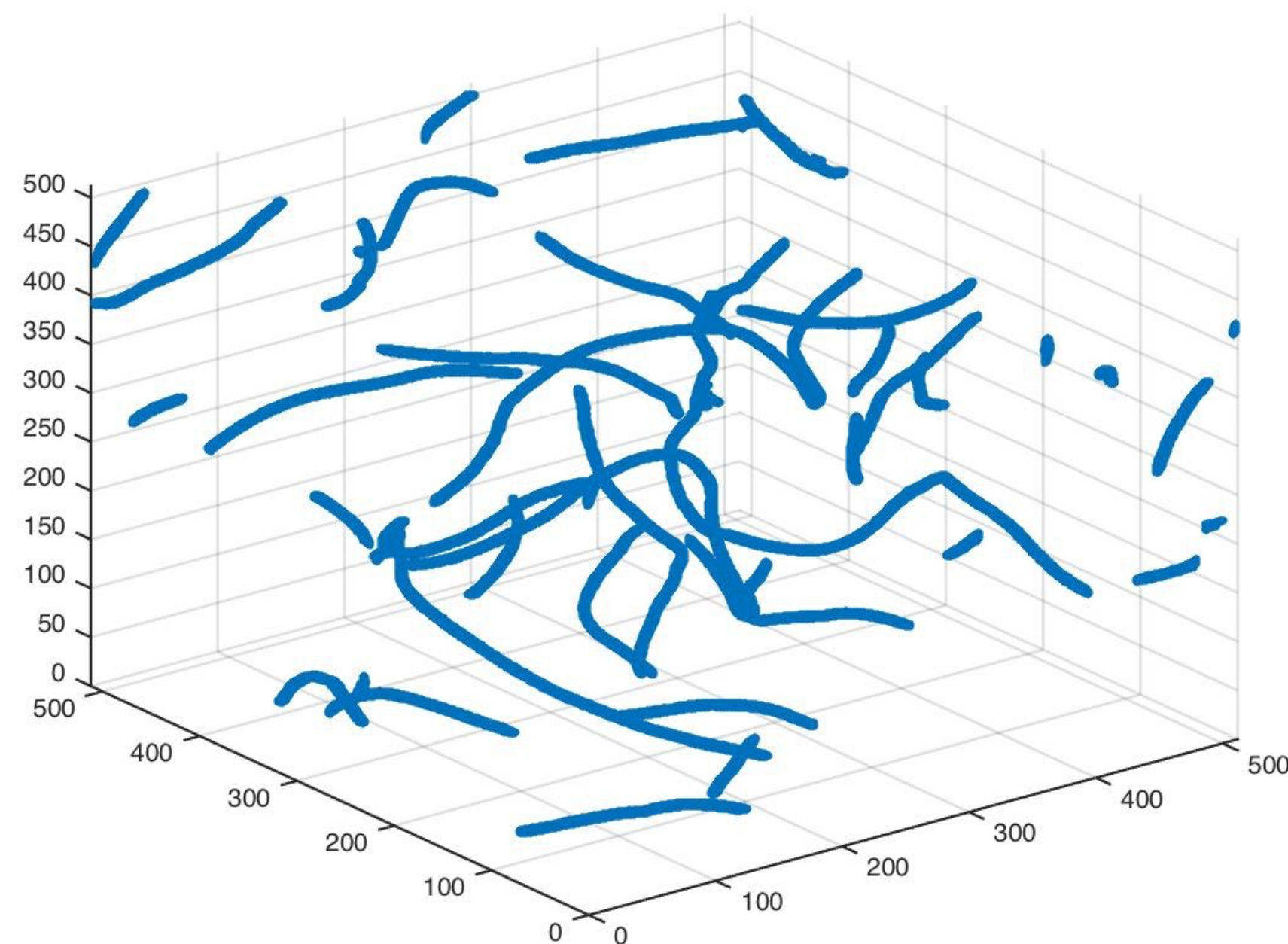
- We perform χ^2 analysis to determine the best values for the parameters

Summary

- TWO VOS models for Semilocal string networks
- We perform χ^2 analysis:
 - Determine the best values of the parameters
 - Conclude which model describes better the network

Future Work

- Improve parameter analysis:
 - Obtaining v_s distribution from simulations
 - Obtain segment end (monopole) velocities



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Extending the velocity-dependent one-scale model for domain walls.



I.Yu. Rybak,
CAUP, IA

in collaboration with
C.J.A.P. Martins,
A. Avgoustidis,
E.P.S. Shellard

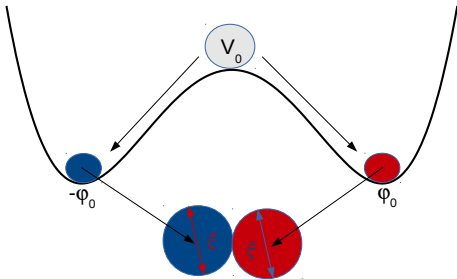
Phys.Rev.D93(2016)no.4,043534, ([arxiv\[hep-ph\] 1602.01322](#))

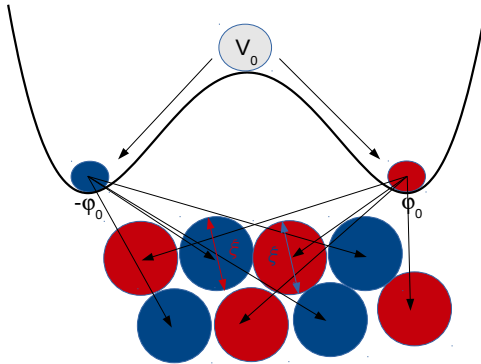
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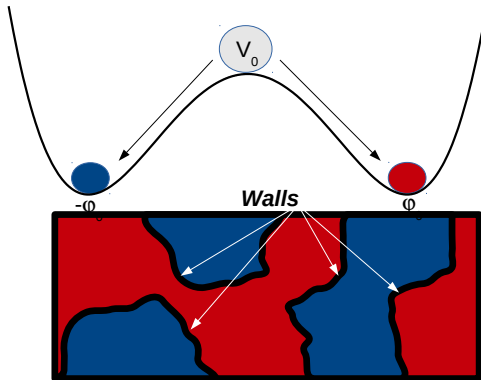
Kibble mechanism

[Kibble, J. Phys. A 9 (1976), 1387-1398] CTP/75/5]

$$L = \frac{1}{2} (\partial\varphi)^2 - V(\varphi)$$
$$V(\varphi) = V_0 \left(1 - \frac{\varphi^2}{\varphi_0^2}\right)^2$$







Field theory simulation (4096^3 boxes)

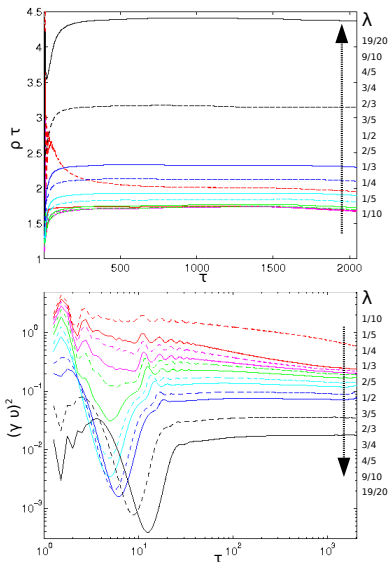
Scalar field model:

[Press, Ryden, Spergel, *Astrophys. J.* 347, 590 (1989)]

$$\frac{\partial^2 \phi}{\partial \tau^2} + 3 \frac{d \ln a}{d \ln \tau} \frac{\partial \phi}{\partial \tau} - \frac{\partial^2 \phi}{\partial x^i \partial x_i} = - \frac{\partial V}{\partial \phi},$$

Measured values (asymptotic):

- $(\gamma v)^2$ (v - velocity).
- ξ_c / τ (ξ_c - correlation length $\sim \frac{1}{\rho}$)
(for $a \sim t^\lambda$)



Velocity-depend one scale (VOS) model

Dirac-Nambu-Goto action: $S = -\sigma_w \int \sqrt{G} d^2\sigma d\tau,$

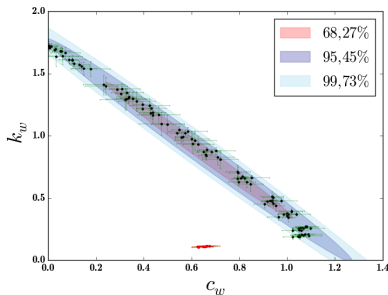
[Sousa, Avelino, Phys. Rev. D, 84, 063502 (2011)]

(averaged) $\Downarrow \int \dots d^2\sigma$

$$\frac{dL}{dt} = (1 + 3v^2) HL + c_w v,$$

$$\frac{dv}{dt} = (1 - v^2) \left(\frac{k_w}{L} - 3Hv \right),$$

Scaling solution is: $L = \epsilon t, v$ (ϵ, v - constants).



Momentum parameter for VOS model

From the microscopic description

$$k_w(v) = k_0 \frac{1 - (qv^2)^\beta}{1 + (qv^2)^\beta}$$

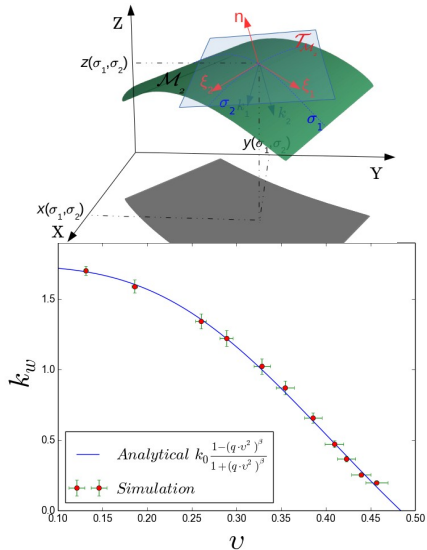
Physical restrictions:

- $0 \leq k_0 \leq 2$
- $0 < \frac{1}{q} \leq v_w^2 = \frac{2}{3}$

$$k_0 = 1.73 \pm 0.01,$$

$$q = 4.27 \pm 0.10 \quad (<v> \approx 0.48),$$

$$\beta = 1.69 \pm 0.08.$$



Energy loss for VOS model

Energy loss mechanisms:

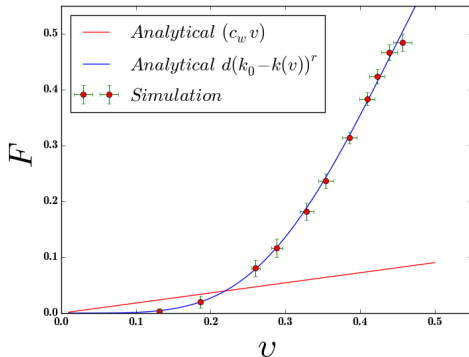
- creation of closed objects

$$c_w v$$

- scalar radiation ($\sim \text{curvature}^r$)

$$d [k_0 - k(v)]^r$$

$$r = 1.30 \pm 0.02, d = 0.28 \pm 0.01, c_w = 0.00 \pm 0.01.$$

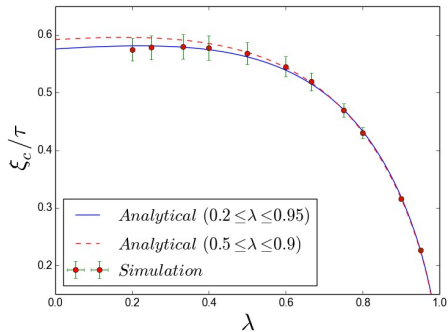
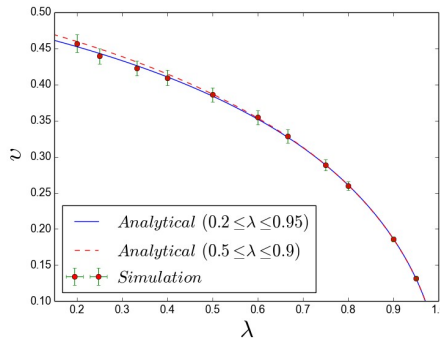


The whole model with found parameters

$$\frac{dL}{dt} = (1 + 3v^2) HL + c_w v + d (k_0 - k(v))^r,$$

$$\frac{dv}{dt} = (1 - v^2) \left(\frac{k(v)}{L} - 3Hv \right),$$

$$k(v) = k_0 \frac{1 - (qv^2)^\beta}{1 + (qv^2)^\beta}$$



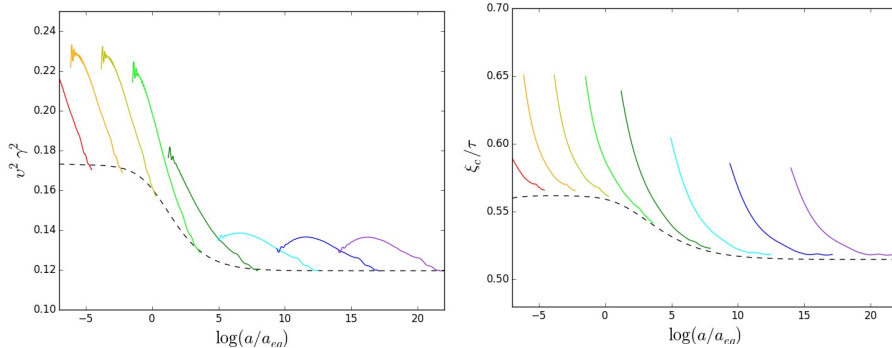
Radiation-matter transition

Scale factor

$$\frac{a(\tau)}{a_{eq}} = \left(\frac{\tau}{\tau_*}\right)^2 + 2\left(\frac{\tau}{\tau_*}\right),$$

where $\tau_* = \tau_{eq}/(\sqrt{2} - 1)$.

Simulations with different a_{eq} , τ_{eq} to span the entire transition



Results

- The largest currently available field-theory simulations;
- Adjustment of the VOS model;
- Direct comparison of energy loss mechanisms;
- Description of the radiation-matter transition by the extended VOS model;

Interesting avenues for further study

- To extend this analysis to the case of cosmic strings for better understanding the differences between Goto-Nambu and field theory simulations;

Thank you for your attention!

FCT

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